

# A Journey Through the “Clumpy” Universe

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In collaboration with:

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Daniel Holz (Los Alamos), Asantha Cooray (UCI).

Carnegie Mellon   McWilliams Center for Cosmology Lunch Seminar   November 21, '08



Dark Energy & Primordial non-Gaussianity  
with Future Generation Surveys:  
Weak Lensing on the Way

with a sneak-peek to

Detecting Gravity Waves with Weak  
Gravitational Lensing



# Agenda

## Dark Energy

- . Constrainíng the EOS
- . To Bín or Not to Bín
- . SNe Ia ++
- . Lensíng of SNe
- . Other Worríes

## Non-Gaussianíty

- . Beyond Gaussianíty
- . CMB Bíspectrum
- . Lensíng of CMB
- . Lensed Bíspectrum
- . S/N Redúction & Bías

Gravity Waves vía  
Weak Gravítational Lensíng



# Agenda

## Dark Energy

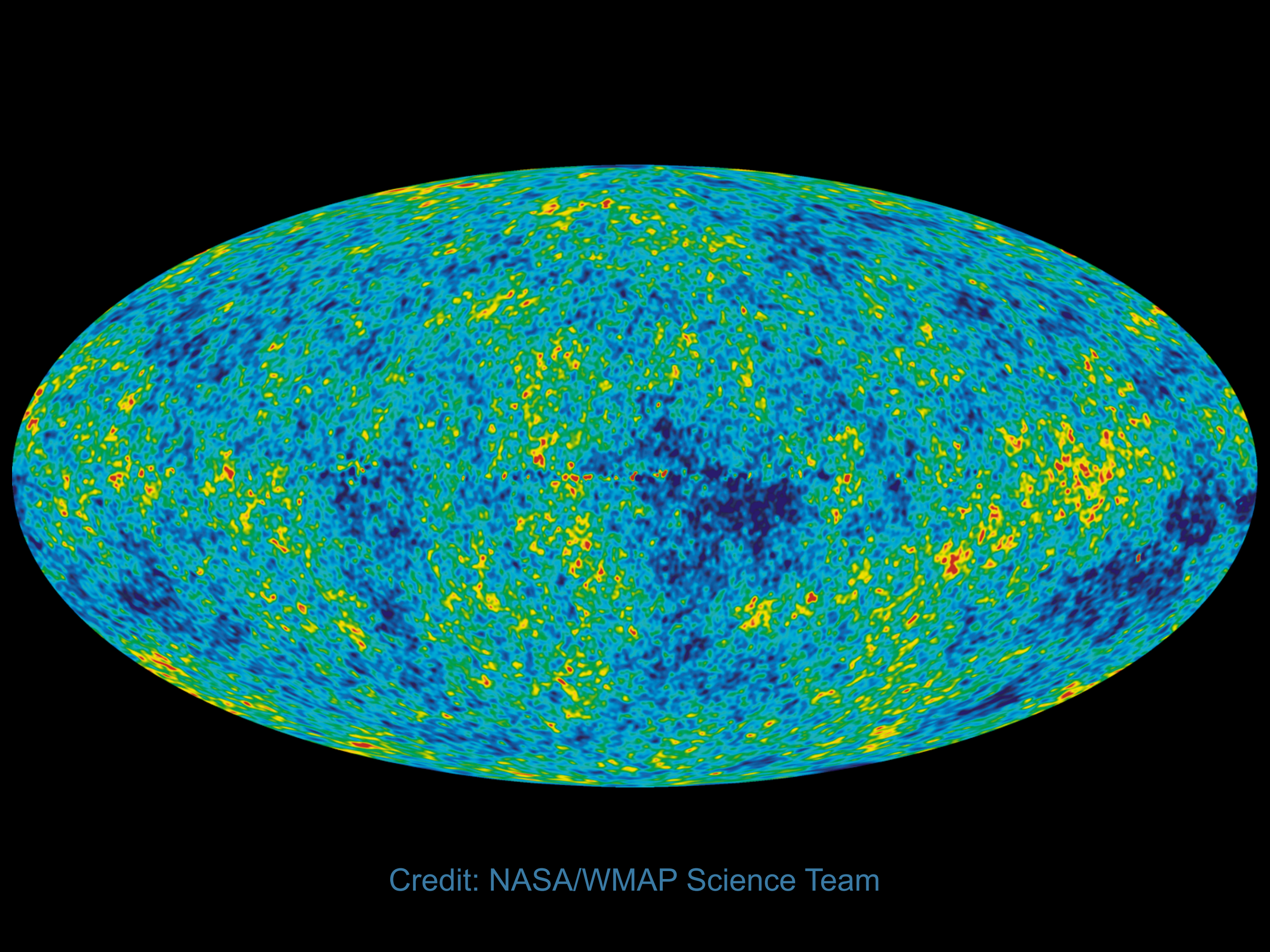
- . Constrain the EOS
- . To Bin or Not to Bin
- . SNe Ia ++
- . Lensing of SNe
- . Other Worries

## Non-Gaussianity

- . Beyond Gaussianity
- . CMB Bispectrum
- . Lensing of CMB
- . Lensed Bispectrum
- . S/N Reduction & Bias

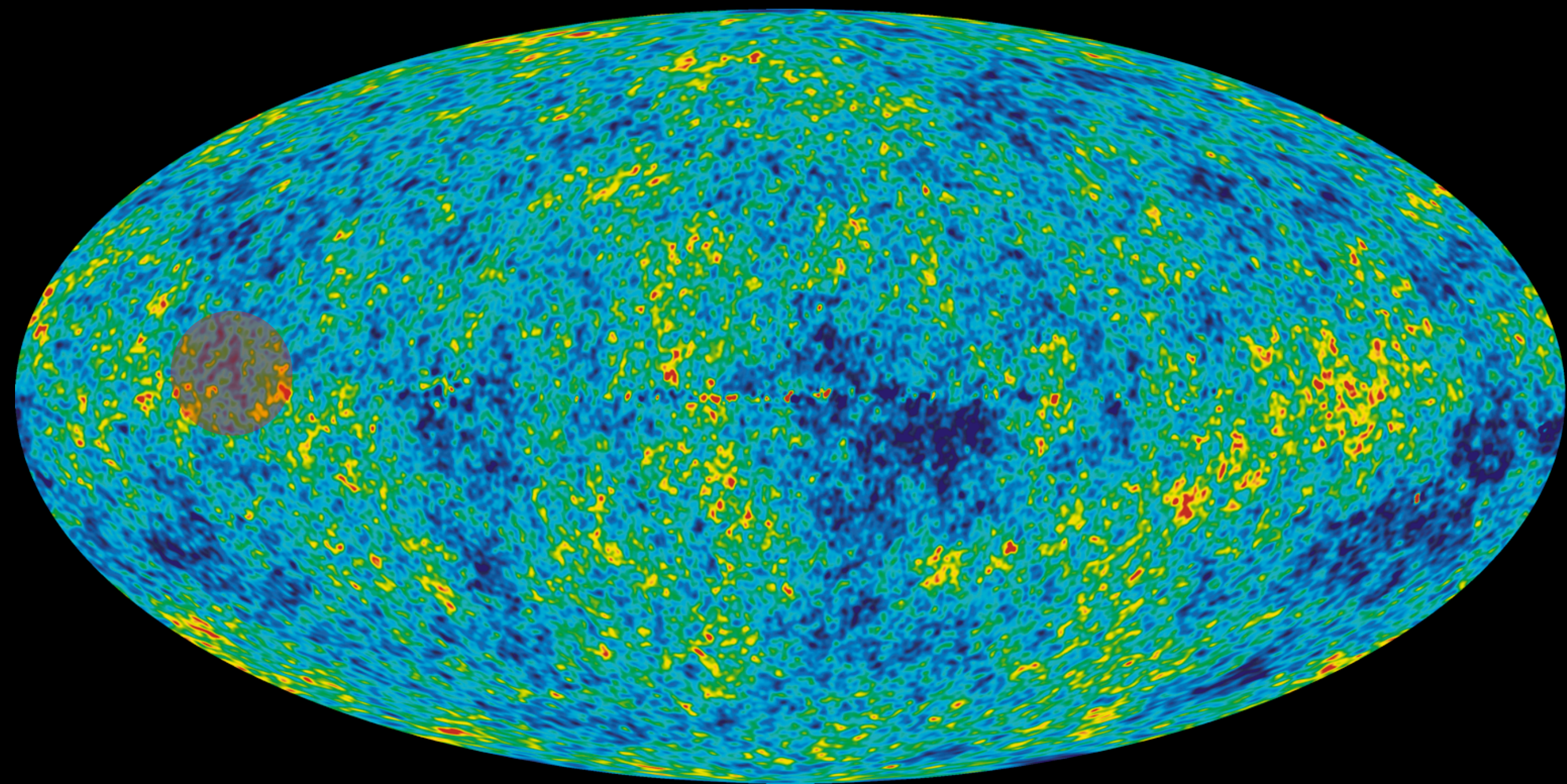
Gravity Waves via  
Weak Gravitational Lensing





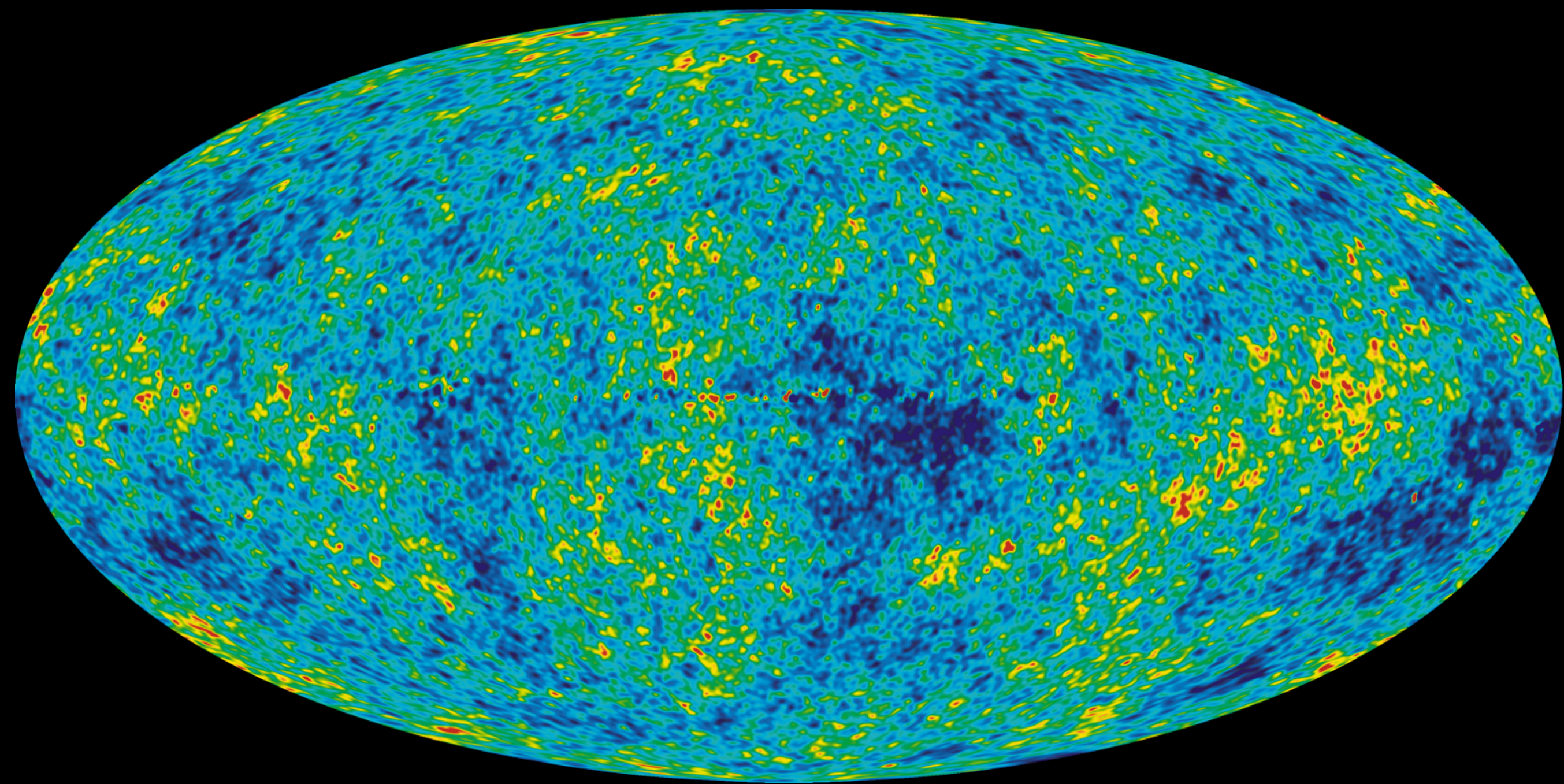
Credit: NASA/WMAP Science Team





Credit: NASA/WMAP Science Team





Credit: NASA/WMAP Science Team

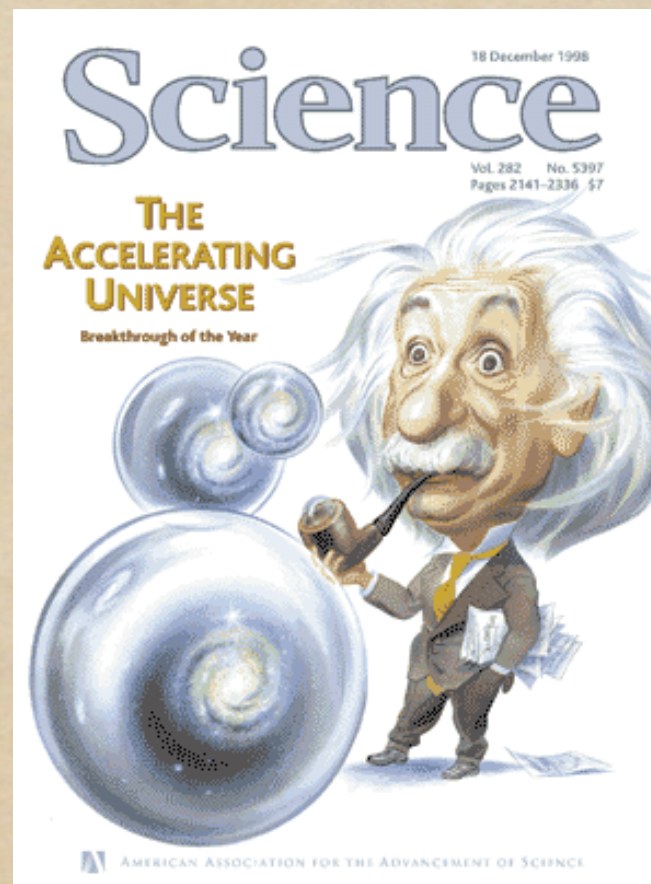


## OBSERVATIONAL EVIDENCE FROM SUPERNOVAE FOR AN ACCELERATING UNIVERSE AND A COSMOLOGICAL CONSTANT

ADAM G. RIESS,<sup>1</sup> ALEXEI V. FILIPPENKO,<sup>1</sup> PETER CHALLIS,<sup>2</sup> ALEJANDRO CLOCCHIATTI,<sup>3</sup> ALAN DIERCKS,<sup>4</sup>  
PETER M. GARNAVICH,<sup>2</sup> RON L. GILLILAND,<sup>5</sup> CRAIG J. HOGAN,<sup>4</sup> SAURABH JHA,<sup>2</sup> ROBERT P. KIRSHNER,<sup>2</sup>  
B. LEIBUNDGUT,<sup>6</sup> M. M. PHILLIPS,<sup>7</sup> DAVID REISS,<sup>4</sup> BRIAN P. SCHMIDT,<sup>8,9</sup> ROBERT A. SCHOMMER,<sup>7</sup>  
R. CHRIS SMITH,<sup>7,10</sup> J. SPYROMILIO,<sup>6</sup> CHRISTOPHER STUBBS,<sup>4</sup>  
NICHOLAS B. SUNTZEFF,<sup>7</sup> AND JOHN TONRY<sup>11</sup>

*Received 1998 March 13; revised 1998 May 6*

Illustration: John Kascht





# MEASUREMENTS OF $\Omega$ AND $\Lambda$ FROM 42 HIGH-REDSHIFT SUPERNOVAE

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(THE SUPERNOVA COSMOLOGY PROJECT)

*Received 1998 September 8; accepted 1998 December 17*



# TYPE Ia SUPERNOVA DISCOVERIES AT $z > 1$ FROM THE *HUBBLE SPACE TELESCOPE*: EVIDENCE FOR PAST DECELERATION AND CONSTRAINTS ON DARK ENERGY EVOLUTION<sup>1</sup>

ADAM G. RIESS,<sup>2</sup> LOUIS-GREGORY STROLGER,<sup>2</sup> JOHN TONRY,<sup>3</sup> STEFANO CASERTANO,<sup>2</sup> HENRY C. FERGUSON,<sup>2</sup> BAHRAM MOBASHER,<sup>2</sup>  
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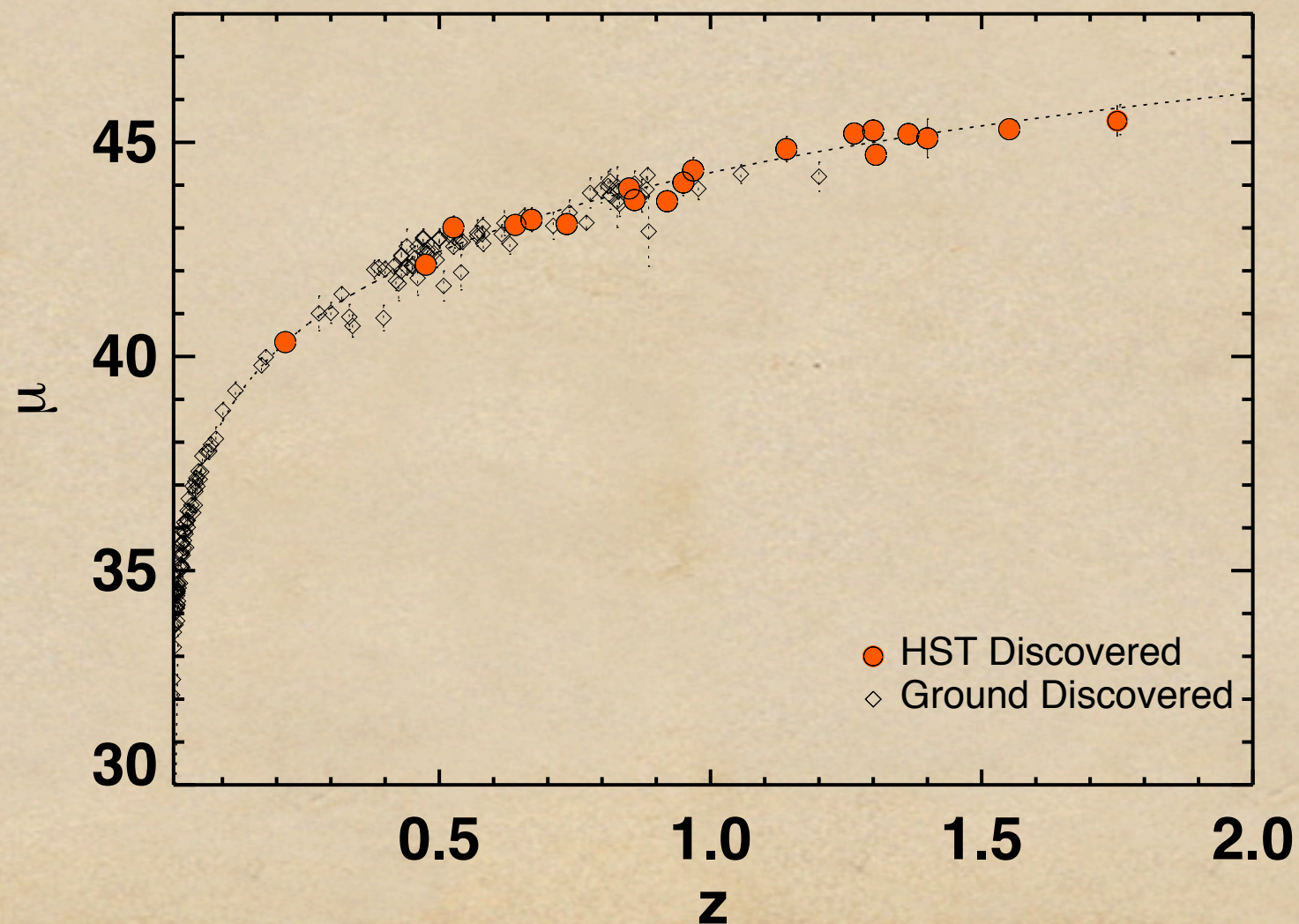
*Received 2004 January 20; accepted 2004 February 16*



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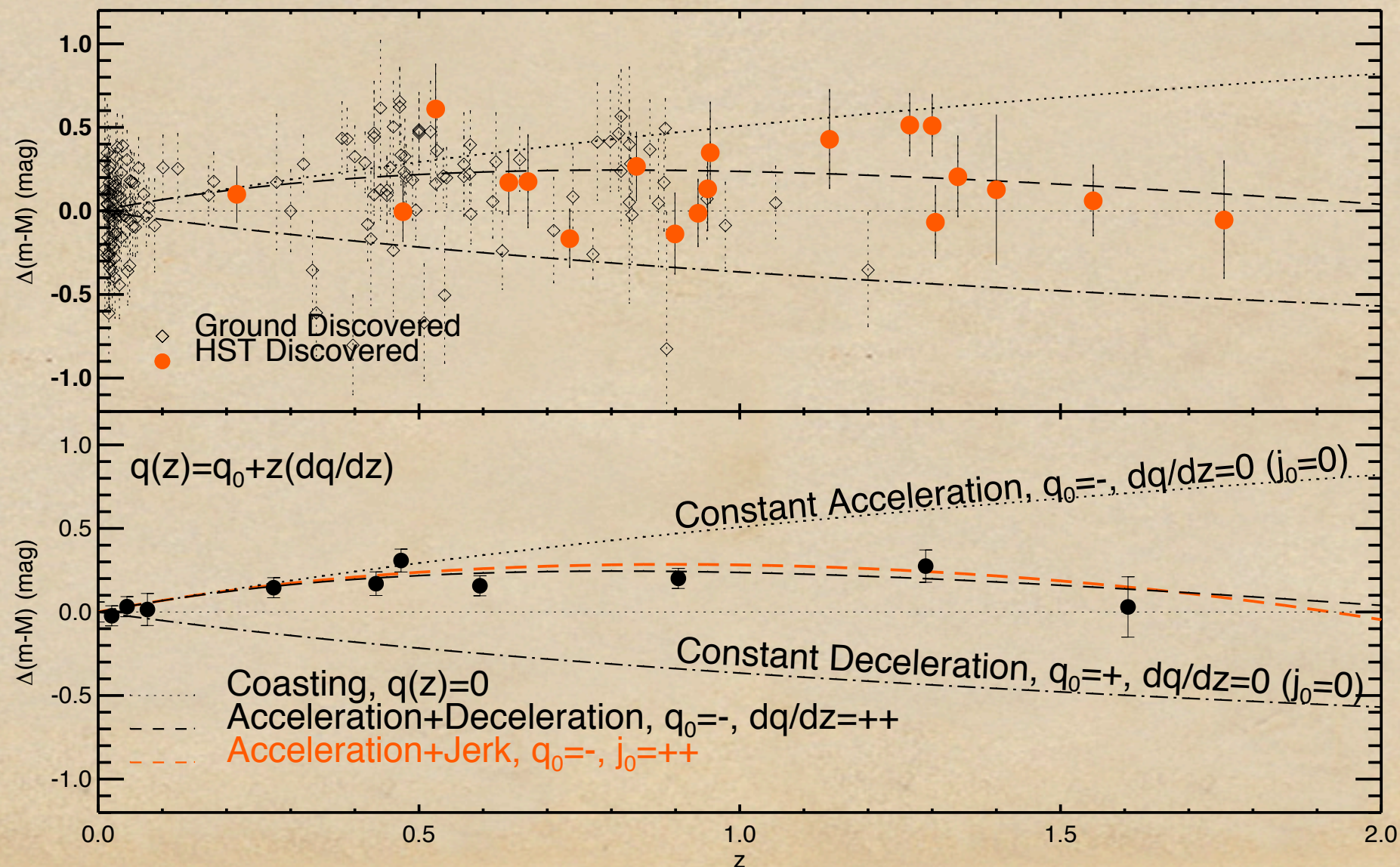




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# Cosmic Acceleration

Modified Gravity

Dark Energy

$$H^2 - \frac{H}{r_c} = \frac{8\pi G}{3} (\rho + \rho_V)$$

Modification of Friedmann  
equation (5D Gravity)

Vacuum Energy  
(Cosmological Constant)

Phenomenological  
modification to the GR  
Lagrangian

Scalar Fields  
Evolving Equation of State

New Physics/Surprises?



# Where Do We Stand? After...

A DECADE OF  
**DARK ENERGY**

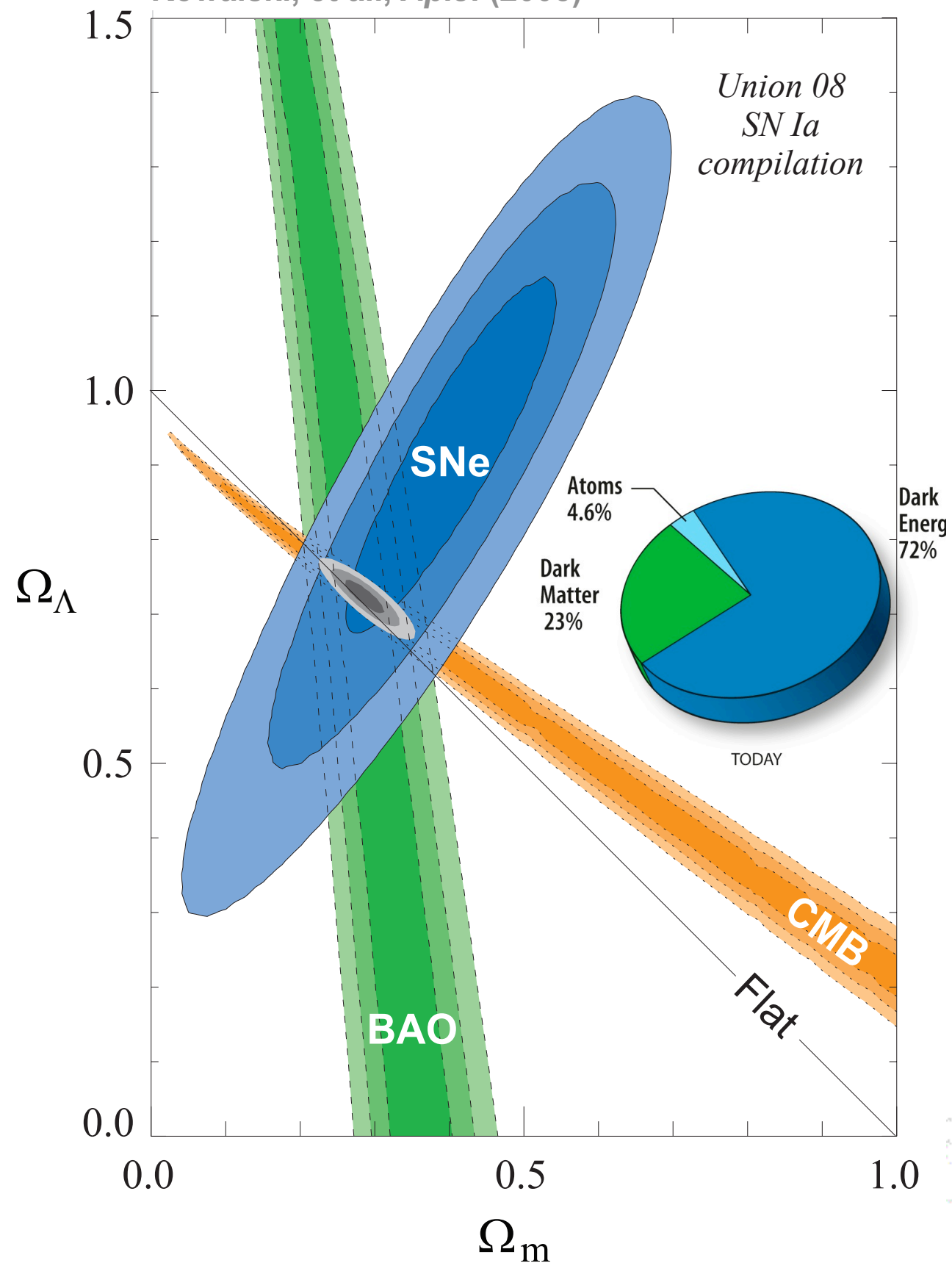
MAY 5-8, 2008

Space Telescope Science Institute, Baltimore, MD



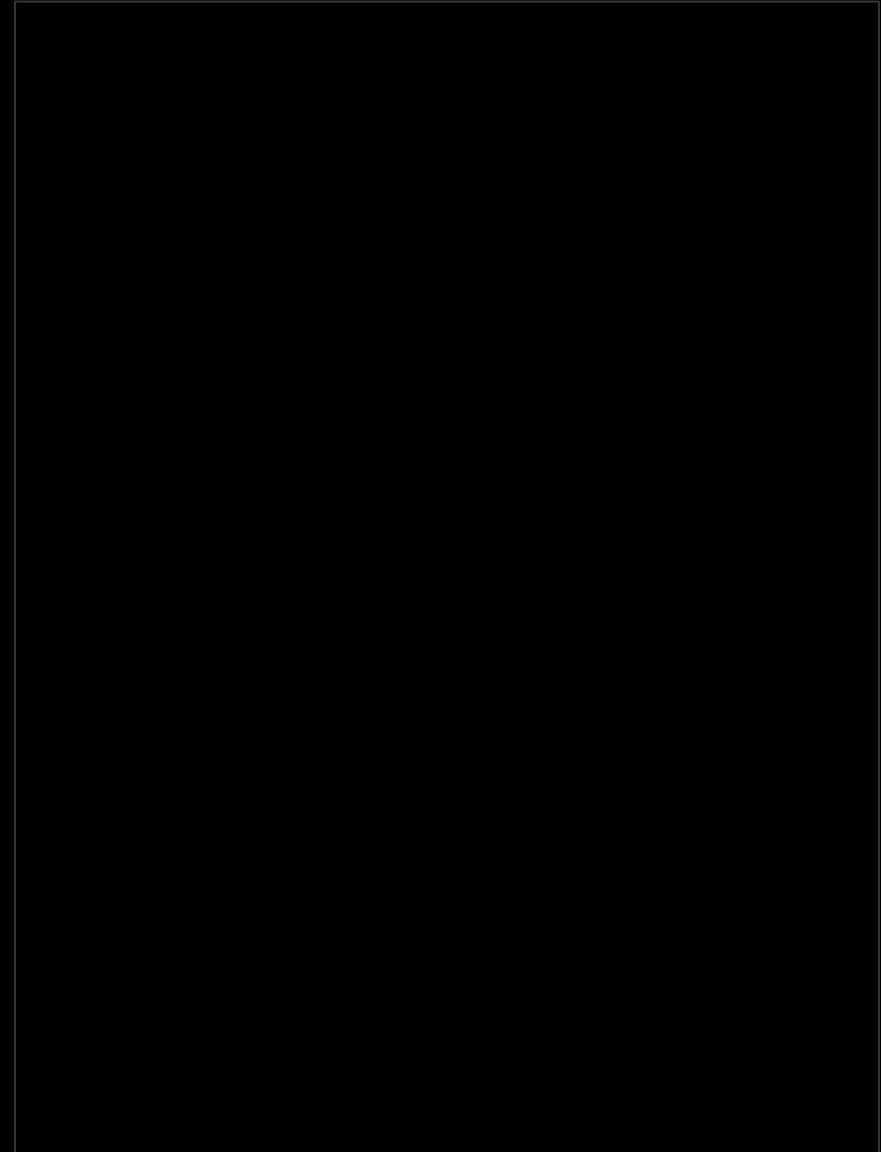
$$\Omega_{\Lambda} = 0.713^{+0.027}_{-0.029}(\text{stat})^{+0.036}_{-0.039}(\text{sys})$$

Supernova Cosmology Project  
Kowalski, et al., *Ap.J.* (2008)





# What is Dark Energy?





# What is Dark Energy?

“Dark Energy is made from an exclusive blend of vital L-amino acids, beneficial vitamins and bionutrients that allows faster and greater ion penetration of the cell walls, visibly enhancing the rate of growth”

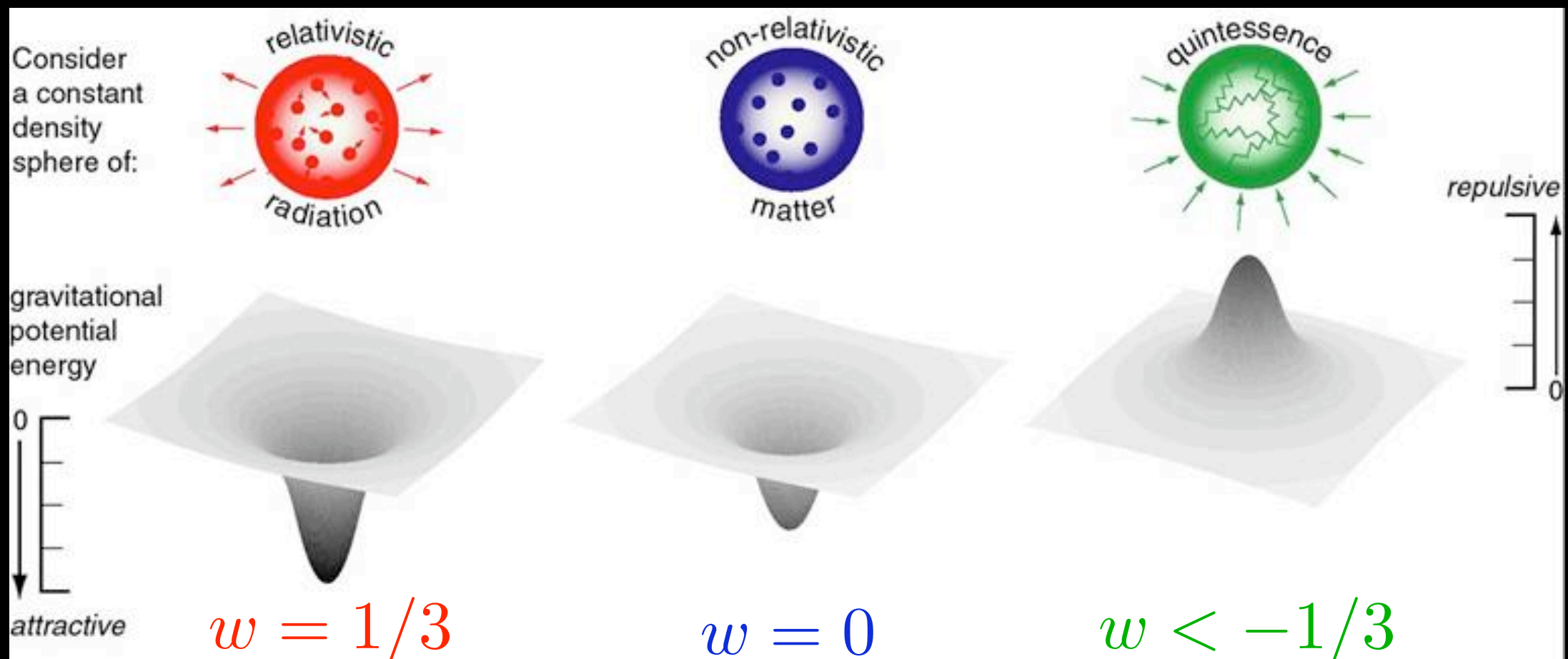


[GrowLightSource.com](http://GrowLightSource.com)



# Dark Energy Equation Of State

$$T_{\mu}^{\nu} = \text{diag}(\rho, -p, -p, -p) \quad p = w\rho$$



For Cosmological Constant...  $w = -1$



# “Seeing” The Dark Energy

...via its effect on the expansion of the Universe

$$H(z) = H_0 \left[ \Omega_m (1+z)^3 + \Omega_k (1+z)^2 + (1 - \Omega_k - \Omega_m) F(z) \right]^{1/2}$$



# “Seeing” The Dark Energy

...via its effect on the expansion of the Universe

$$H(z) = H_0 \left[ \Omega_m (1+z)^3 + \Omega_k (1+z)^2 + (1 - \Omega_k - \Omega_m) F(z) \right]^{1/2}$$

$$F(z) = \exp \left( 3 \int_0^z dz' \frac{1 + w(z')}{1 + z'} \right)$$





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Approaches...

🌀 Standard Candles: Luminosity Distance of SNe

🌀 Standard Rulers:

➤ Angular Diameter Distance via BAO

➤ Distance to the Last Scattering Surface

🌀 Weak Lensing Tomography



# DE EOS Revisited: Different Approaches...

(A) Parameterize  $w(z)$

[Adopted by the DETF]

$$w(a) = w_0 + (1 - a)w_a$$

*Chevallier & Polarski (2001)*  
*(Linder 2003)*



# DE EOS Revisited: Different Approaches...

(A) Parameterize  $w(z)$

[Adopted by the DETF]

$$w(z) = w_0 + w_a z / (1 + z)$$

*Chevallier & Polarski (2001)*  
*(Linder 2003)*



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[Adopted by the DETF]

$$w(z) = w_0 + w_a z / (1 + z)$$

*Chevallier & Polarski (2001)*  
*(Linder 2003)*

(B) Non-Parametric  $w(z)$

- ✓ Unbiased Estimate of DE Density (Wang & Lovelace 2001)
- ✓ Principal Component Approach (Huterer & Starkman 2003)
- ✓ Uncorrelated Estimates (Huterer & Cooray 2005)

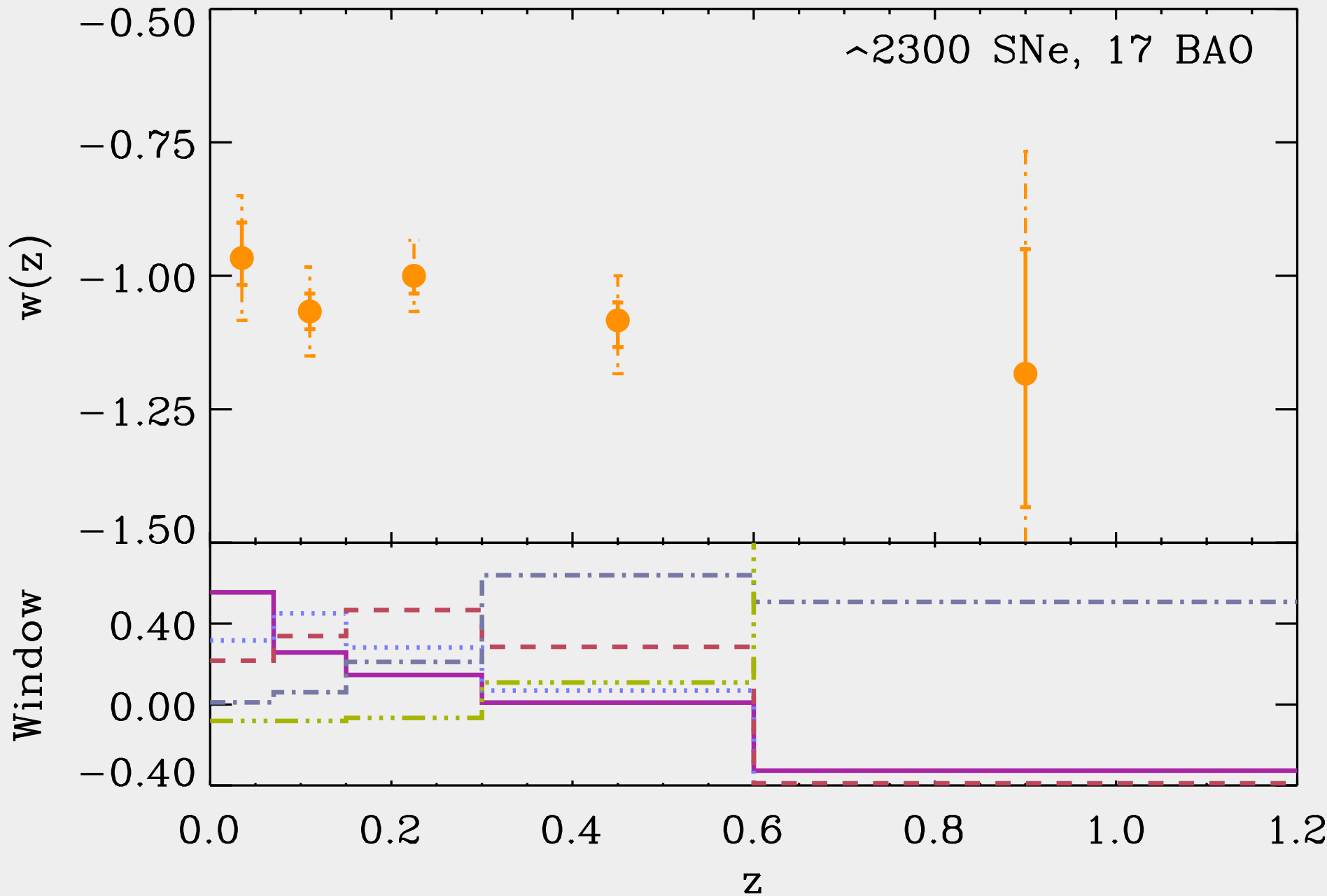
✓ ...

For a review: Please see Sahni and Starobinsky (2006) [arXiv:astro-ph/0610026]



# Binned Estimates: Future

$$F(z_n > z > z_{n-1}) = (1+z)^{3(1+w_n)} \prod_{i=0}^{n-1} (1+z_i)^{3(w_i-w_{i+1})}$$

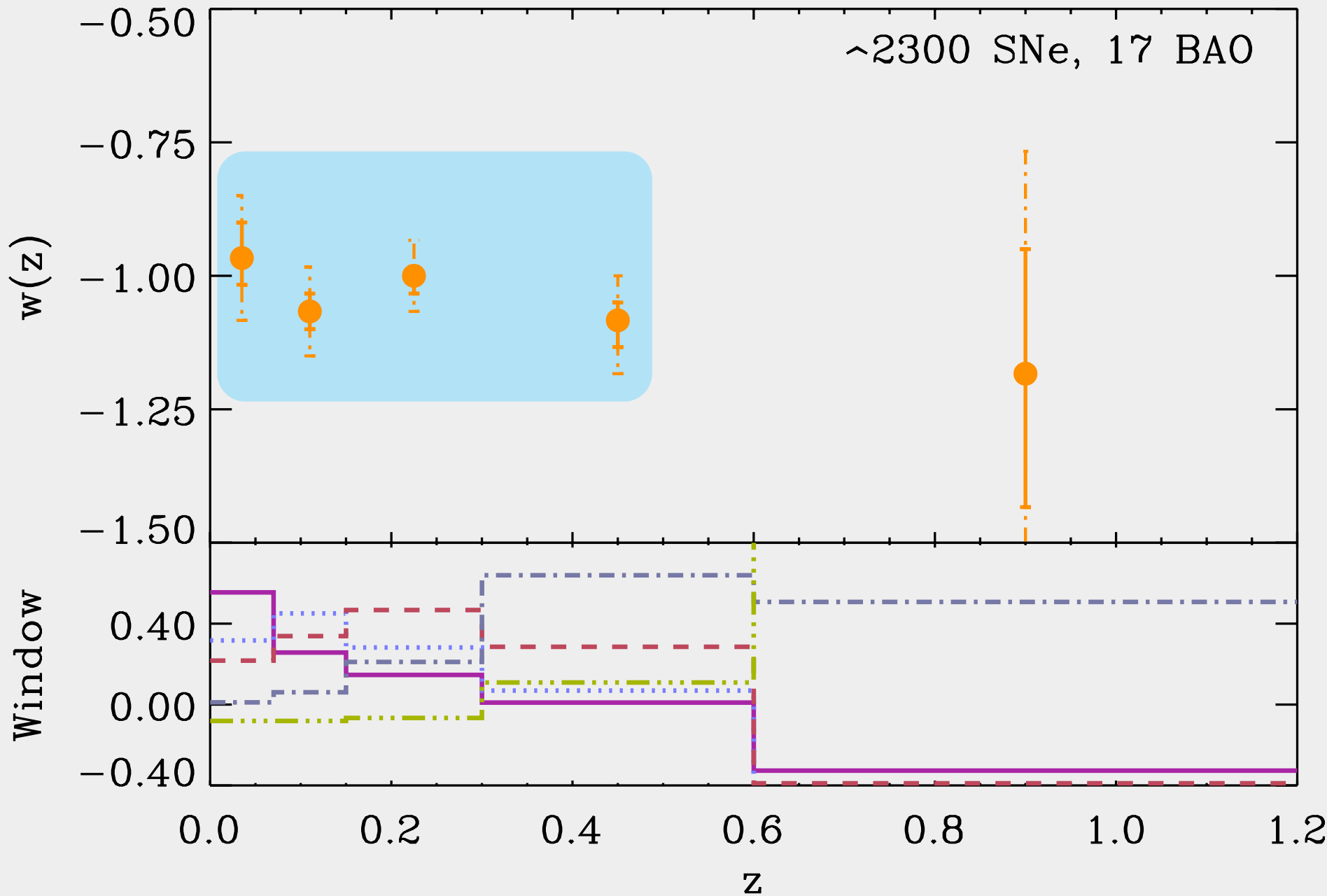


$w_1$	0-.07
$w_2$	.07-.15
$w_3$	0.15-.3
$w_4$	0.3-0.6
$w_5$	0.6-1.2
$w_6$	1.2-2.0



# Binned Estimates: Future

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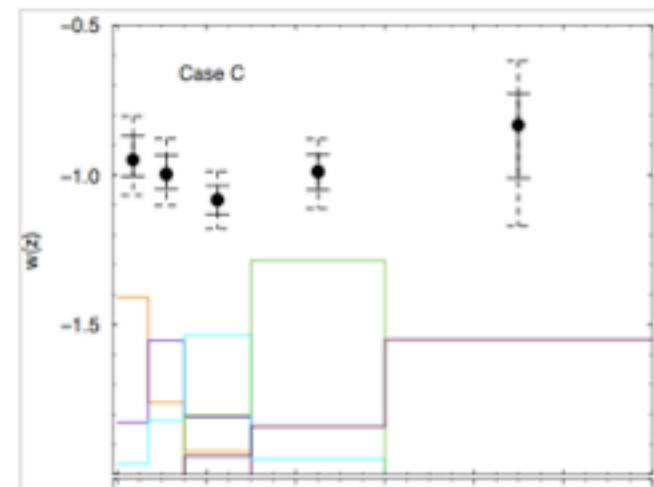
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*wzBinned* is a numerical code to extract uncorrelated binned estimates of the dark energy equation of state,  $w(z)$ , using Type Ia supernovae distance-redshift data and other cosmological probes and priors. It is written in C programming language and based on Markov chain Monte Carlo method. For further details please refer to [Sarkar et al., Phys. Rev. Lett. 100 241302 \(2008\)](#), and [Sullivan et al., JCAP 09 004 \(2007\)](#).



**COSMOMC**

► **CMBFAST**

IDL Astro



# Agenda

## Dark Energy

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- . To Bin or Not to Bin
- . SNe Ia ++
- . Lensing of SNe
- . Other Worries

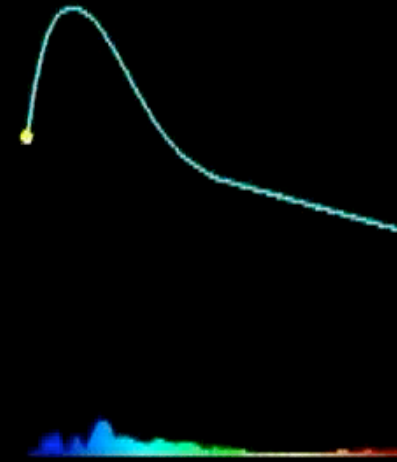
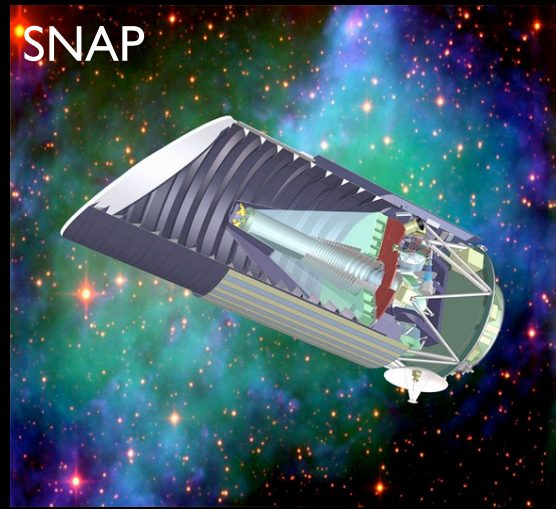
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Weak Gravitational Lensing



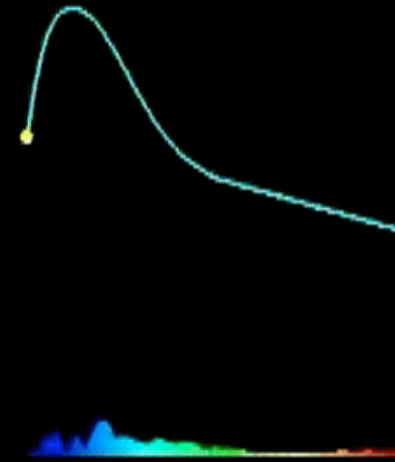
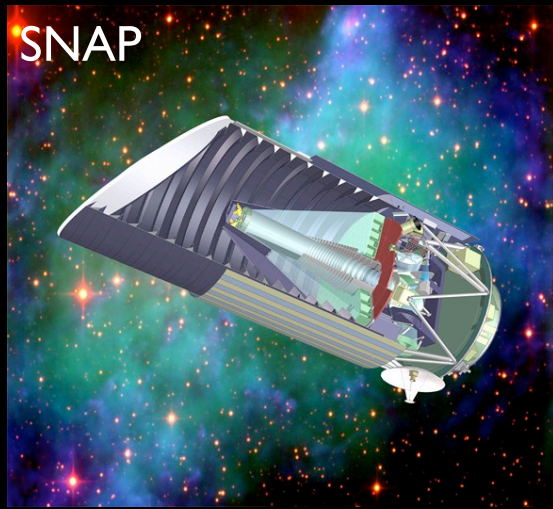
# Cosmology with SNe Ia: Revisited



Credit: This clip was prepared by the [Supernova Cosmology Project](#) (P. Nugent: spectral sequence; A. Conley: image sequence) with the help of Lawrence Berkeley National Laboratory's Computer Visualization Laboratory (N. Johnston: animation) at the National Energy Research Scientific Computing Center.



# Cosmology with SNe Ia: Revisited

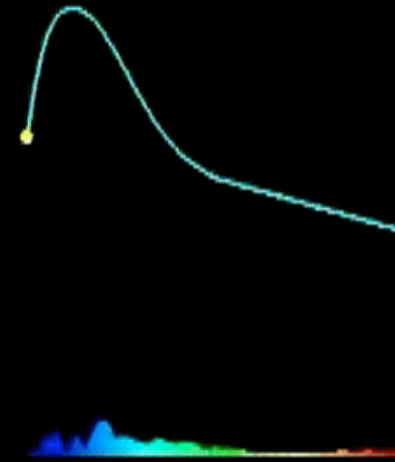
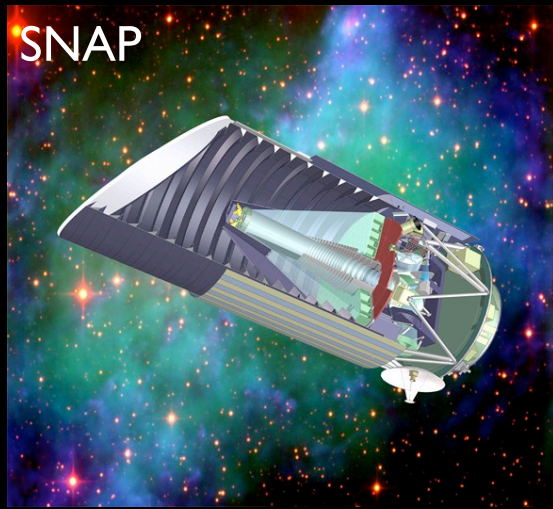


## Advantages

- ✓ Direct measure of accl.
- ✓ Small dispersion
- ✓ Single objects (easier!)
- ✓ Can be observed over wide  $z$
- ✓ Not cosmic variance limited
- ✓ Straightforward tests of sys.



# Cosmology with SNe Ia: Revisited



## Advantages

- ✓ Direct measure of accl.
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- ✓ Not cosmic variance limited
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## Challenges

- 📌 Dust extinction
- 📌 Photometric calibration (Vega)
- 📌 Malmquist bias
- 📌 K-corrections
- 📌 Evolution, chemical comp.
- 📌 Population bias + Grav. Lensing



# Challenges: Systematic Uncertainties

source of uncertainty	common (mag)	sample-dep.(mag)	treatment
Extinction	0.013	-	Multi-band photometry including near-IR
Calibration	0.021	0.021	Calibration of standard stars (optical thru near-IR) to <1%
Malmquist	-	0.020	High S/N lightcurves & spectra; requirement of pre-rise data
Lightcurve	0.028	-	SN spectra with broad $\lambda$ , temporal coverage
Evolution	0.015	-	High-resolution spectroscopy

Kowalski et al. (2008), Carnegie Supernova Project: W. Freedman

Lensing	
2-Population	



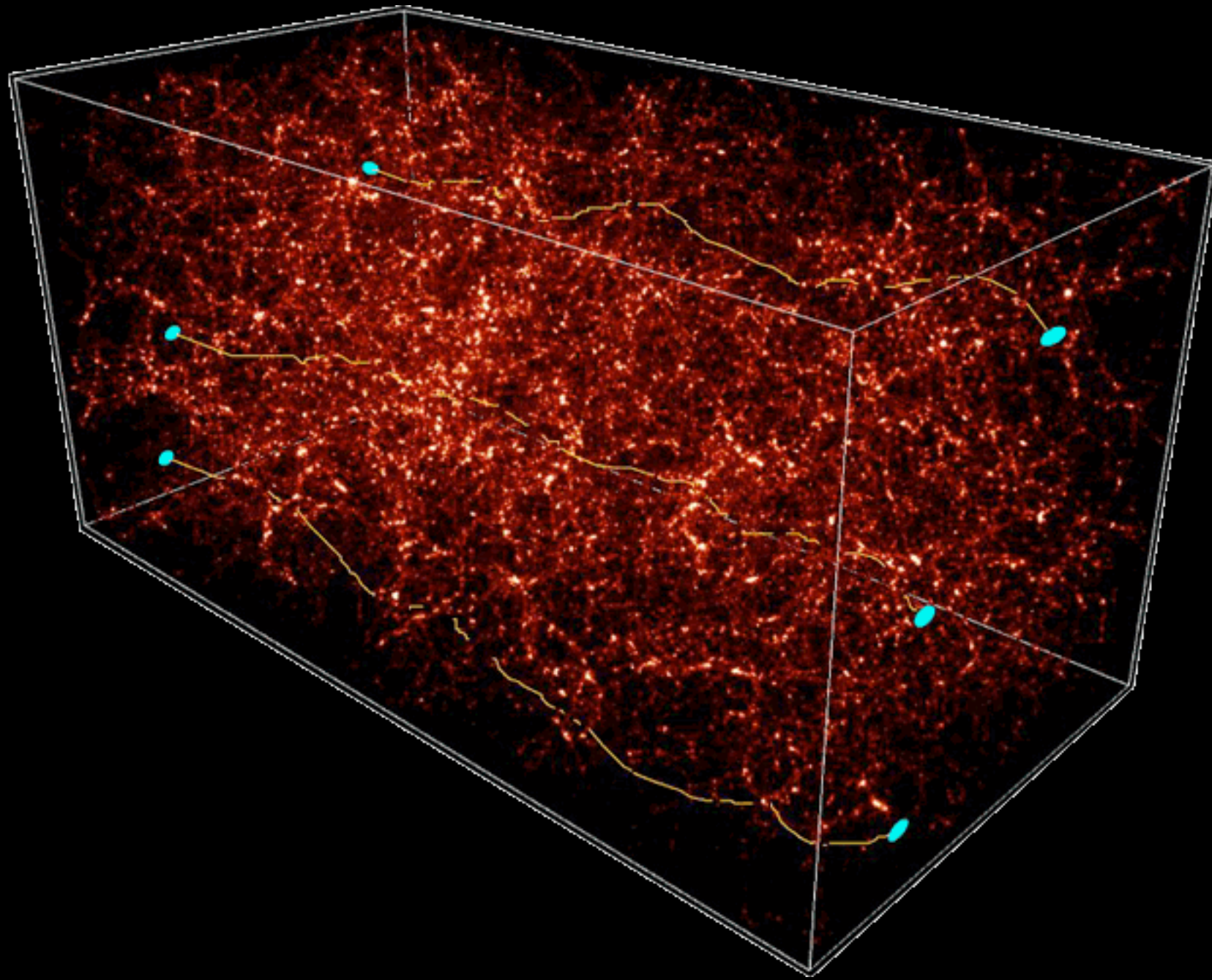
# Influence of Gravitational Lensing?

Lensing Galaxy



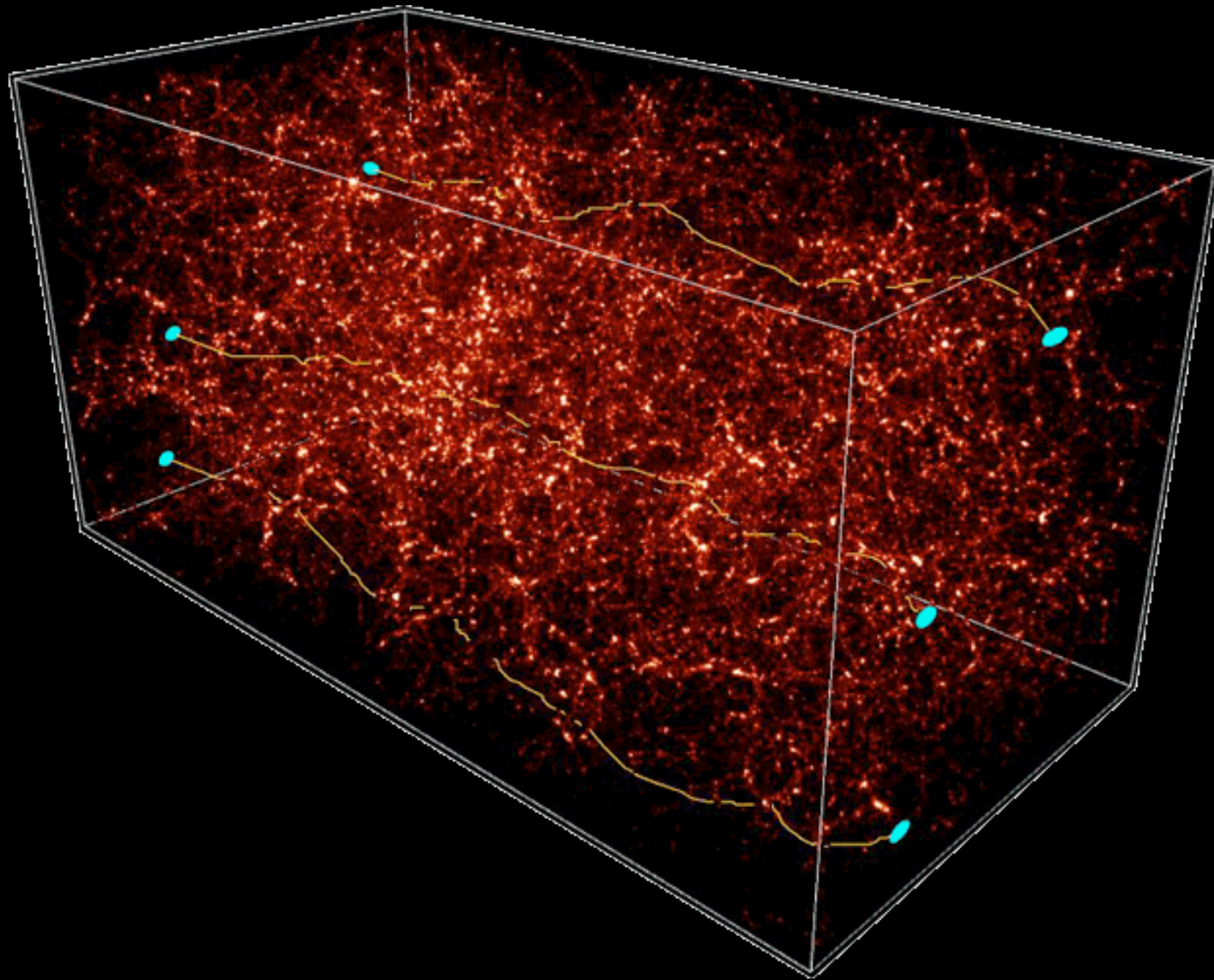


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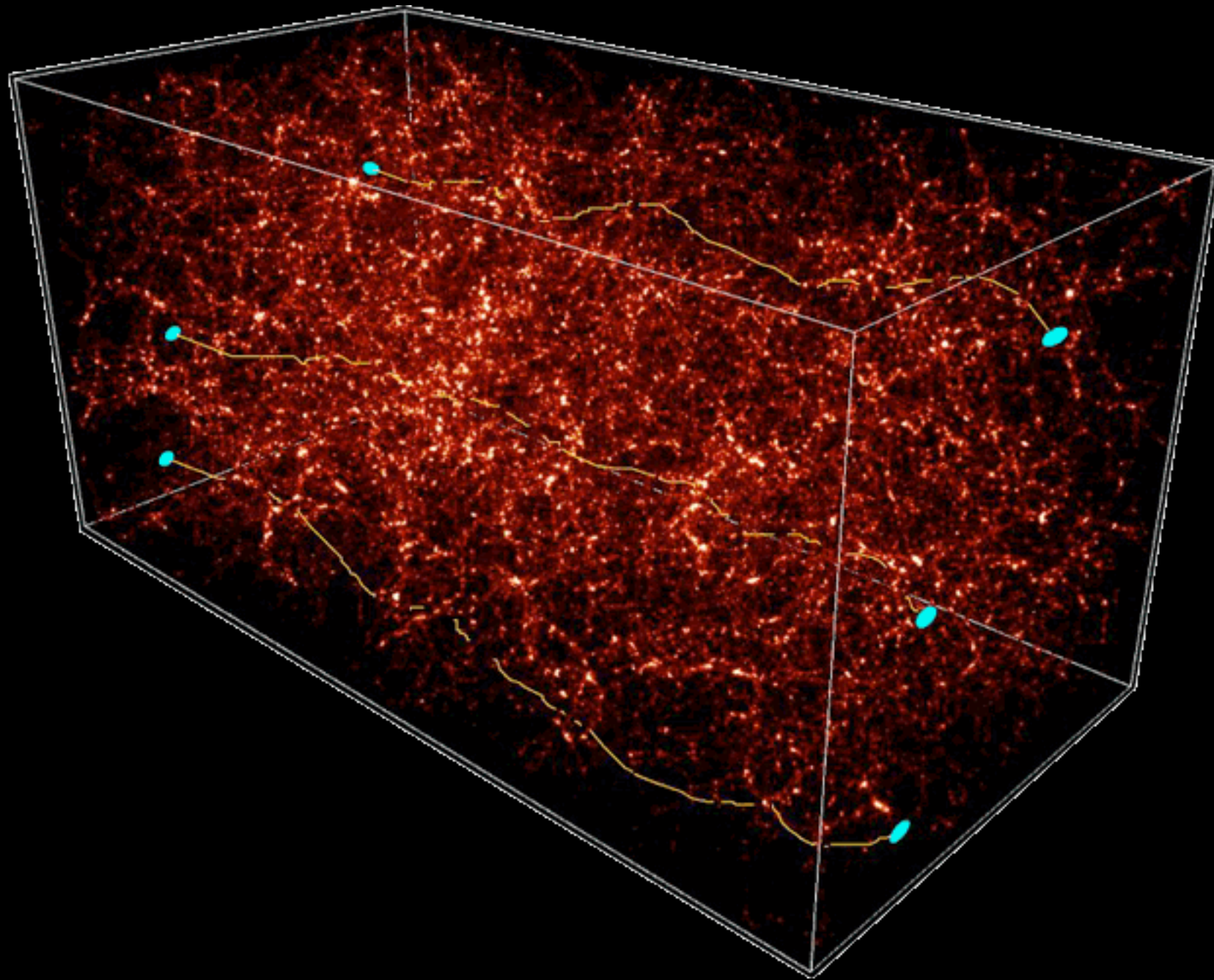
# Influence of Gravitational Lensing?



$$\mathcal{F}^{\text{obs,lensed}}(z, \hat{\mathbf{n}}) = \mu(z, \hat{\mathbf{n}}) \mathcal{F}^{\text{obs,true}}(z)$$



# Influence of Gravitational Lensing?

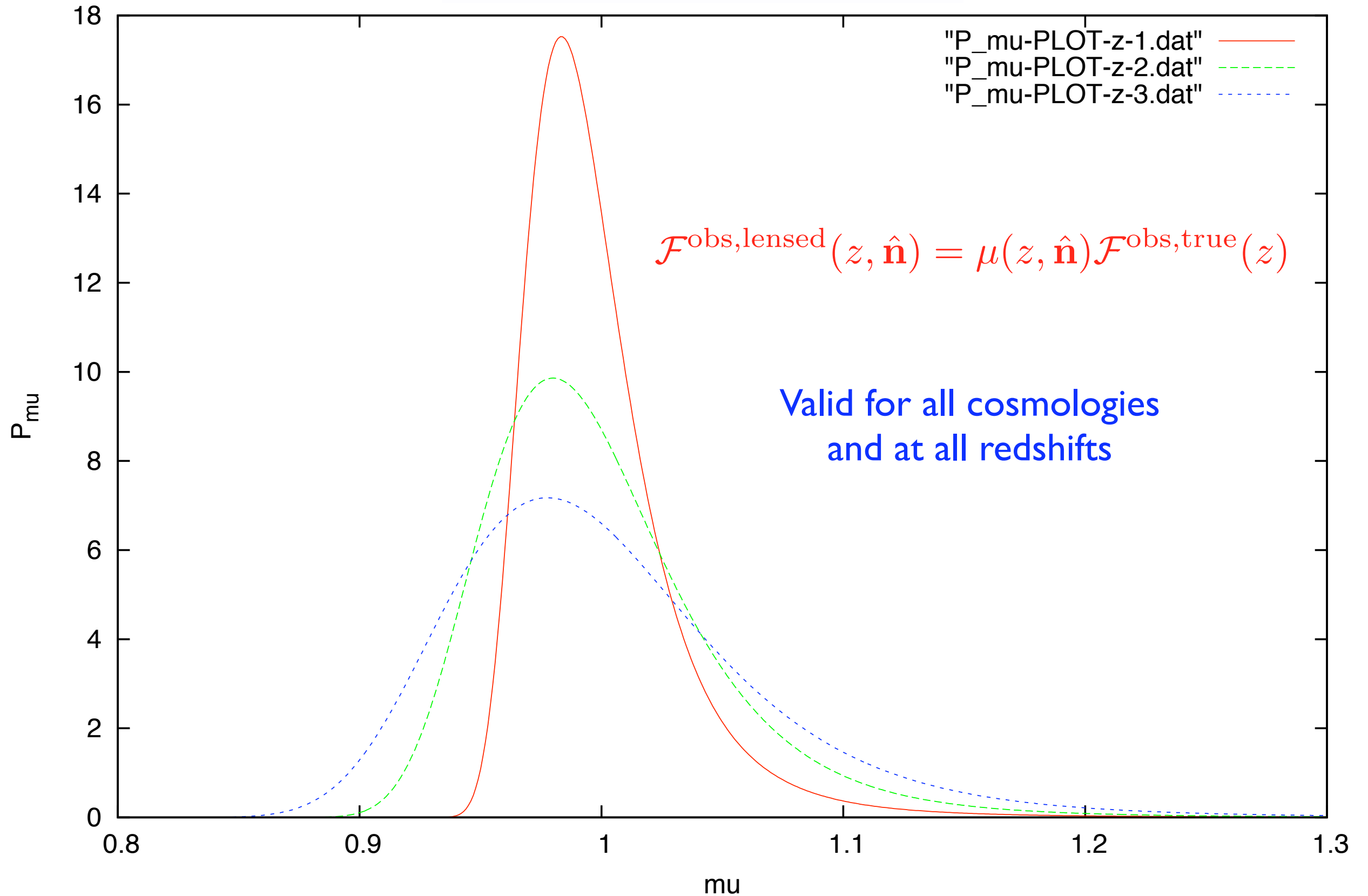


$$\mathcal{F}^{\text{obs,lensed}}(z, \hat{\mathbf{n}}) = \mu(z, \hat{\mathbf{n}}) \mathcal{F}^{\text{obs,true}}(z)$$

Weak lensing can modify the SNa flux & bias estimates of  $w$

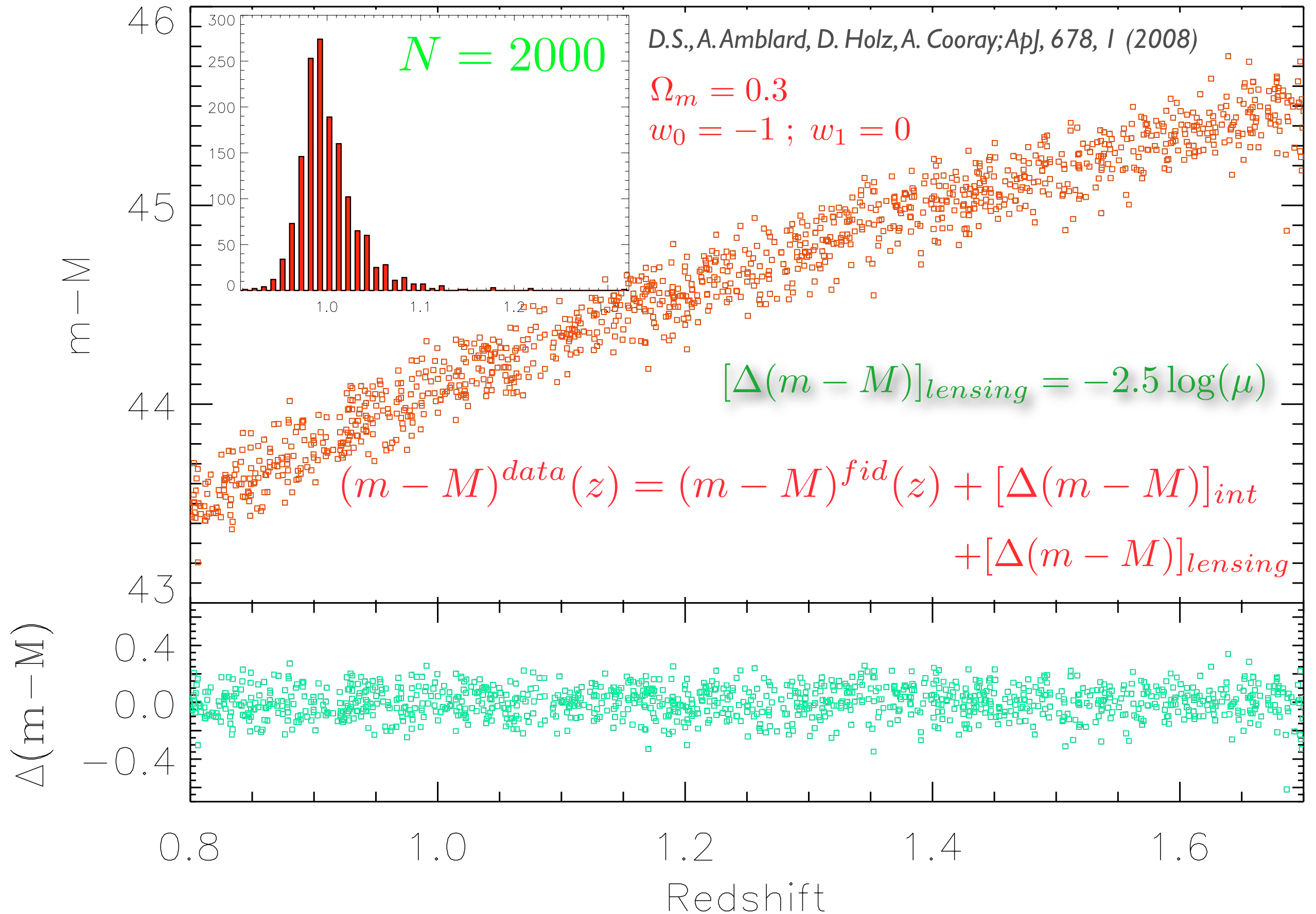


# Amplification Probability Distribution



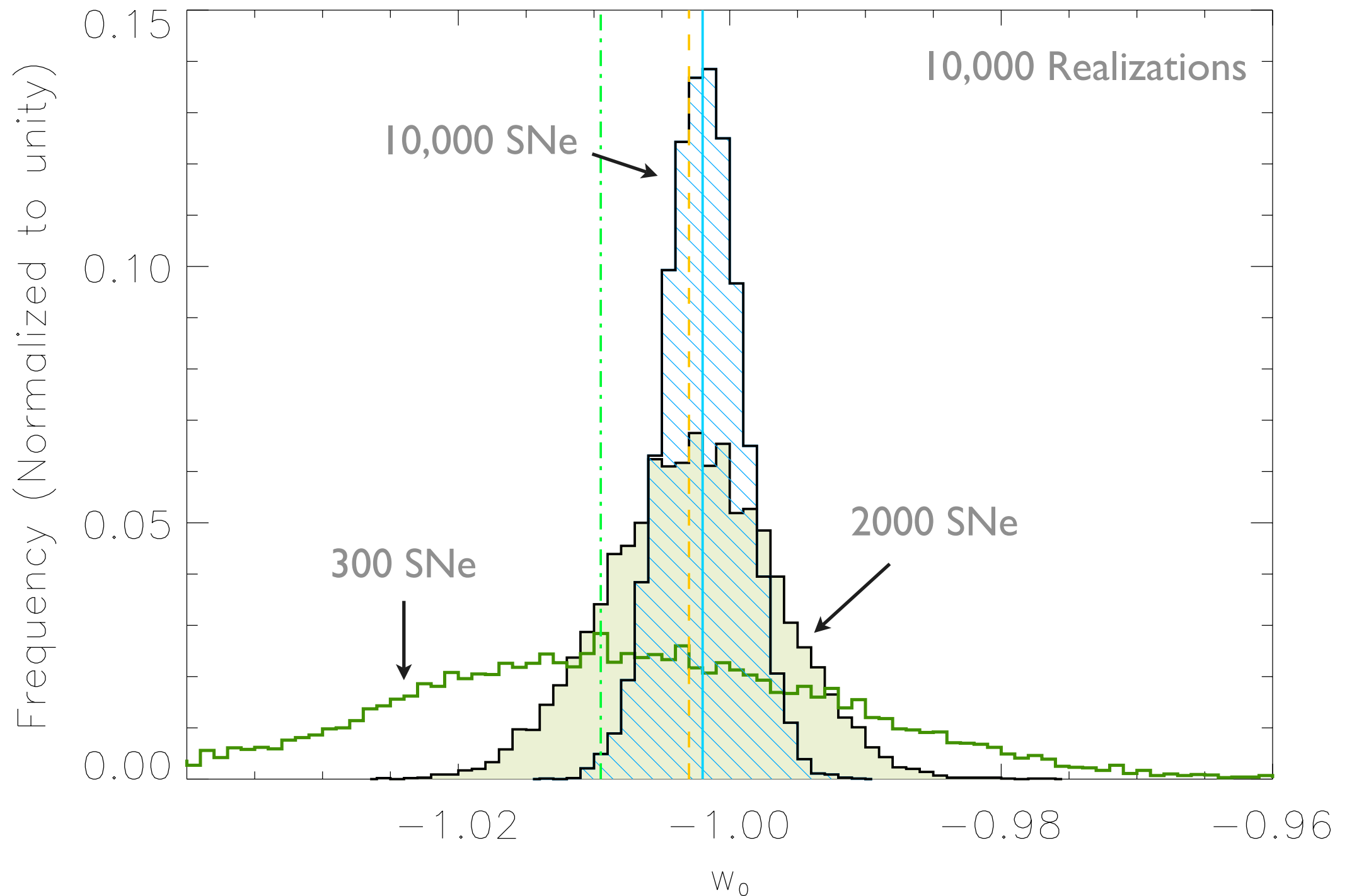


# Our Analysis with Mock Catalogs





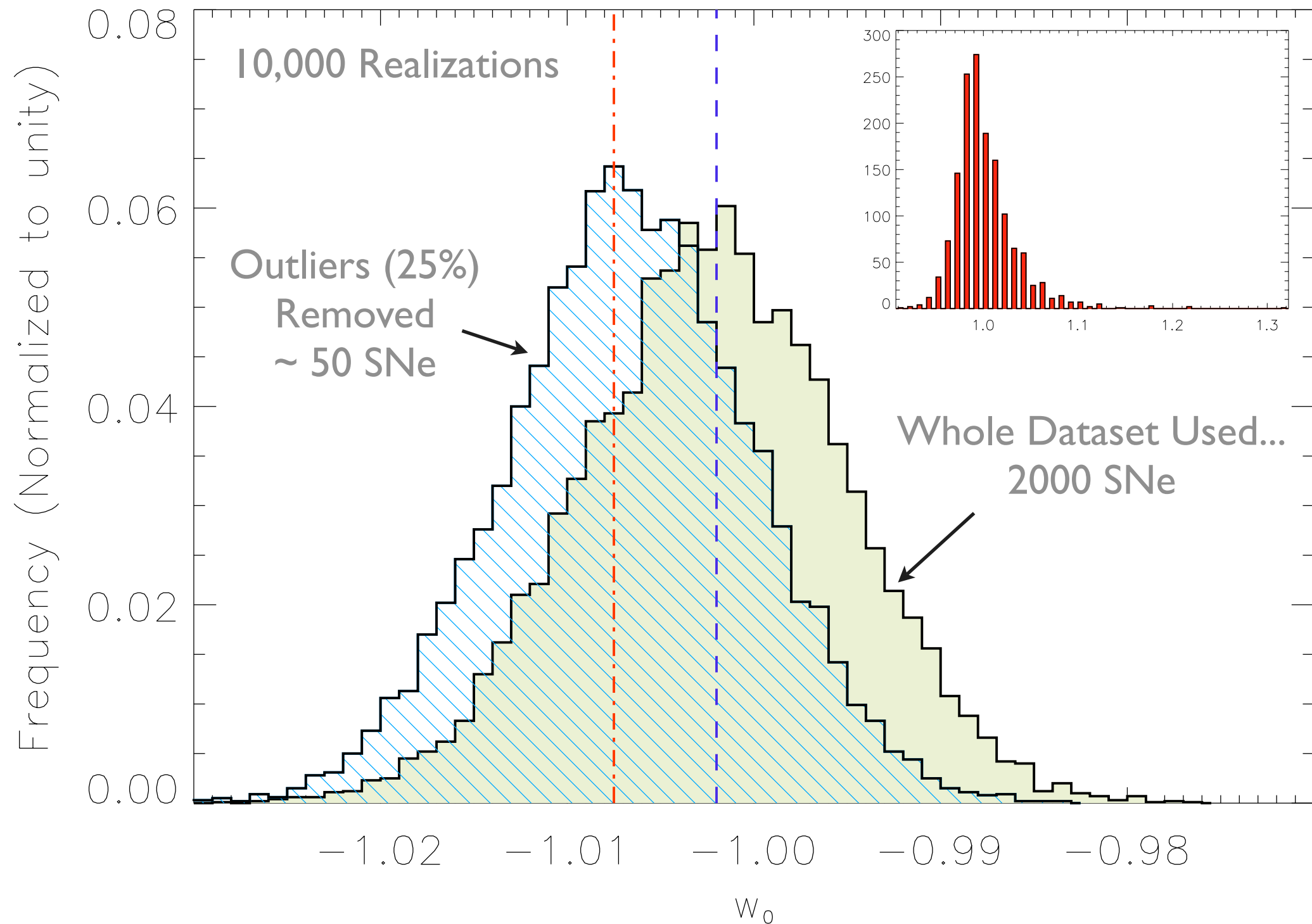
# Effect of Weak Lensing on Estimates of “w”



*D.S., A. Amblard, D. Holz, A. Cooray; ApJ, 678, 1 (2008)*



# Effect of Removing the Outliers



*D.S., A. Amblard, D. Holz, A. Cooray; ApJ, 678, 1 (2008)*



# Challenges: Systematic Uncertainties

source of uncertainty	common (mag)	sample-dep.(mag)	treatment
Extinction	0.013	-	Multi-band photometry including near-IR
Calibration	0.021	0.021	Calibration of standard stars (optical thru near-IR) to <1%
Malmquist	-	0.020	High S/N lightcurves & spectra; requirement of pre-rise data
Lightcurve	0.028	-	SN spectra with broad $\lambda$ , temporal coverage
Evolution	0.015	-	High-resolution spectroscopy

Kowalski et al. (2008), Carnegie Supernova Project: W. Freedman

Lensing	Need a large # of SNe per redshift bin to keep bias < 1%
2-Population	



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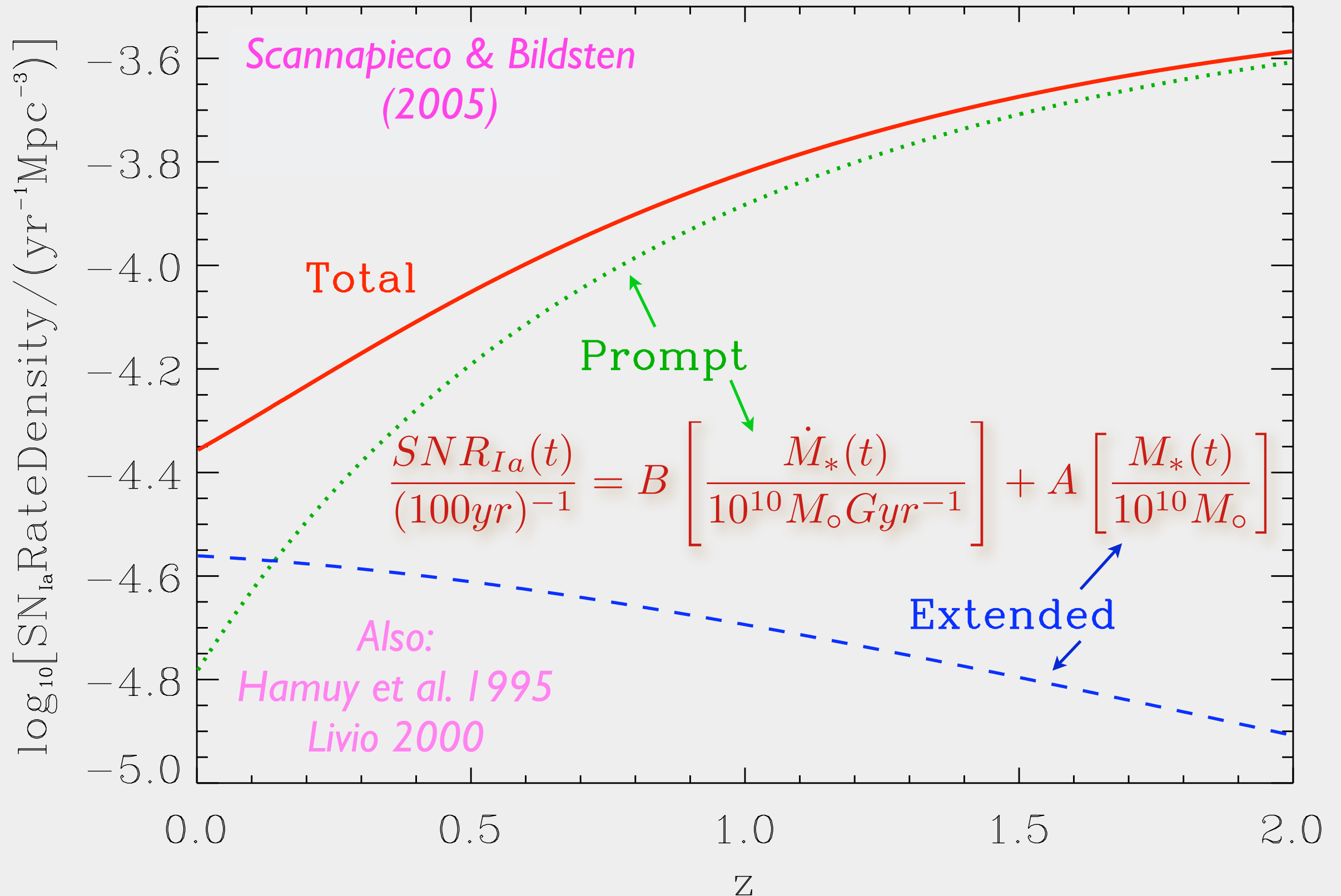
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# Evolution based on Two SN Populations





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Kowalski et al. (2008), Carnegie Supernova Project: W. Freedman

Lensing	Need a large # of SNe per redshift bin to keep bias < 1%
2-Population	More Important! <i>D.S., A. Amblard, A. Cooray, and D. Holz; ApJL, 684, L13 (2008)</i>



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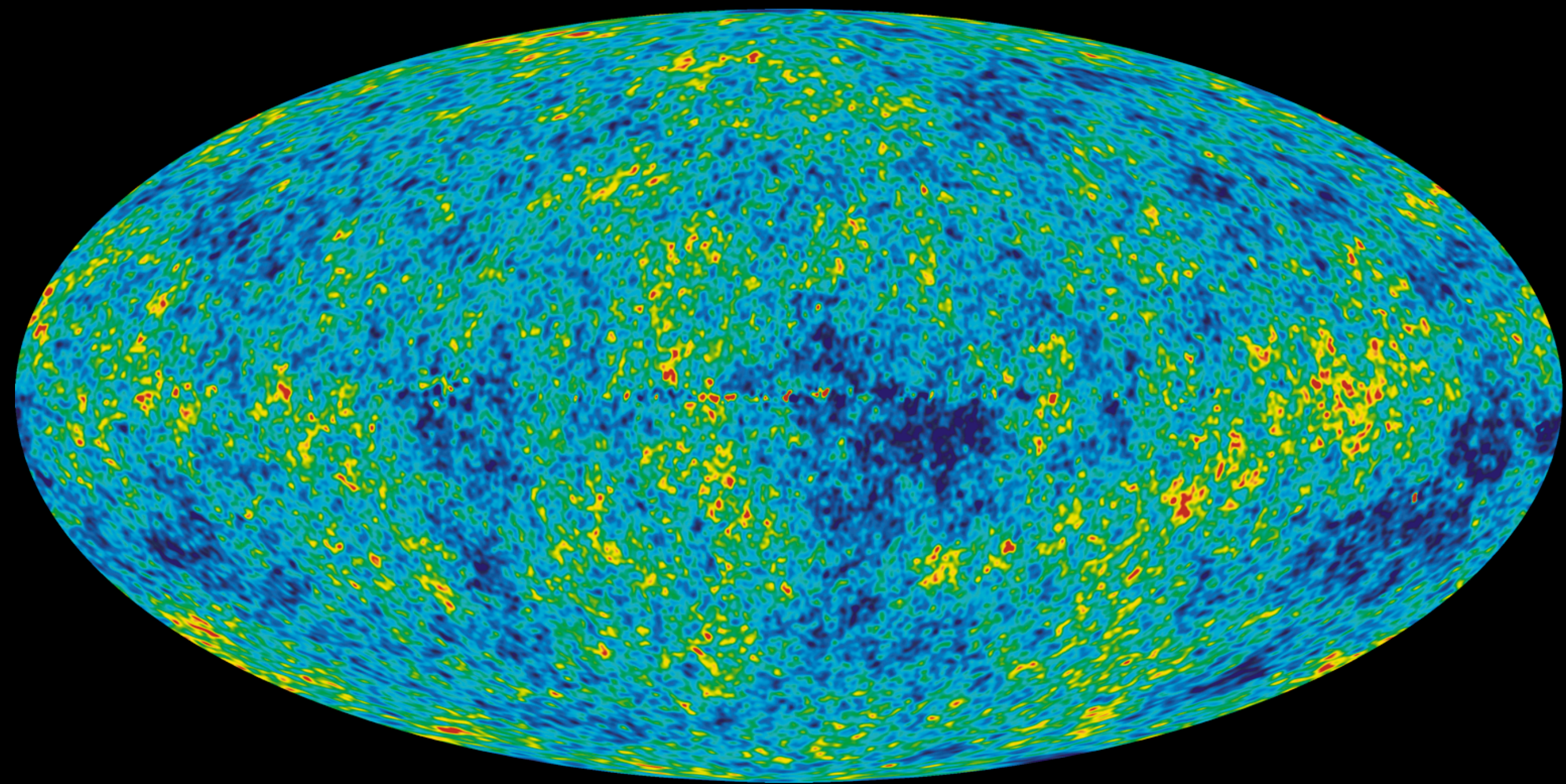
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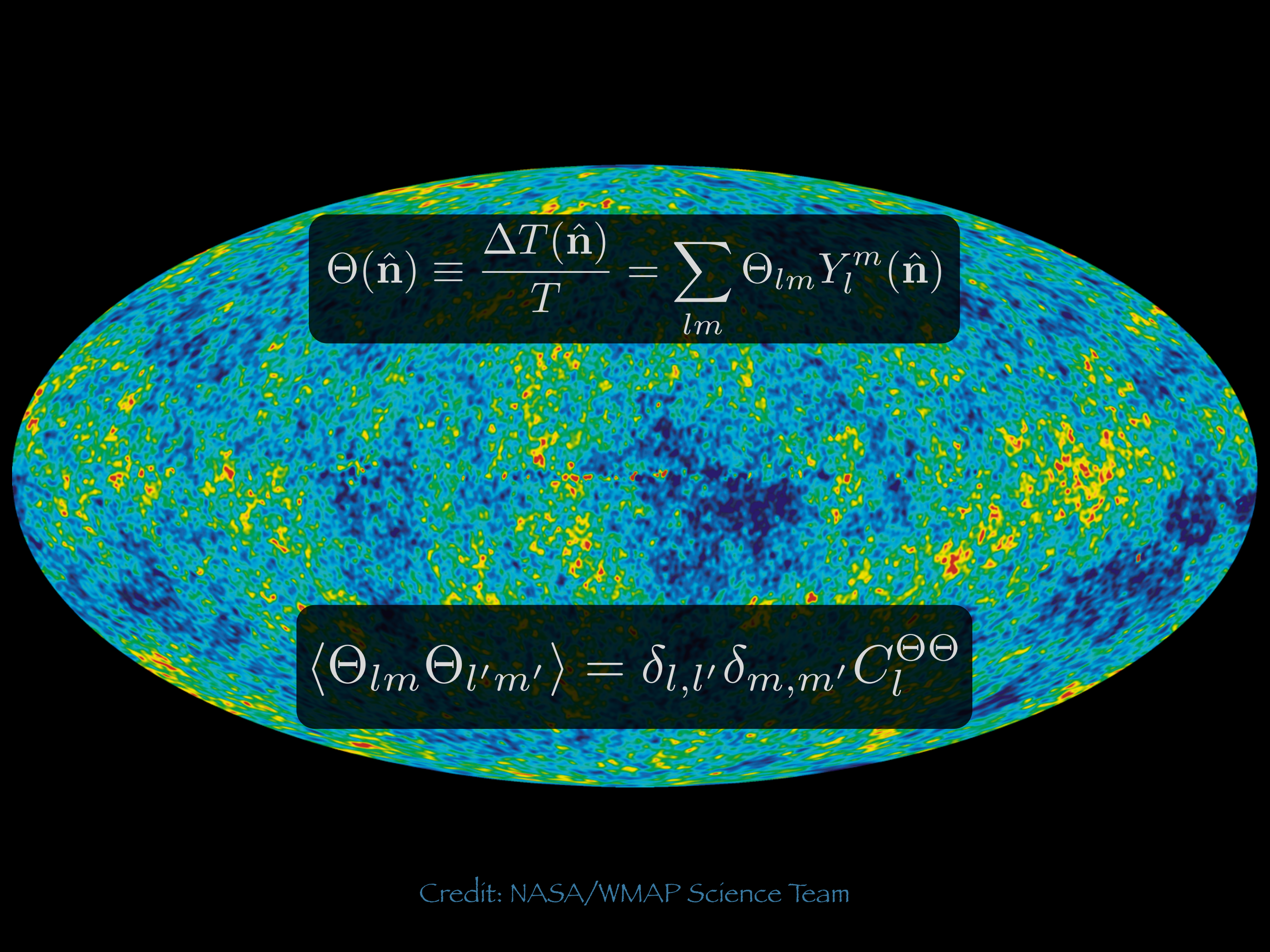
Gravity Waves via  
Weak Gravitational Lensing





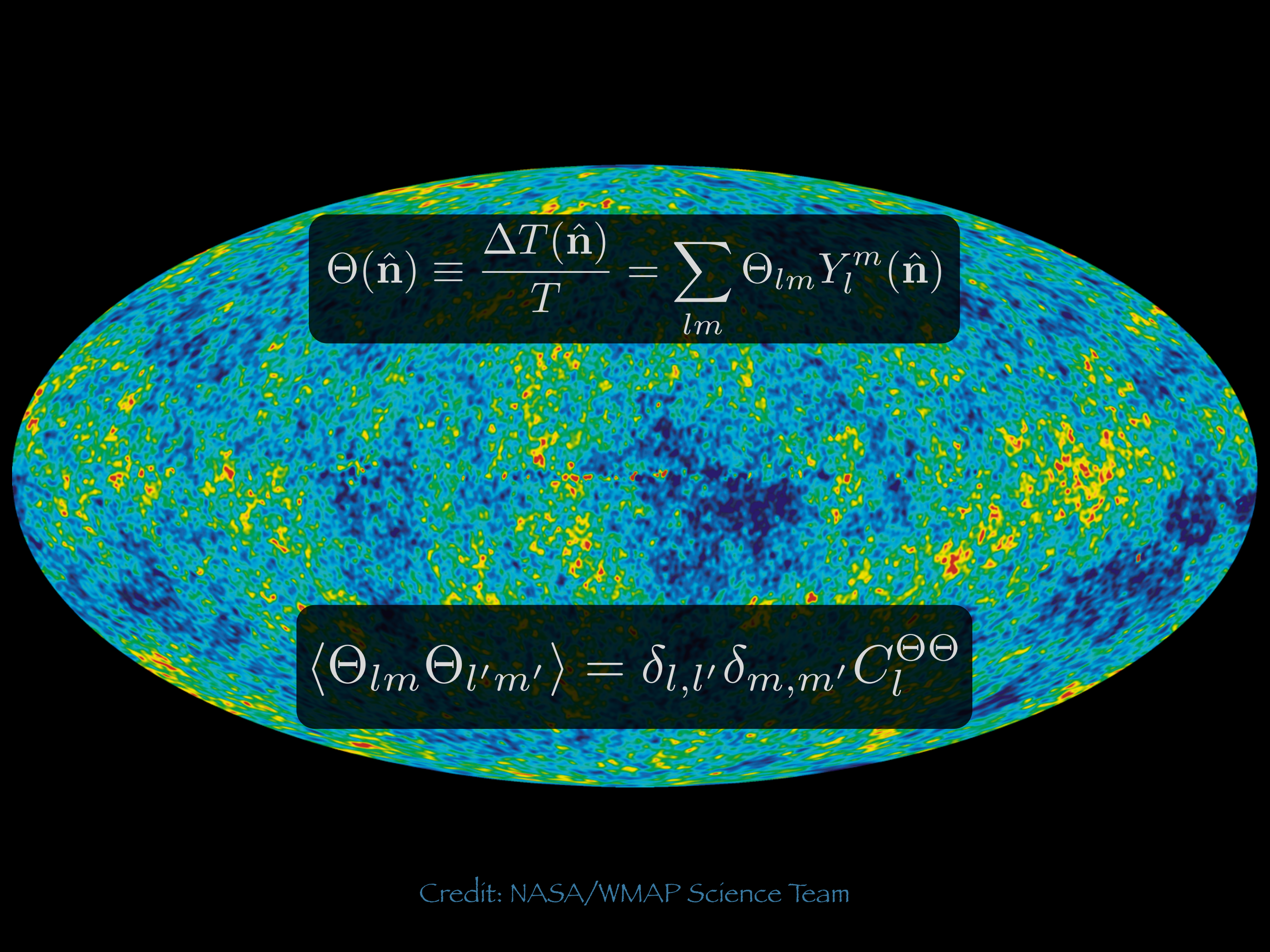
Credit: NASA/WMAP Science Team




$$\Theta(\hat{\mathbf{n}}) \equiv \frac{\Delta T(\hat{\mathbf{n}})}{T} = \sum_{lm} \Theta_{lm} Y_l^m(\hat{\mathbf{n}})$$

Credit: NASA/WMAP Science Team

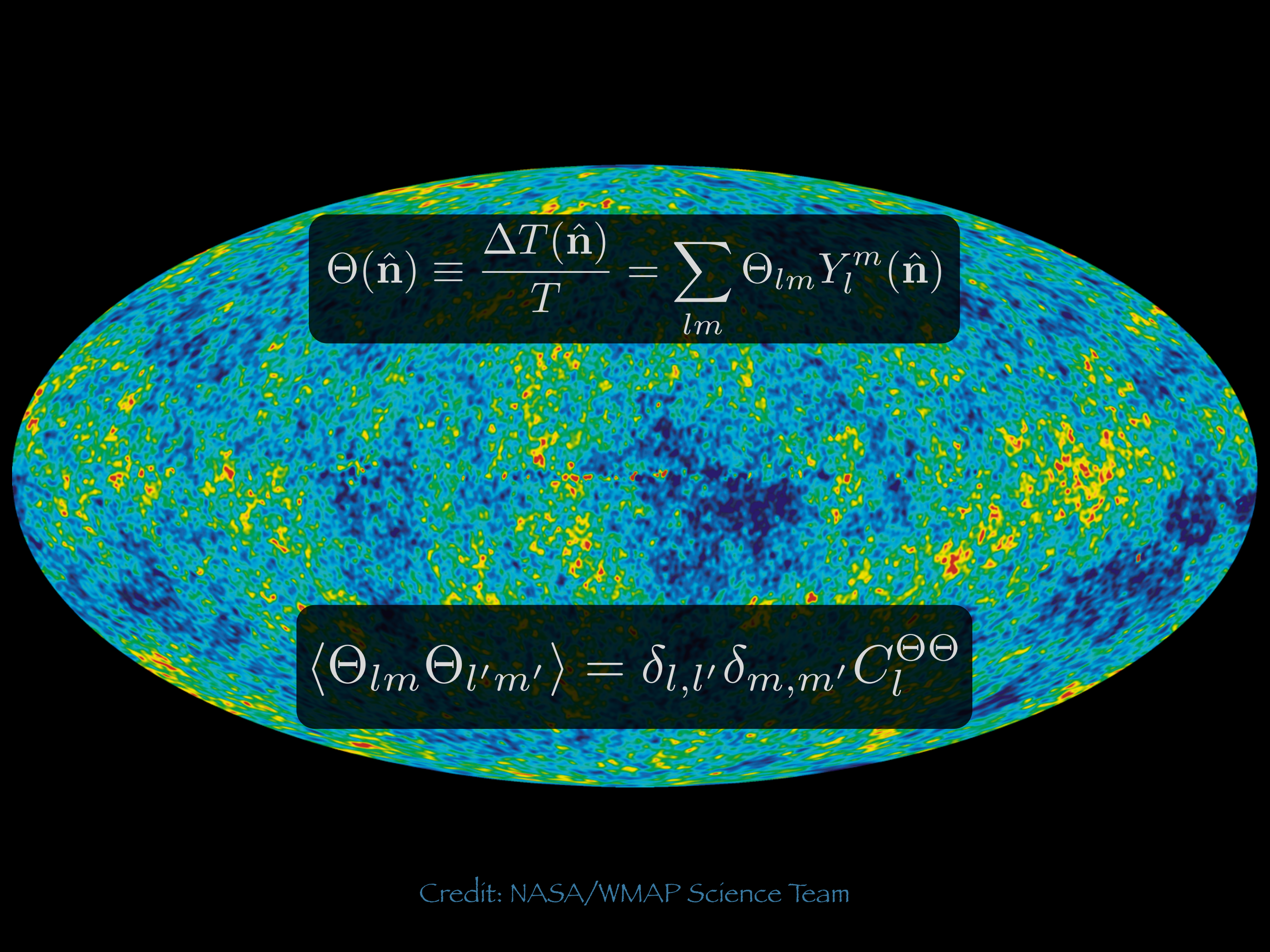



$$\Theta(\hat{\mathbf{n}}) \equiv \frac{\Delta T(\hat{\mathbf{n}})}{T} = \sum_{lm} \Theta_{lm} Y_l^m(\hat{\mathbf{n}})$$

$$\langle \Theta_{lm} \Theta_{l'm'} \rangle = \delta_{l,l'} \delta_{m,m'} C_l^{\Theta\Theta}$$

Credit: NASA/WMAP Science Team





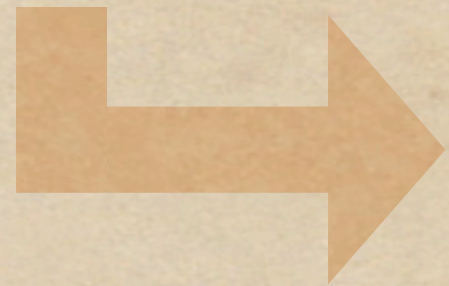
$$\Theta(\hat{\mathbf{n}}) \equiv \frac{\Delta T(\hat{\mathbf{n}})}{T} = \sum_{lm} \Theta_{lm} Y_l^m(\hat{\mathbf{n}})$$

$$\langle \Theta_{l_1 m_1} \Theta_{l_2 m_2} \Theta_{l_3 m_3} \rangle = \begin{pmatrix} l_1 & l_2 & l_3 \\ m_1 & m_2 & m_3 \end{pmatrix} B_{l_1 l_2 l_3}^{\Theta}$$

$$\langle \Theta_{lm} \Theta_{l'm'} \rangle = \delta_{l,l'} \delta_{m,m'} C_l^{\Theta\Theta}$$



# Primordial non-Gaussianity

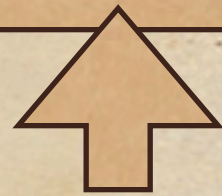


## Primary CMB Bispectrum

$$\frac{\Delta T(\mathbf{x})}{T} \sim \Phi(\mathbf{x})$$



$$\Phi(\mathbf{x}) = \Phi_L(\mathbf{x}) + f_{NL} [\Phi_L^2(\mathbf{x}) - \langle \Phi_L^2(\mathbf{x}) \rangle]$$

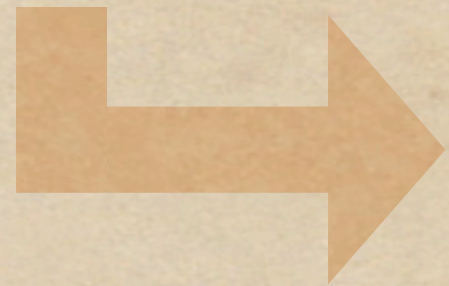


Non-Linear Coupling Parameter

Measurement of non-Gaussian CMB anisotropies can potentially constrain non-linearity, “slow-rollness”, and “adiabaticity” in inflation.



# Primordial non-Gaussianity



## Primary CMB Bispectrum

Non-Gaussianity from the simplest inflation model is very small:

$$f_{NL} \sim 0.01 - 1$$

Much higher level of primordial non-Gaussianity is predicted by:

- Models with Multiple Scalar Fields
- Non-Adiabatic Fluctuations
- Features in the Inflation Potential
- Non-Canonical Kinetic Terms
- ...



# Evidence of Primordial Non-Gaussianity ( $f_{\text{NL}}$ ) in the Wilkinson Microwave Anisotropy Probe 3-Year Data at $2.8\sigma$

Amit P. S. Yadav<sup>1</sup> and Benjamin D. Wandelt<sup>1,2</sup>

<sup>1</sup>*Department of Astronomy, University of Illinois at Urbana-Champaign, 1002 W. Green Street, Urbana, Illinois 61801, USA*

<sup>2</sup>*Department of Physics, University of Illinois at Urbana-Champaign, 1110 W. Green Street, Urbana, Illinois 61801, USA*

(Received 7 December 2007; revised manuscript received 6 March 2008; published 7 May 2008)

We present evidence for primordial non-Gaussianity of the local type ( $f_{\text{NL}}$ ) in the temperature anisotropy of the cosmic microwave background. Analyzing the bispectrum of the Wilkinson Microwave Anisotropy Probe 3-year data up to  $\ell_{\text{max}} = 750$  we find  $27 < f_{\text{NL}} < 147$  (95% C.L.). This amounts to a rejection of  $f_{\text{NL}} = 0$  at  $2.8\sigma$ , disfavoring canonical single-field slow-roll inflation. The signal is robust to variations in  $\ell_{\text{max}}$ , frequency and masks. No known foreground, instrument systematic, or secondary anisotropy explains it. We explore the impact of several analysis choices on the quoted significance and find  $2.5\sigma$  to be conservative.

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## FIVE-YEAR WILKINSON MICROWAVE ANISOTROPY PROBE (WMAP<sup>1</sup>) OBSERVATIONS: COSMOLOGICAL INTERPRETATION

E. KOMATSU<sup>1</sup>, J. DUNKLEY<sup>2,3,4</sup>, M. R. NOLTA<sup>5</sup>, C. L. BENNETT<sup>6</sup>, B. GOLD<sup>6</sup>, G. HINSHAW<sup>7</sup>, N. JAROSIK<sup>2</sup>, D. LARSON<sup>6</sup>, M. LIMON<sup>8</sup>, L. PAGE<sup>2</sup>, D. N. SPERGEL<sup>3,9</sup>, M. HALPERN<sup>10</sup>, R. S. HILL<sup>11</sup>, A. KOGUT<sup>7</sup>, S. S. MEYER<sup>12</sup>, G. S. TUCKER<sup>13</sup>, J. L. WEILAND<sup>10</sup>, E. WOLLACK<sup>7</sup>, AND E. L. WRIGHT<sup>14</sup>

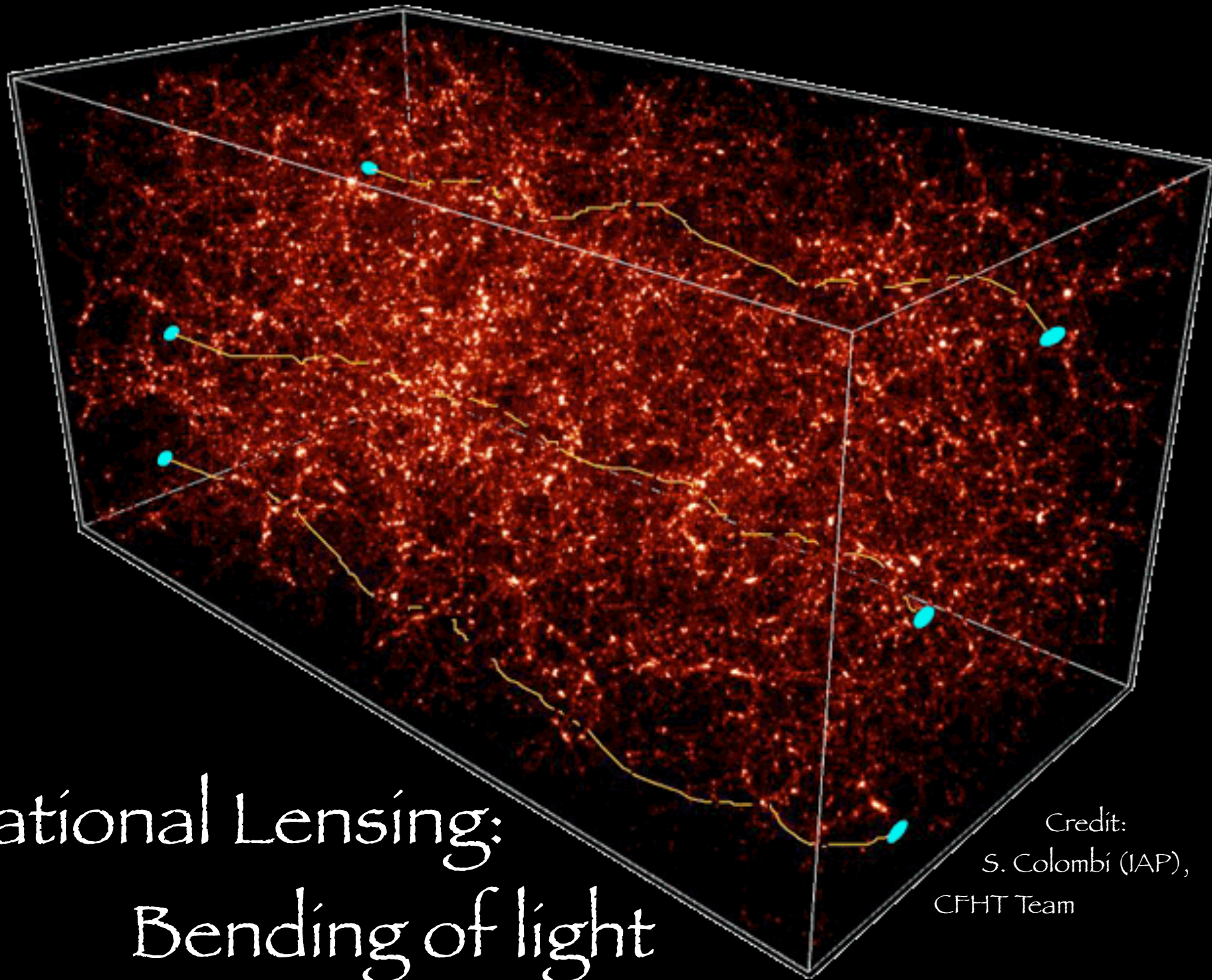
*Submitted to the Astrophysical Journal Supplement Series*

### ABSTRACT

$$-9 < f_{\text{NL}}^{\text{local}} < 111 \text{ and } -151 < f_{\text{NL}}^{\text{equil}} < 253 (95\% \text{ CL})$$



# Journey Through the “Clumpy” Universe

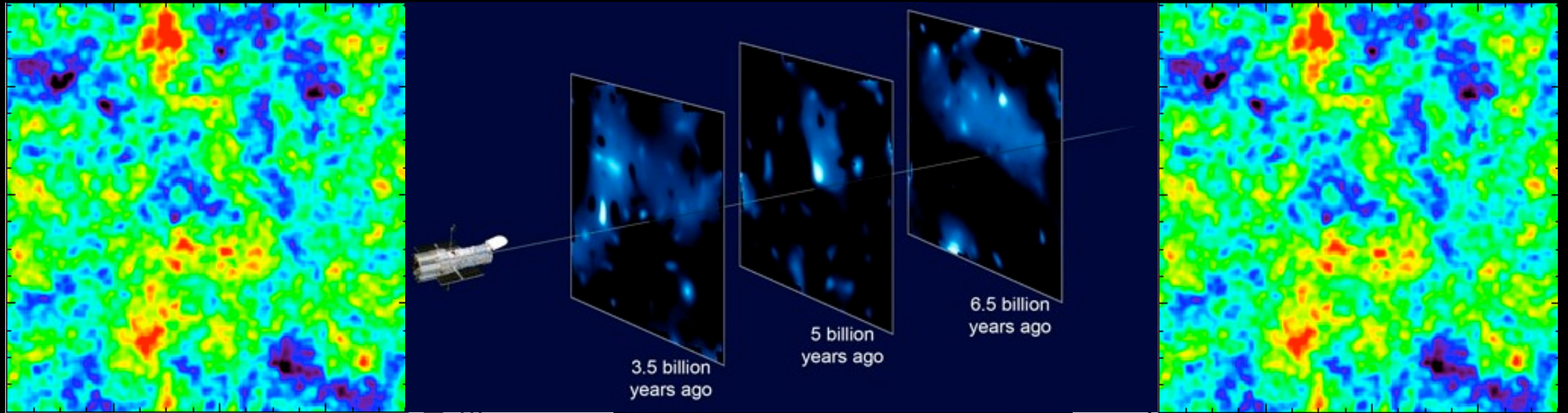


Weak  
Gravitational Lensing:  
Bending of light

Credit:  
S. Colombi (IAP),  
CFHT Team



# Weak Lensing of the Primary Bispectrum



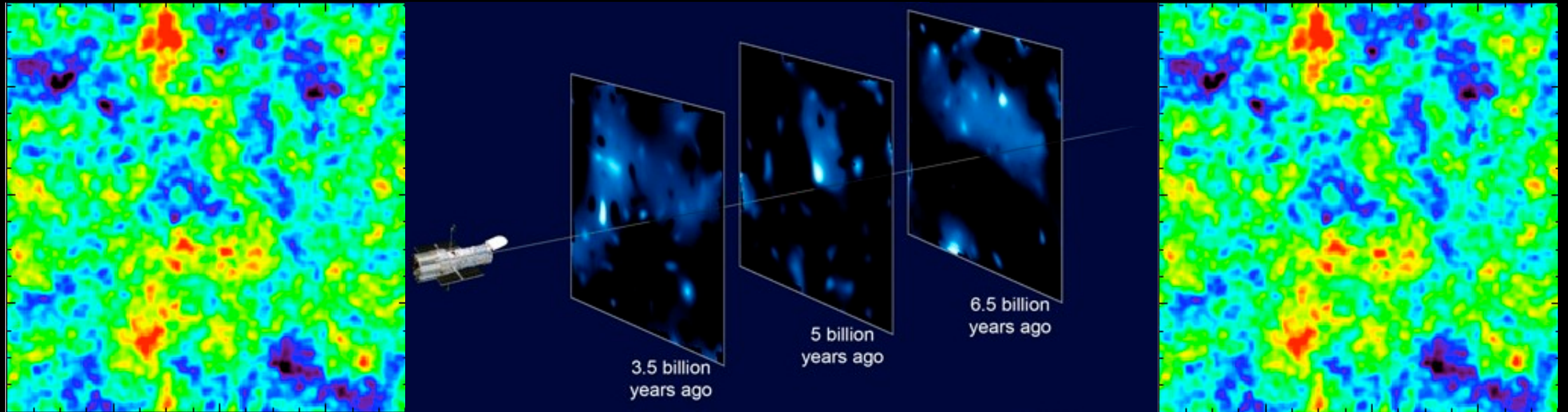
Credit: Vale, Amblard, White (2004)

NASA, ESA, and R. Massey (CalTech)

Credit: Vale, Amblard, White (2004)



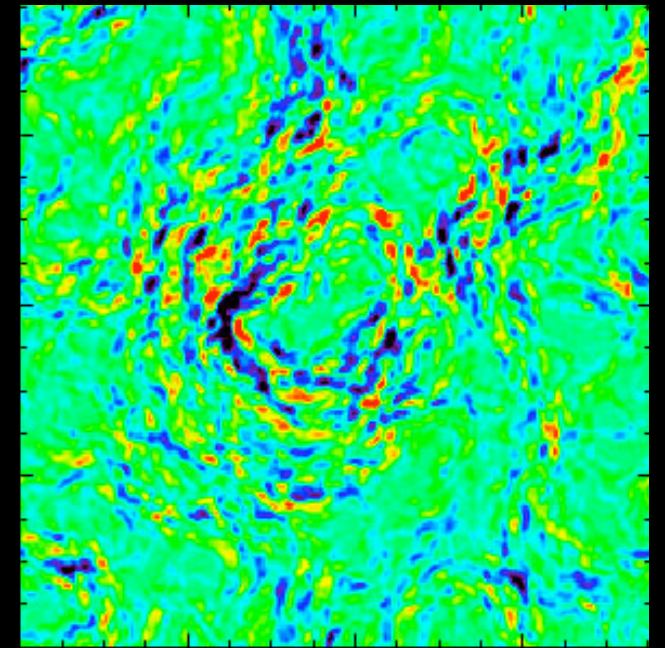
# Weak Lensing of the Primary Bispectrum



Credit: Vale, Amblard, White (2004)

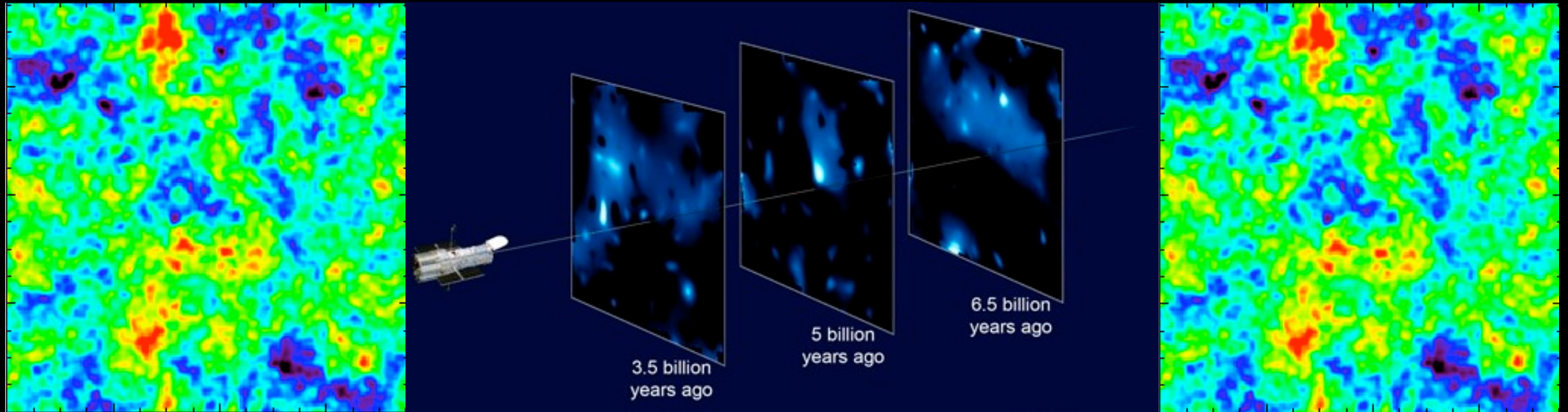
NASA, ESA, and R. Massey (CalTech)

Credit: Vale, Amblard, White (2004)





# Weak Lensing of the Primary Bispectrum

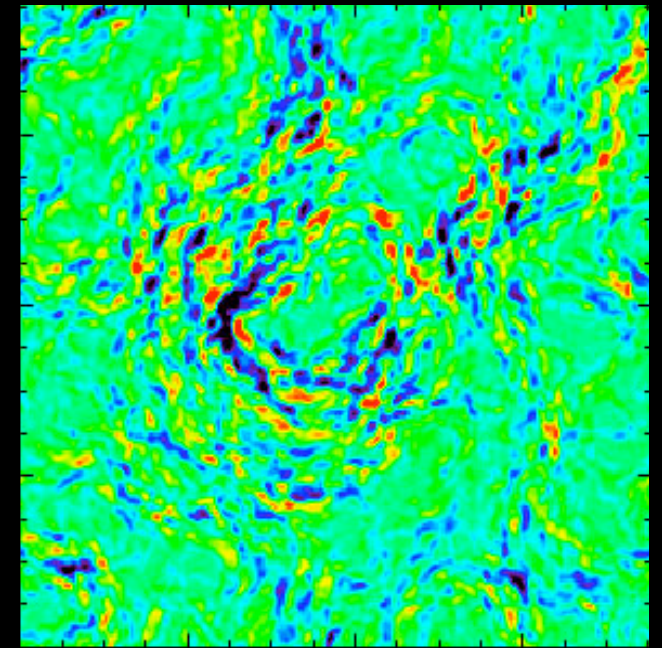


Credit: Vale, Amblard, White (2004)

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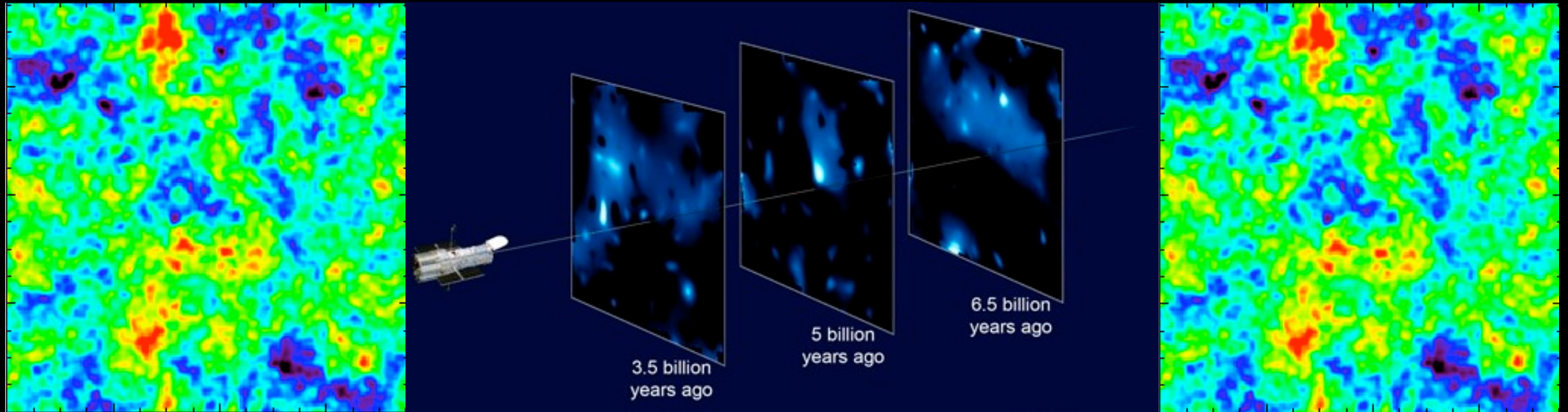
Credit: Vale, Amblard, White (2004)

$$\tilde{\Theta}(\hat{\mathbf{n}}) = \Theta[\hat{\mathbf{n}} + \hat{\alpha}]$$





# Weak Lensing of the Primary Bispectrum

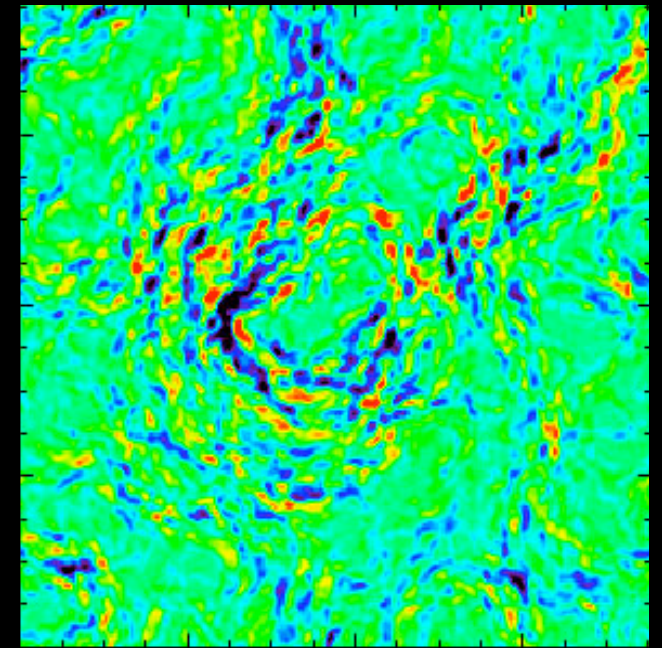


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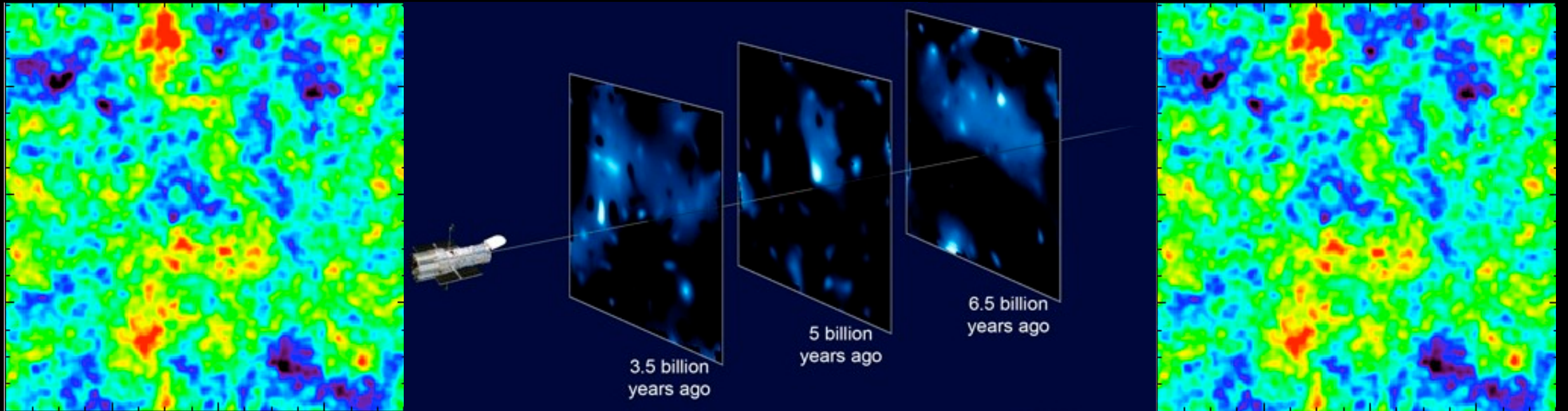
Credit: Vale, Amblard, White (2004)

$$\begin{aligned}\tilde{\Theta}(\hat{\mathbf{n}}) &= \Theta[\hat{\mathbf{n}} + \hat{\alpha}] \\ &= \Theta[\hat{\mathbf{n}} + \nabla\phi(\hat{\mathbf{n}})]\end{aligned}$$





# Weak Lensing of the Primary Bispectrum

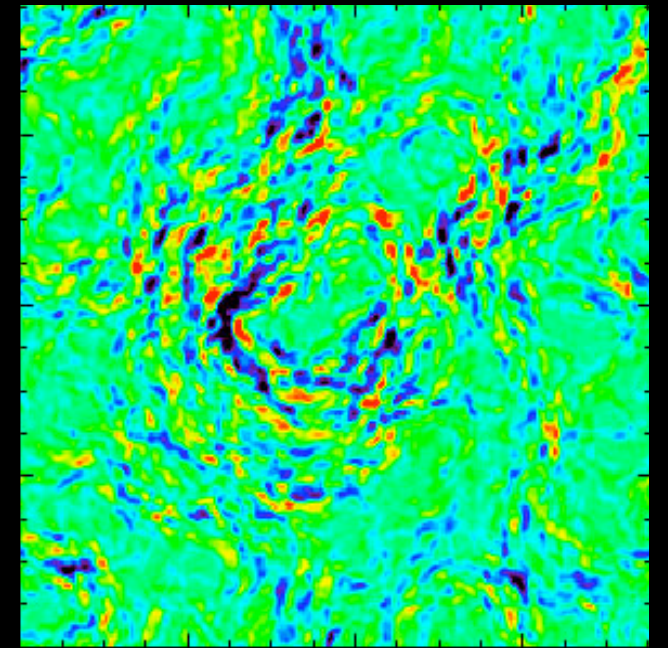


Credit: Vale, Amblard, White (2004)

NASA, ESA, and R. Massey (CalTech)

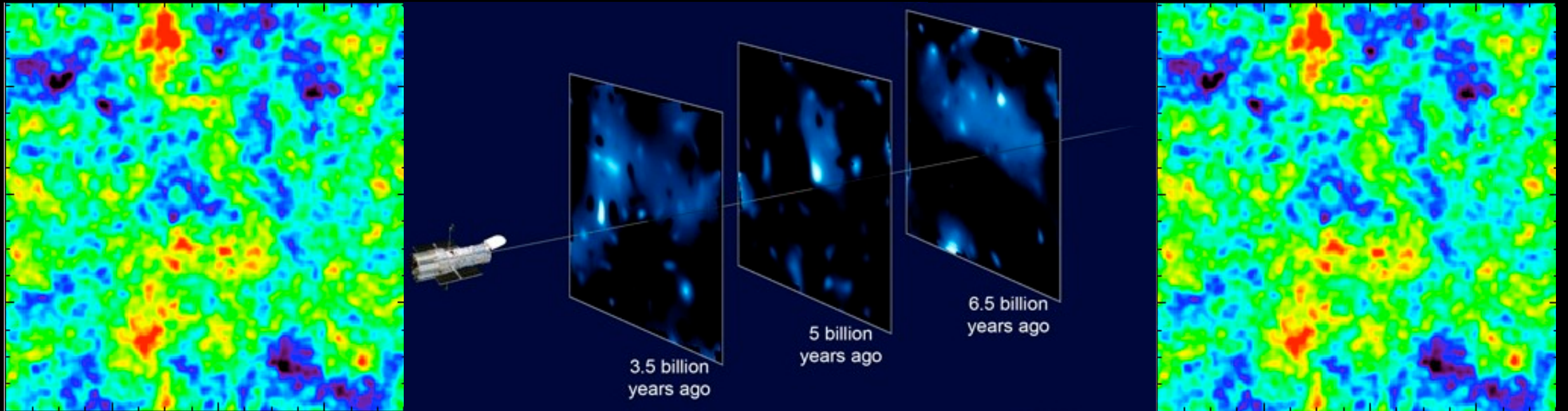
Credit: Vale, Amblard, White (2004)

$$\begin{aligned}
 \tilde{\Theta}(\hat{\mathbf{n}}) &= \Theta[\hat{\mathbf{n}} + \hat{\alpha}] \\
 &= \Theta[\hat{\mathbf{n}} + \nabla\phi(\hat{\mathbf{n}})] \\
 &\approx \Theta(\hat{\mathbf{n}}) + \nabla_i\phi(\hat{\mathbf{n}})\nabla^i\Theta(\hat{\mathbf{n}}) \\
 &\quad + \frac{1}{2}\nabla_i\phi(\hat{\mathbf{n}})\nabla_j\phi(\hat{\mathbf{n}})\nabla^i\nabla^j\Theta(\hat{\mathbf{n}})
 \end{aligned}$$





# Weak Lensing of the Primary Bispectrum

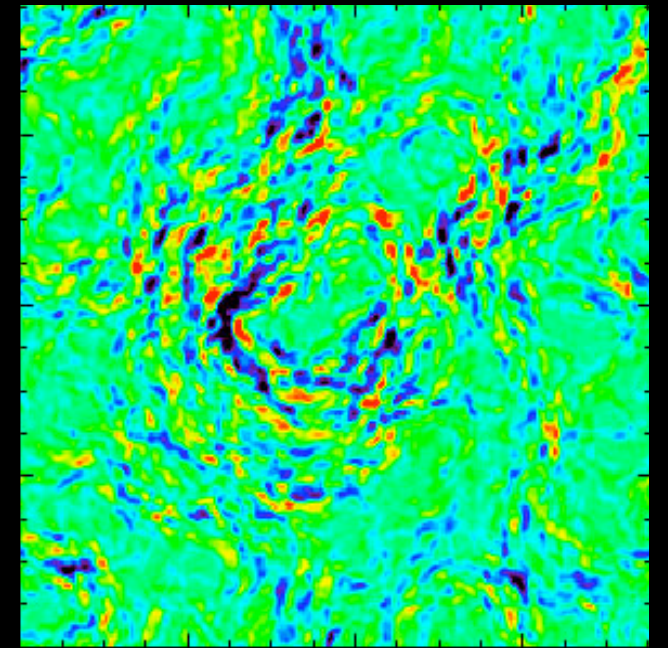


Credit: Vale, Amblard, White (2004)

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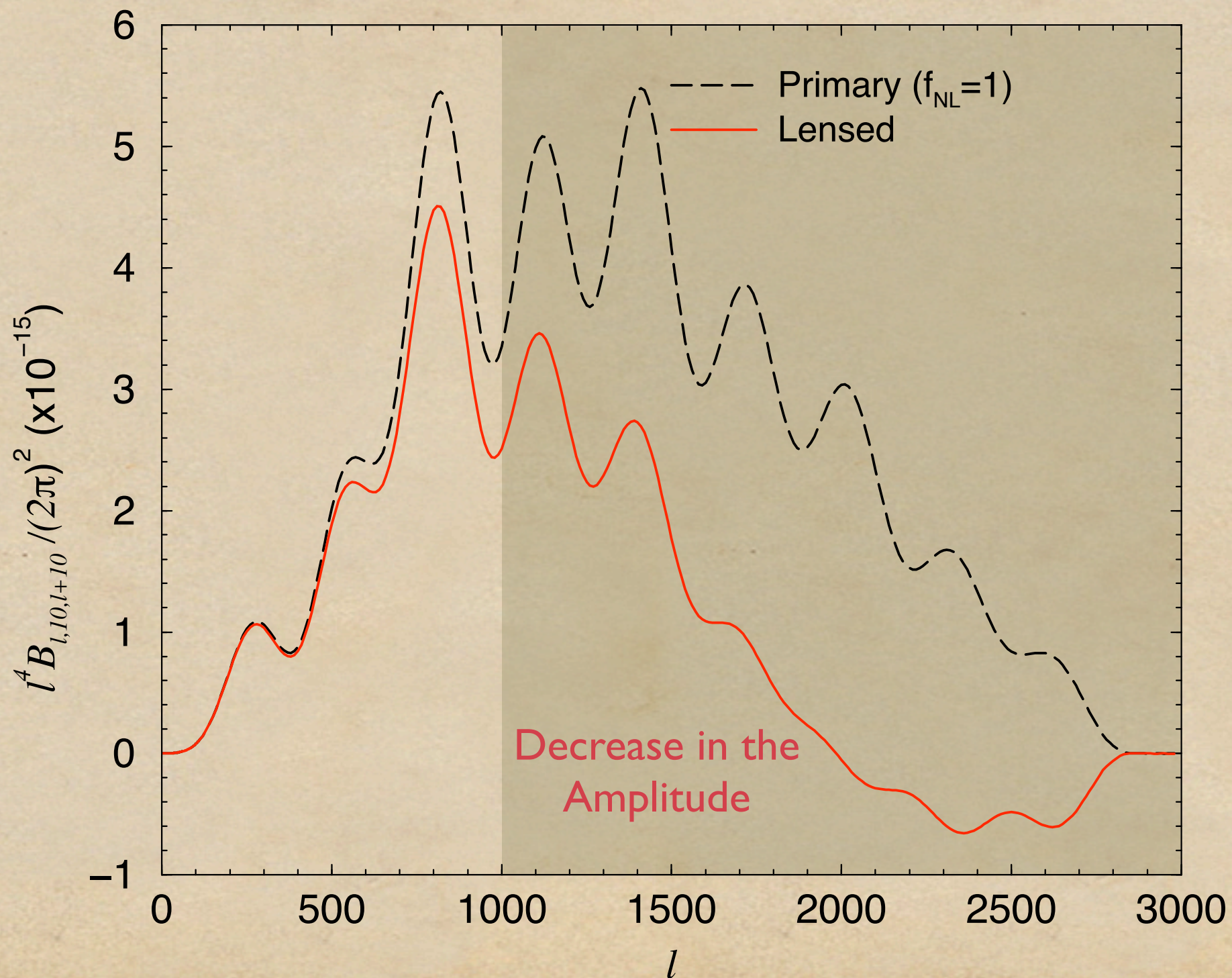
$$\begin{aligned}
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 &\quad + \frac{1}{2}\nabla_i\phi(\hat{\mathbf{n}})\nabla_j\phi(\hat{\mathbf{n}})\nabla^i\nabla^j\Theta(\hat{\mathbf{n}})
 \end{aligned}$$



$$\tilde{B}_{l_1 l_2 l_3}^{\Theta} = \sum_{m_1 m_2 m_3} \begin{pmatrix} l_1 & l_2 & l_3 \\ m_1 & m_2 & m_3 \end{pmatrix} \langle \tilde{\Theta}_{l_1 m_1} \tilde{\Theta}_{l_2 m_2} \tilde{\Theta}_{l_3 m_3} \rangle$$

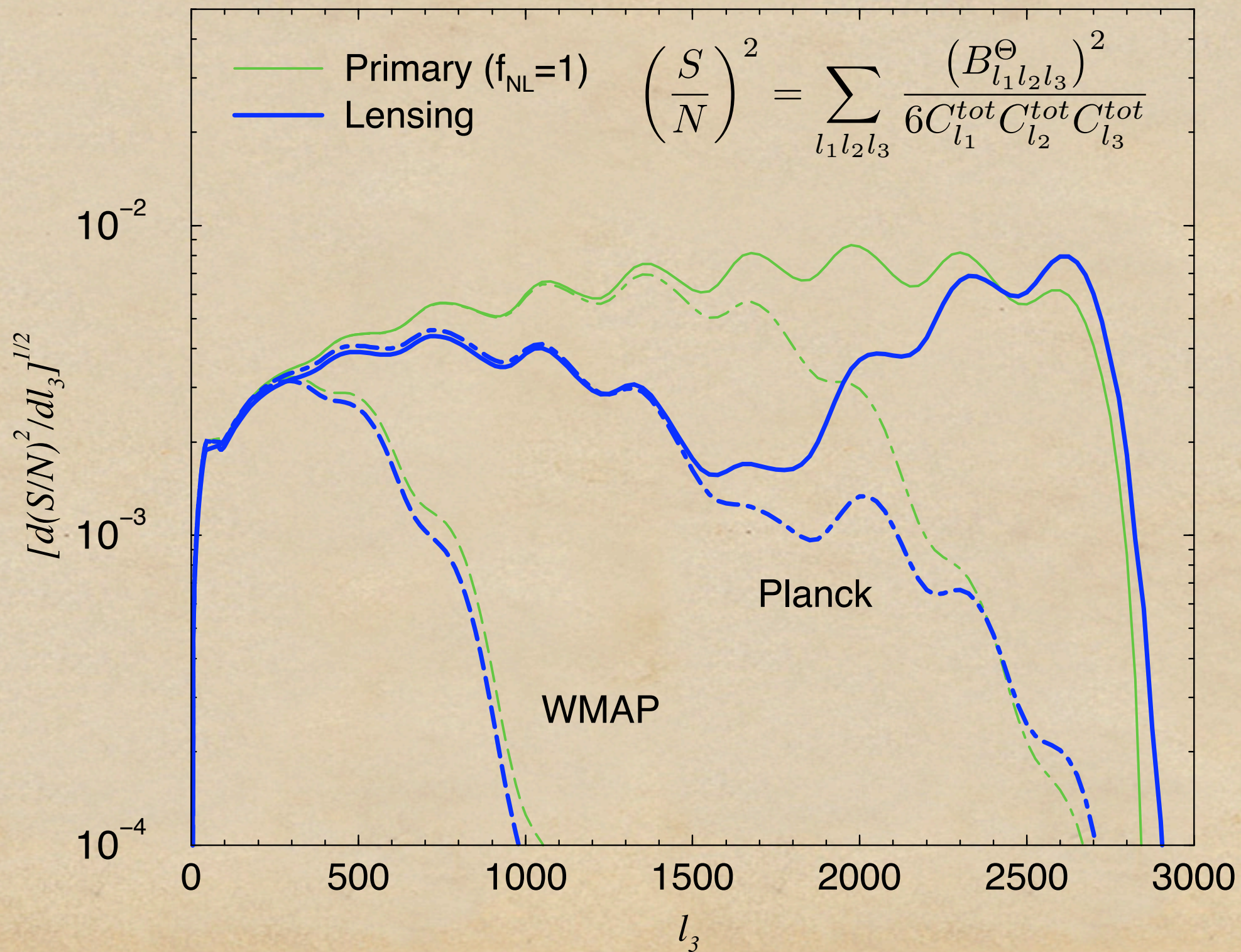


# The Effect of Lensing on the Bispectrum



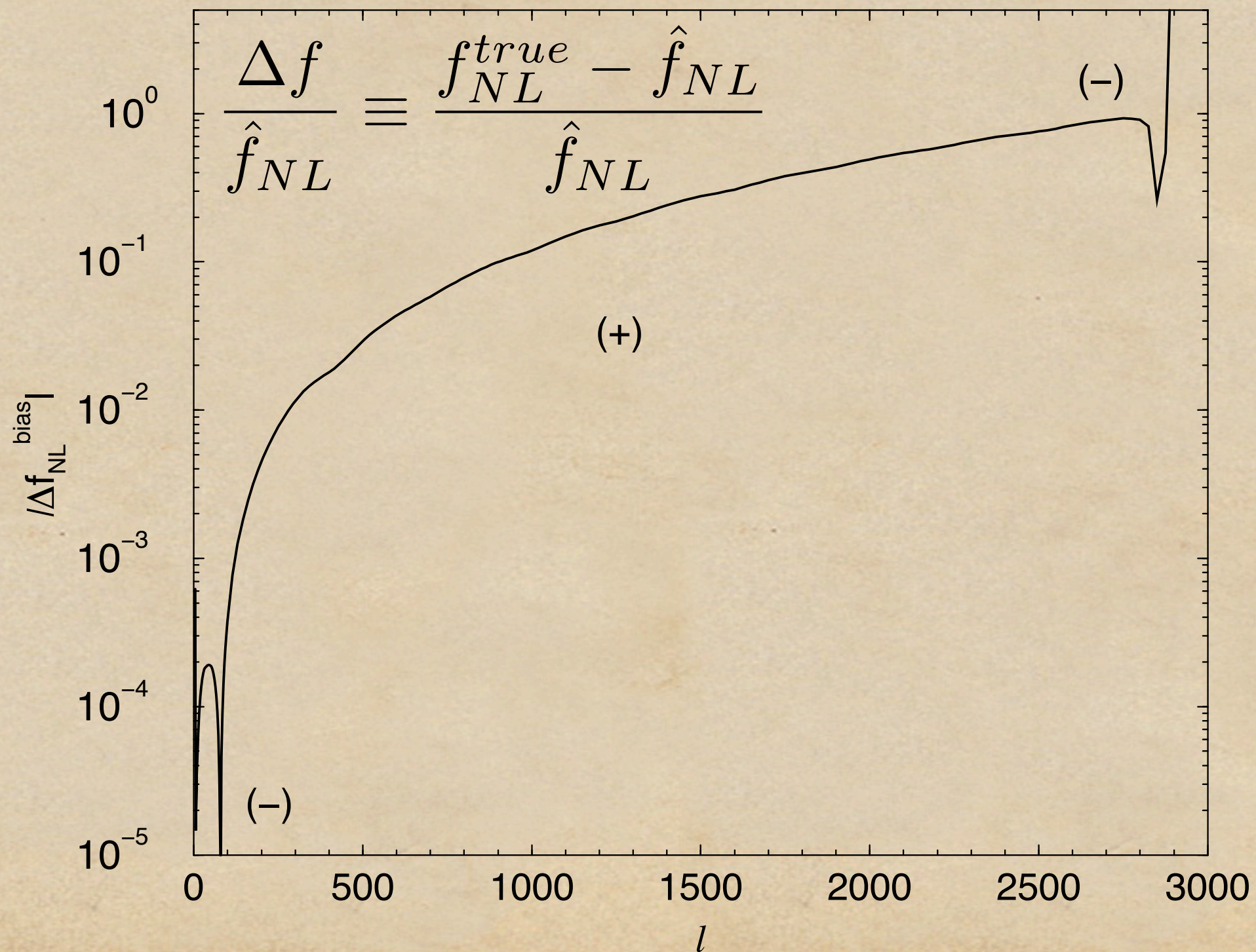


# Reduction in the S/N due to Lensing



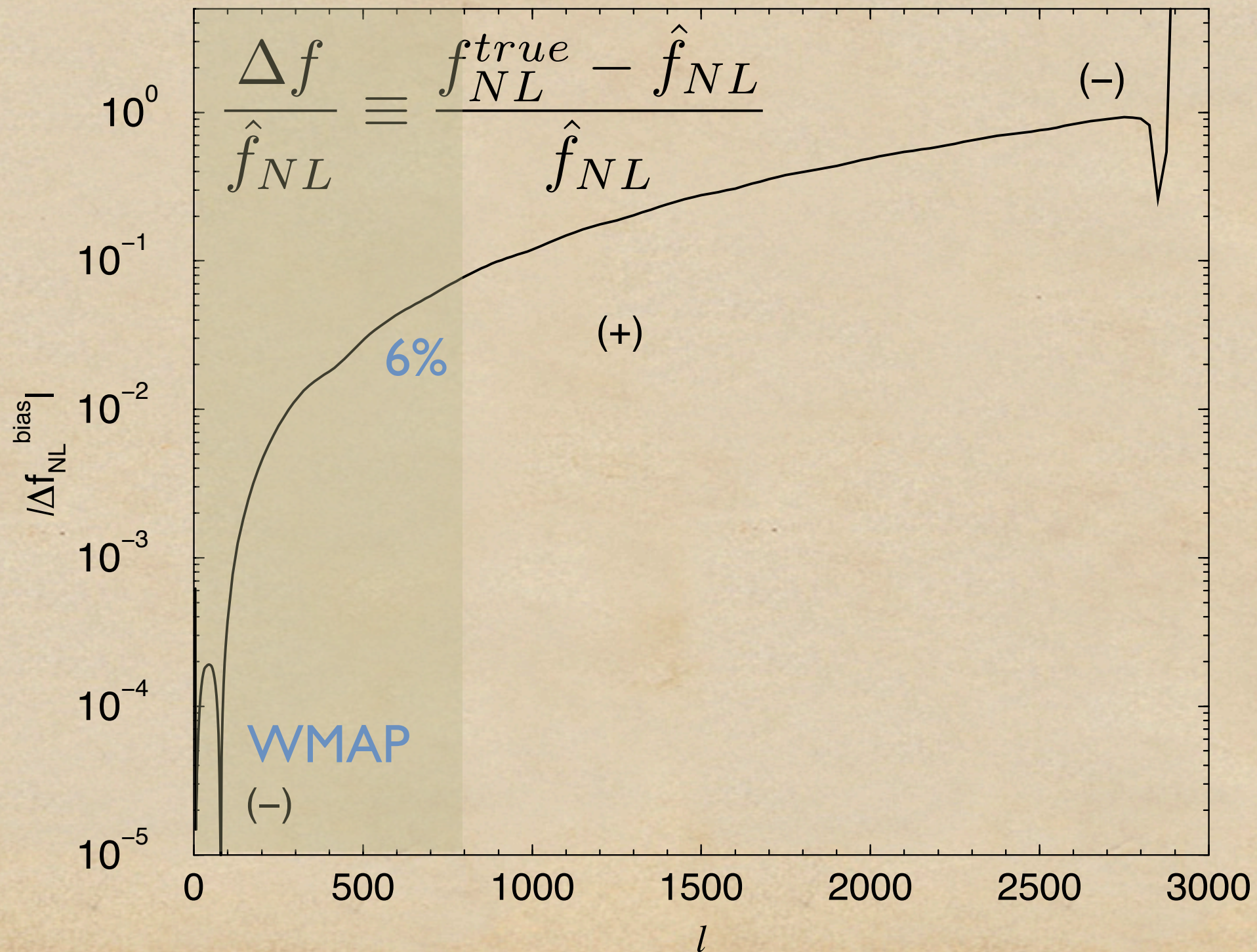


# Bias in the non-Gaussian Parameter



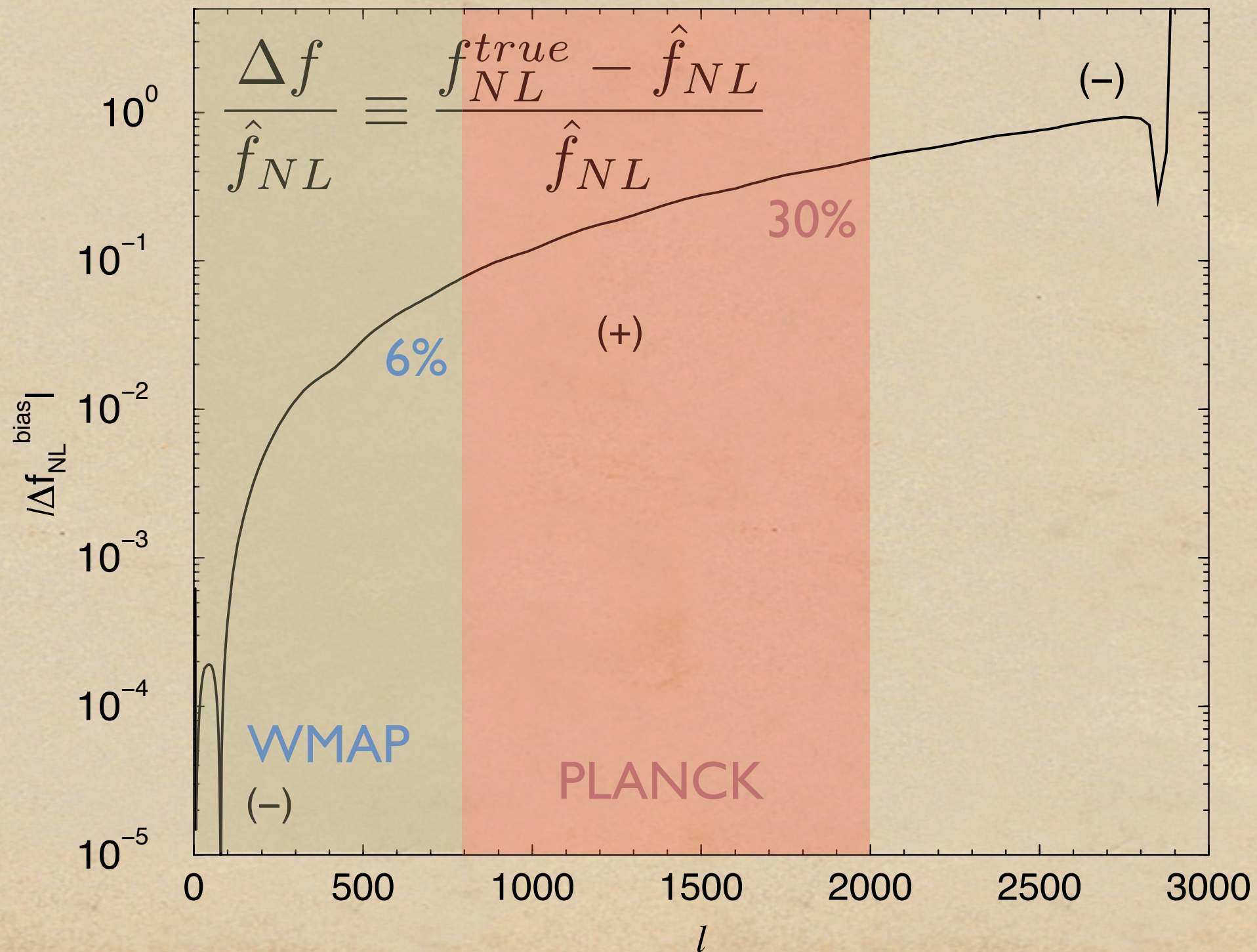


# Bias in the non-Gaussian Parameter



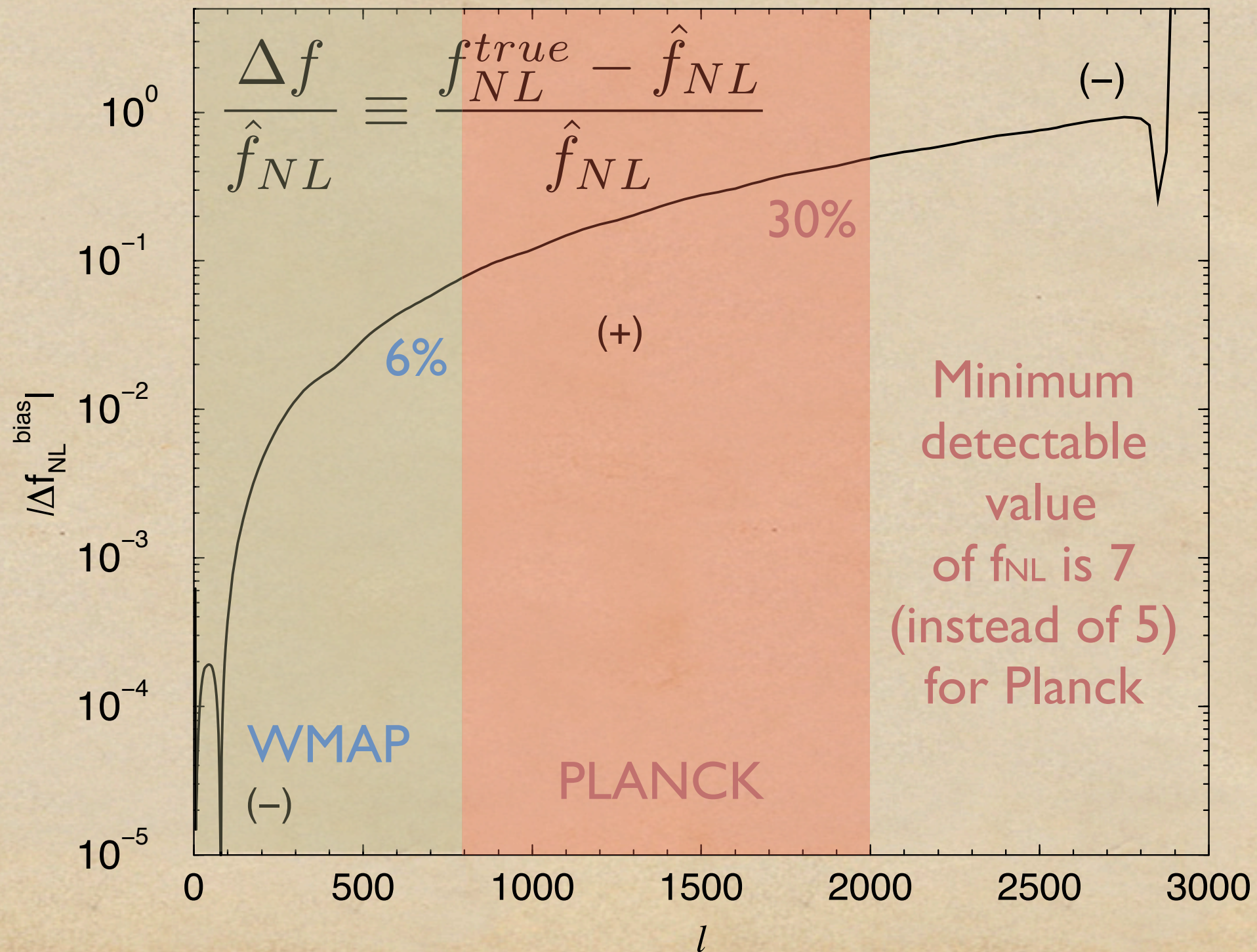


# Bias in the non-Gaussian Parameter





# Bias in the non-Gaussian Parameter





# Agenda

## Dark Energy

- ✧ Constraining the EOS
- ✧ To Bin or Not to Bin
- ✧ SNe Ia ++
- ✧ Lensing of SNe
- ✧ Other Worries

## Non-Gaussianity

- ✧ Beyond Gaussianity
- ✧ CMB Bispectrum
- ✧ Lensing of CMB
- ✧ Lensed Bispectrum
- ✧ S/N Reduction & Bias

Gravity Waves via  
Weak Gravitational Lensing



# Agenda

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## Non-Gaussianity

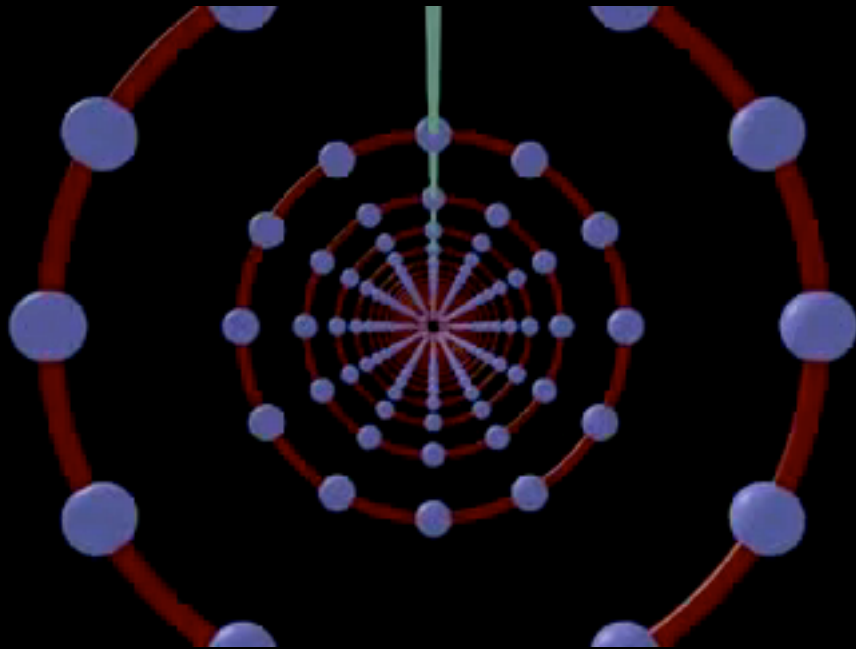
- &• Beyond Gaussianity
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Gravity Waves via  
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# Gravitational Waves

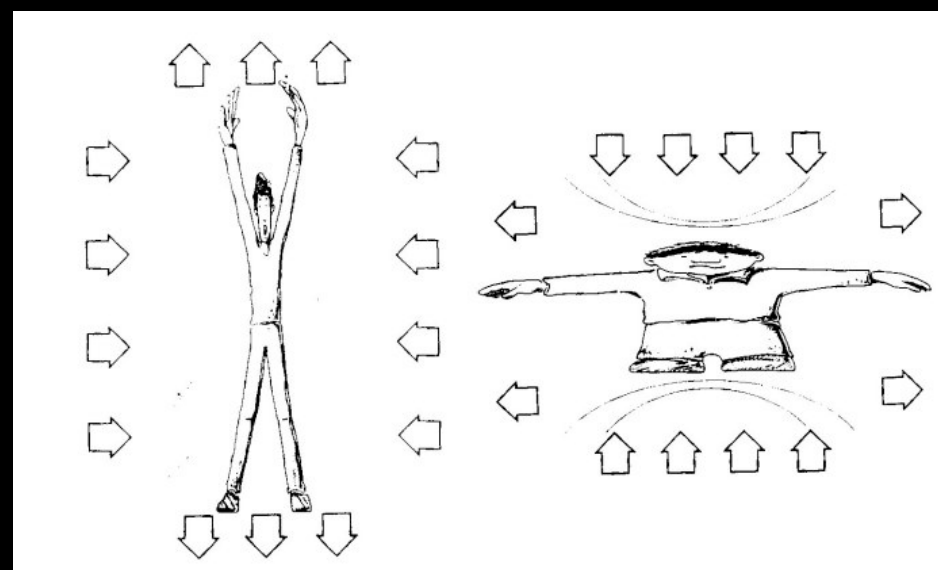
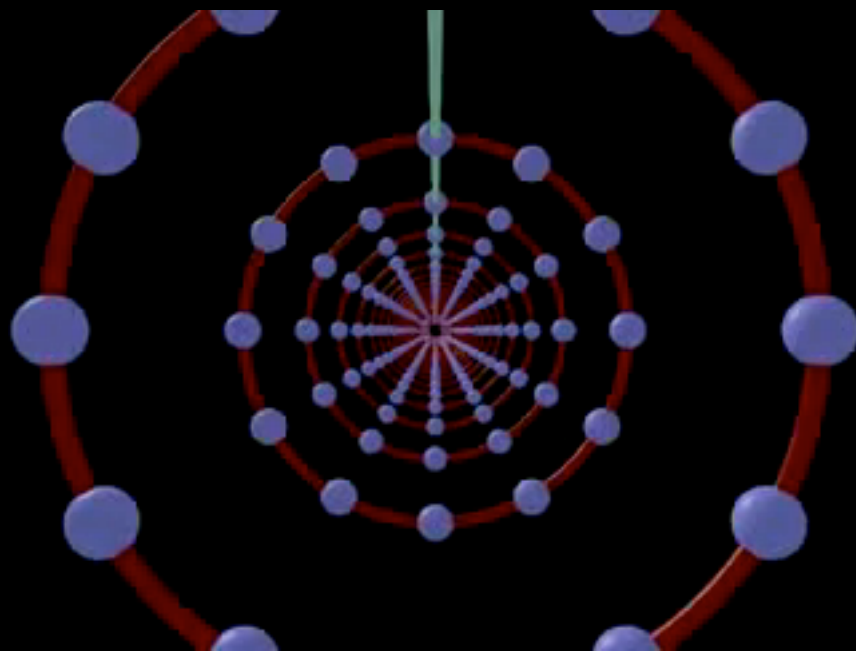
Credit: Michael  
Penn State Schuykill





# Gravitational Waves

Credit: Michael  
Penn State Schuyllkill

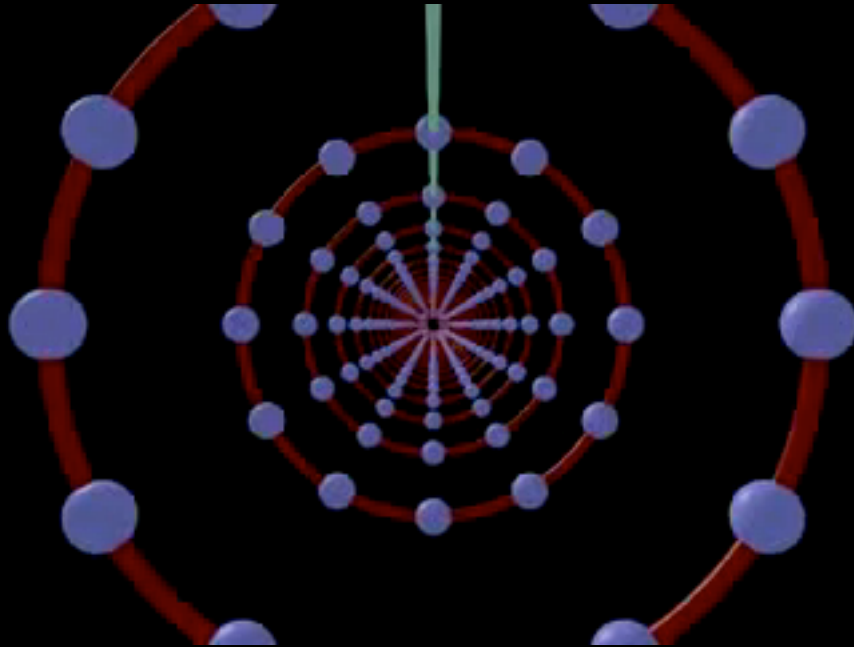


credit: <http://www.inl.infn.it/~auriga/>

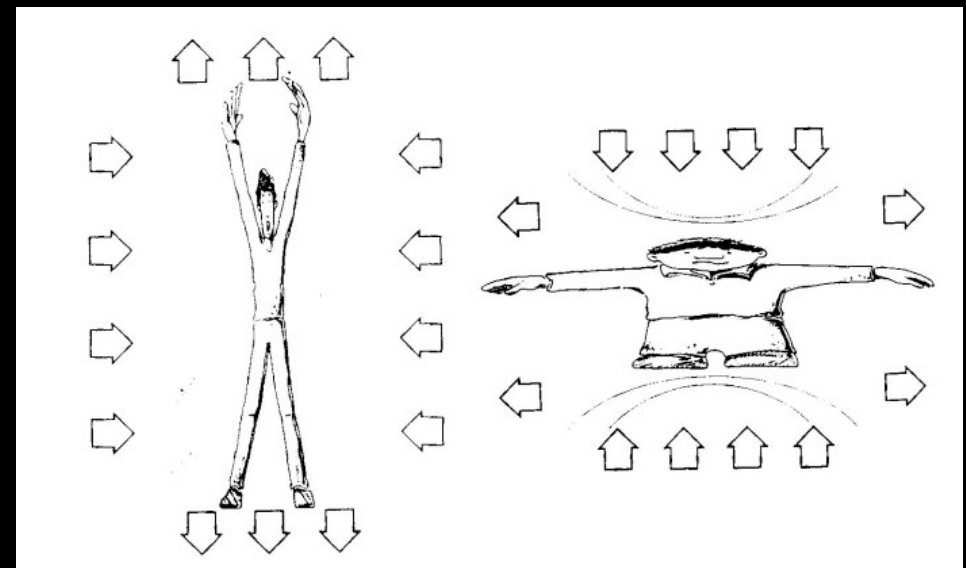
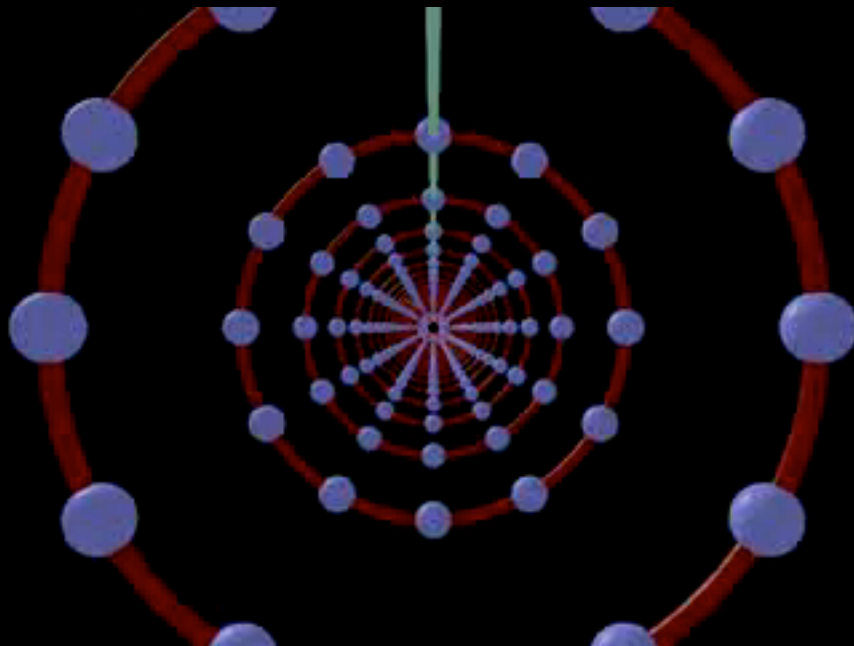


# Gravitational Waves

Credit: Michael  
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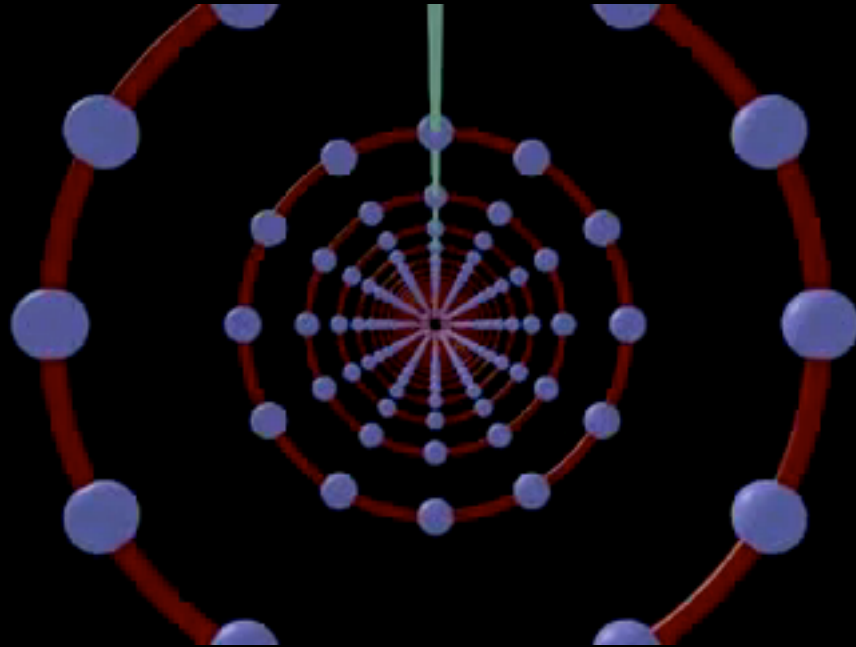


credit: <http://www.inl.infn.it/~auriga/>

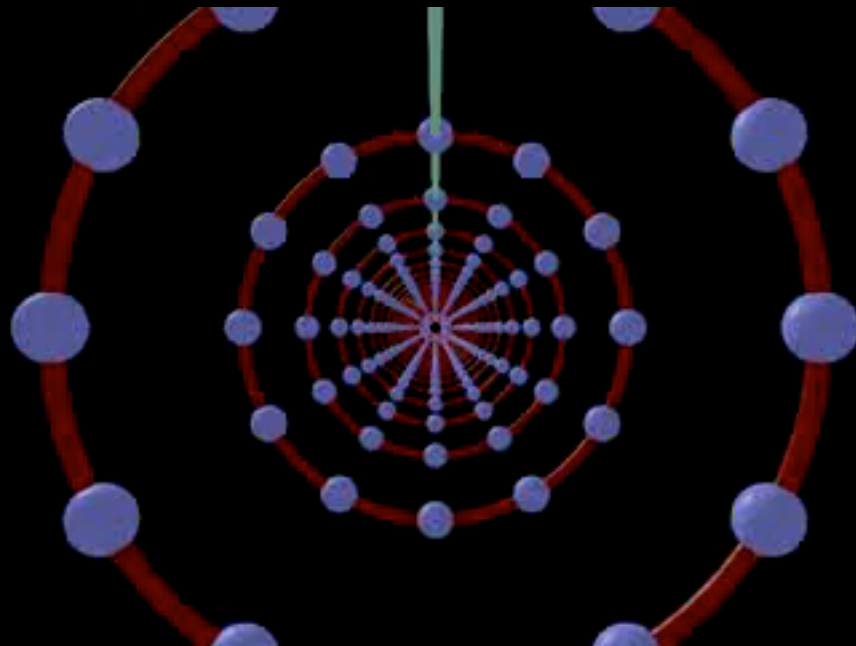


# Gravitational Waves

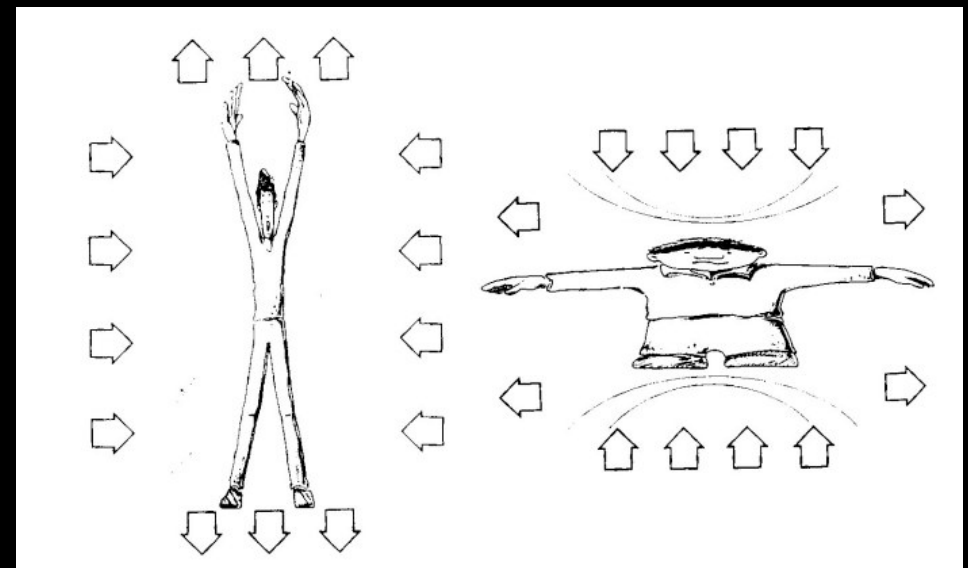
Credit: Michael  
Penn State Schuykill



Credit: Michael  
Penn State Schuykill



Credit: GSFC/D. Berry



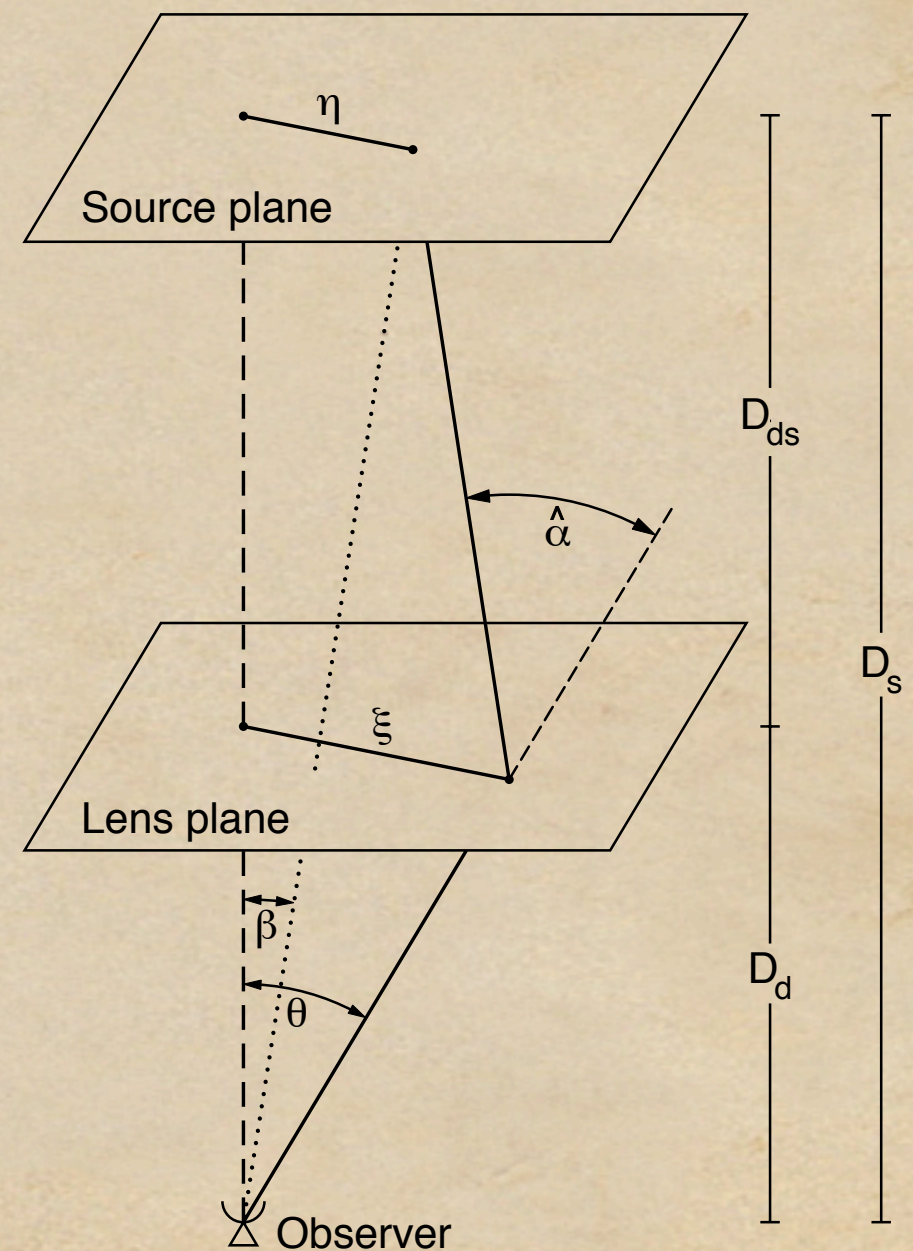
credit: <http://www.inl.infn.it/~auriga/>



# Gravitational Lensing and GW

The Deflection:

$$\vec{\beta} = \vec{\theta} - \vec{\alpha}(\vec{\theta})$$



Credit: Bartelmann and Schneider 2001

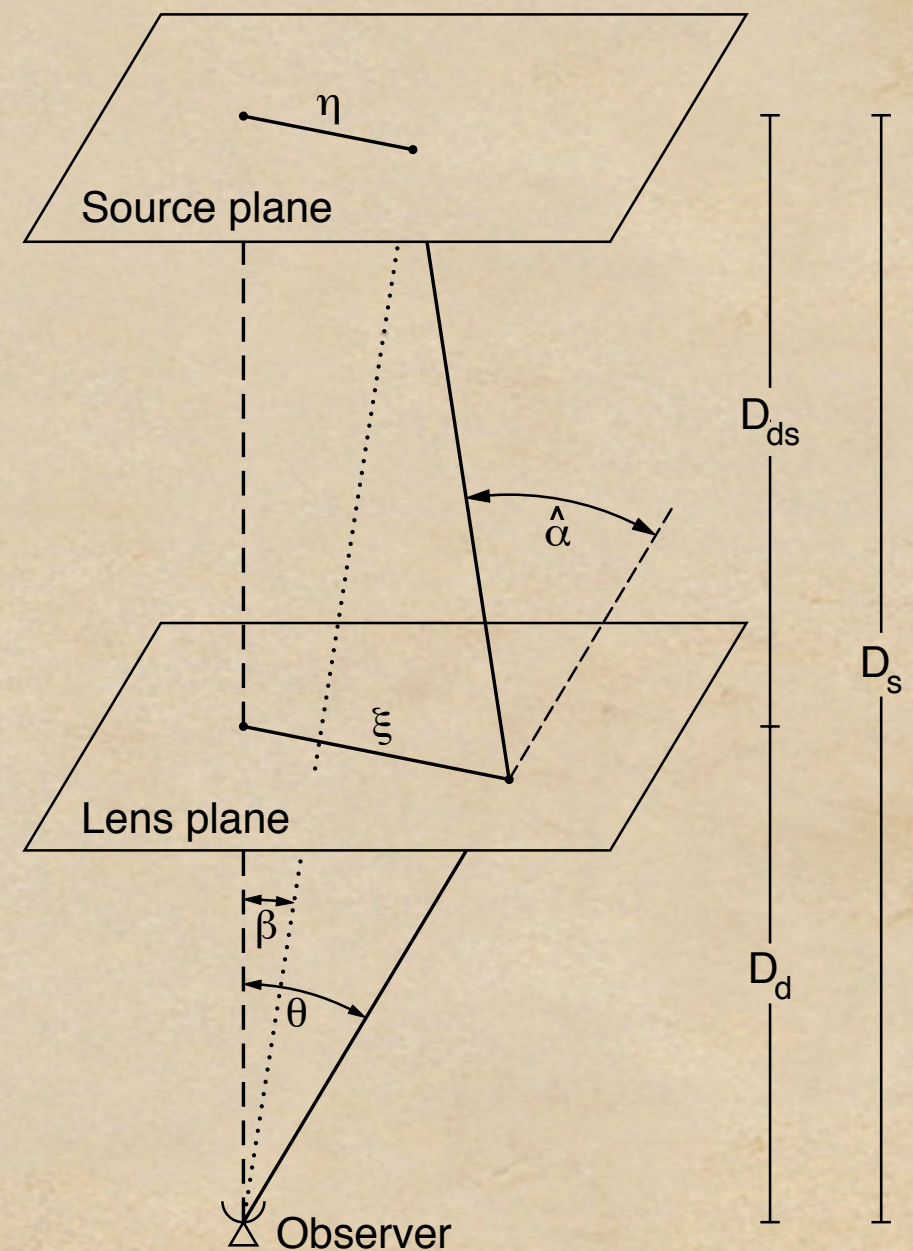


# Gravitational Lensing and GW

The Deflection:

$$\vec{\beta} = \vec{\theta} - \vec{\alpha}(\vec{\theta})$$

$$\vec{\alpha}(\vec{\theta}) = \nabla \phi$$



Credit: Bartelmann and Schneider 2001



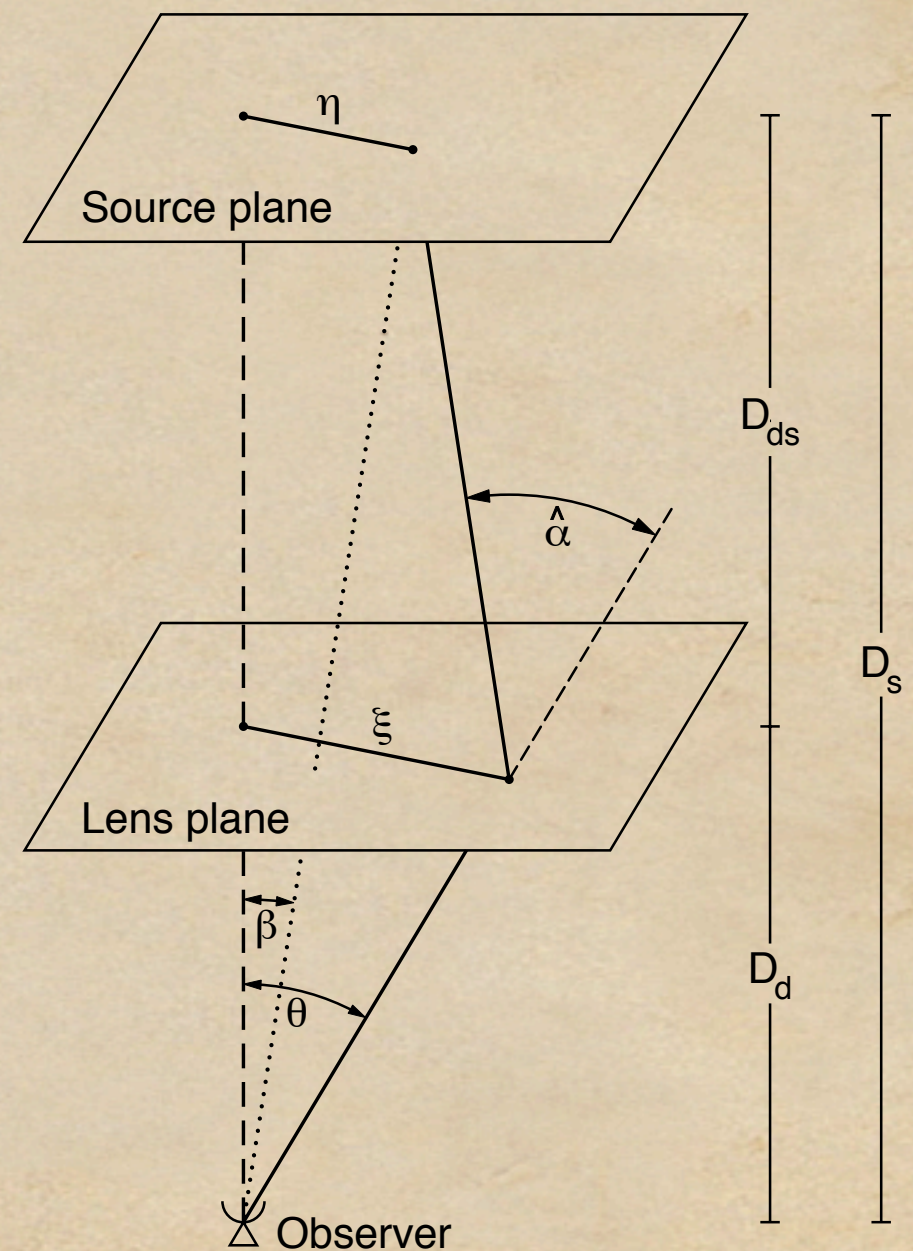
# Gravitational Lensing and GW

The Deflection:

$$\vec{\beta} = \vec{\theta} - \vec{\alpha}(\vec{\theta})$$

$$A_{ij} = \frac{\partial x_i^S}{\partial x_j^I}$$

$$\vec{\alpha}(\vec{\theta}) = \nabla \phi$$



Credit: Bartelmann and Schneider 2001



# Gravitational Lensing and GW

The Deflection:

$$\vec{\beta} = \vec{\theta} - \vec{\alpha}(\vec{\theta})$$

$$\alpha(\vec{\theta}) = \nabla \phi$$

$$A_{ij} = \frac{\partial x_i^S}{\partial x_j^I}$$

$$= (1 - \kappa)\delta_{ij} - \gamma_{ij} + \omega\epsilon_{ij}$$



trace

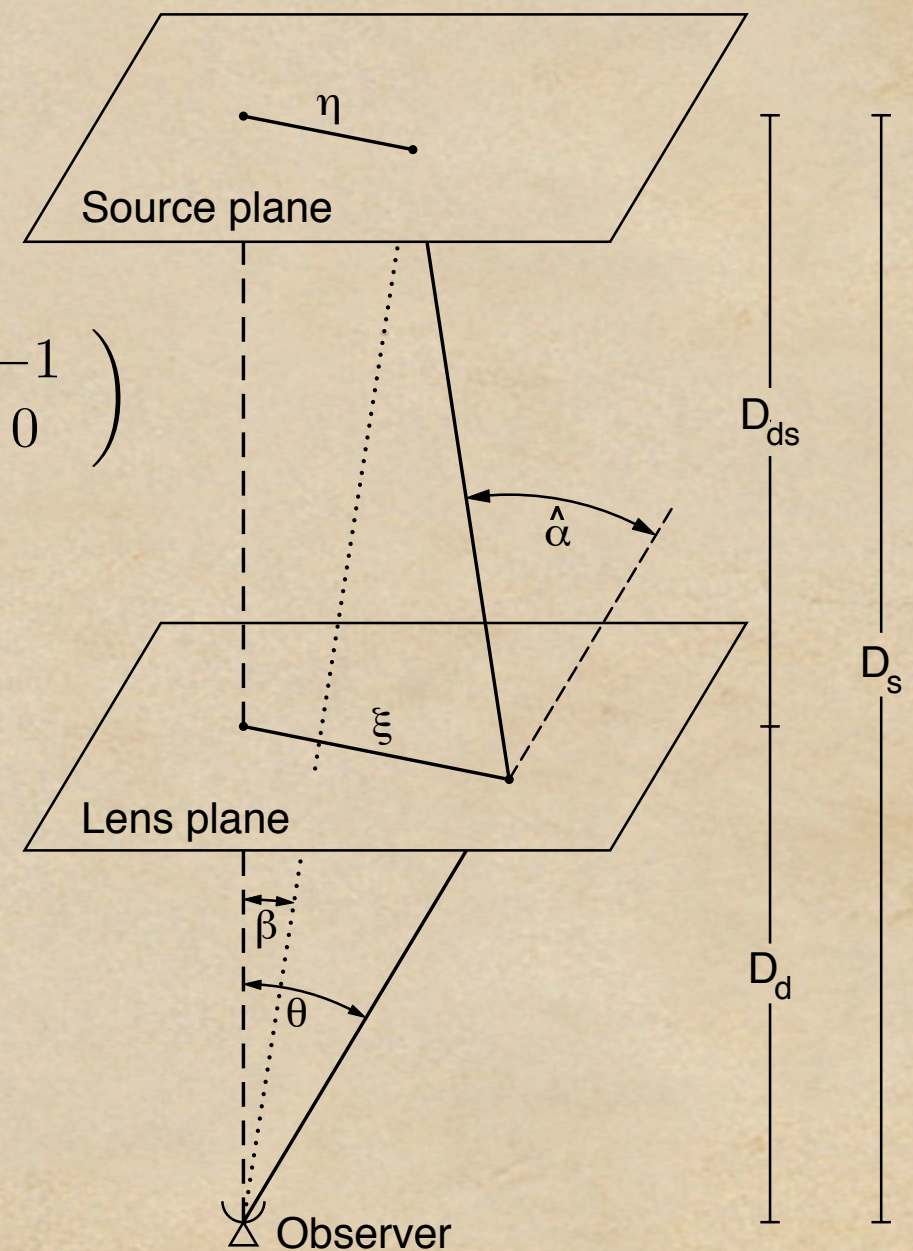


symmetric traceless



antisymmetric rotation

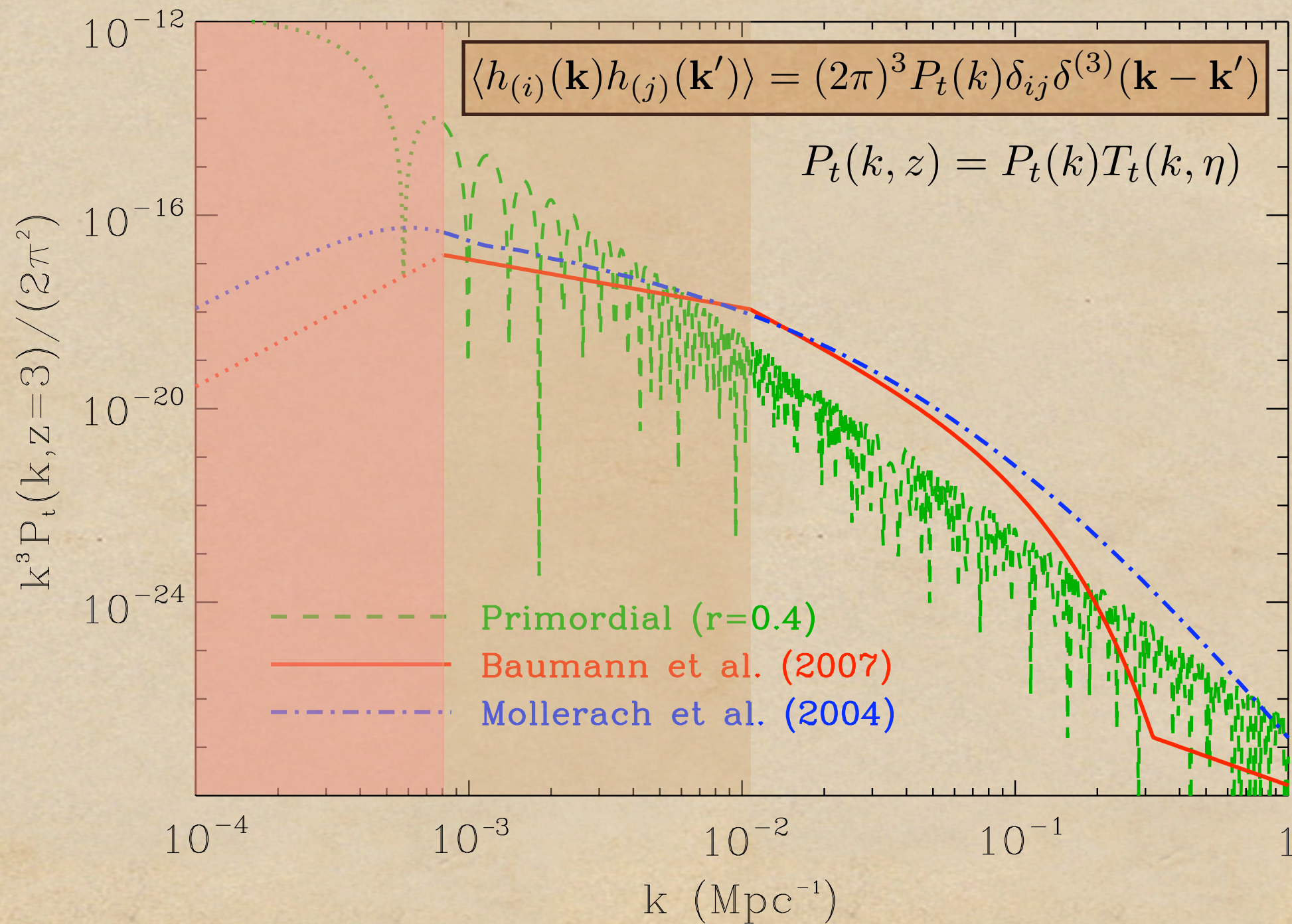
$$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$$



Credit: Bartelmann and Schneider 2001



# GW Power Spectra

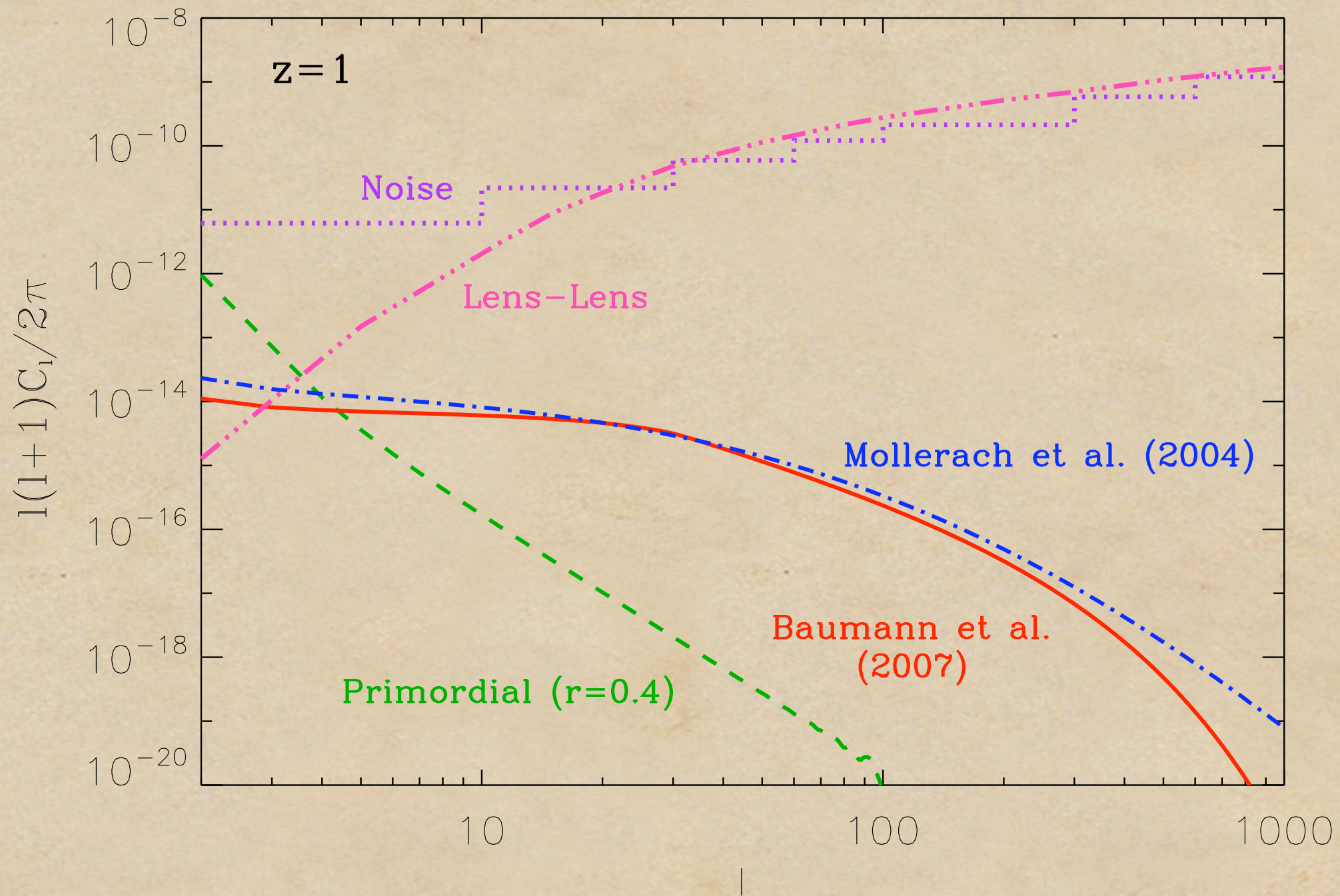


D.S., P. Serra, A. Cooray, K. Ichiki, D. Baumann,

PRD, 77, 103515 (2008)



# Cosmic Shear Curl Mode Power Spectra



D.S., P. Serra, A. Cooray, K. Ichiki, D. Baumann, PRD, 77, 103515 (2008)



# Agenda

## Dark Energy

- . Constrainíng the EOS
- . To Bín or Not to Bín
- . SNe Ia ++
- . Lensíng of SNe
- . Other Worríes

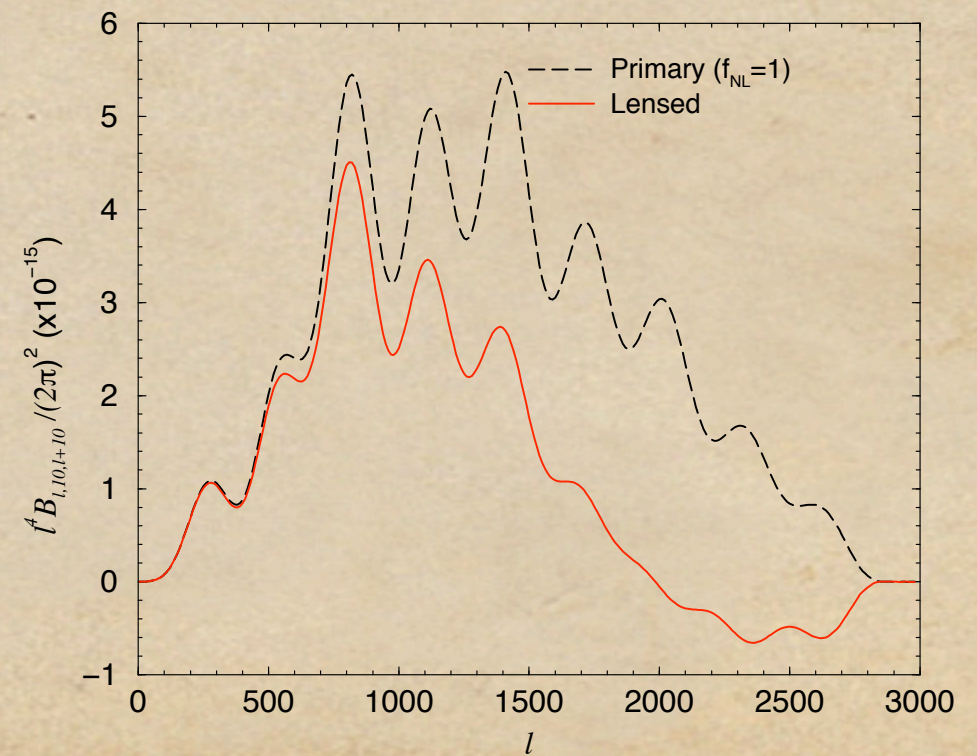
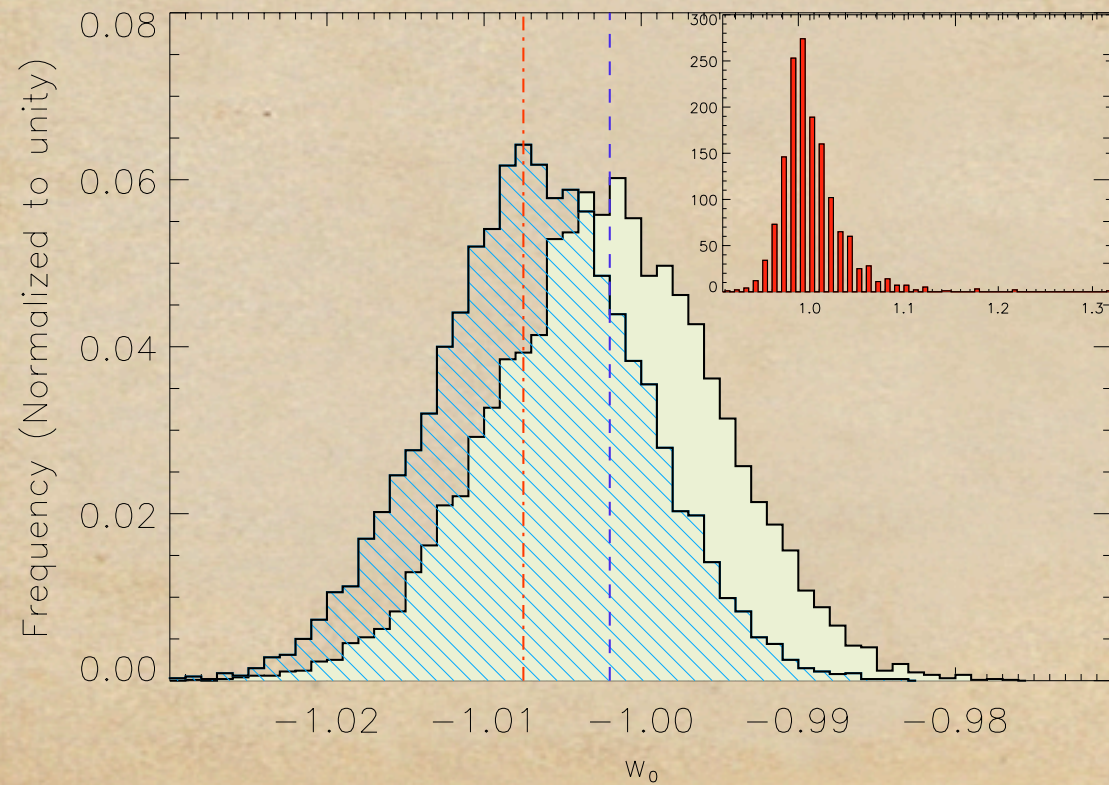
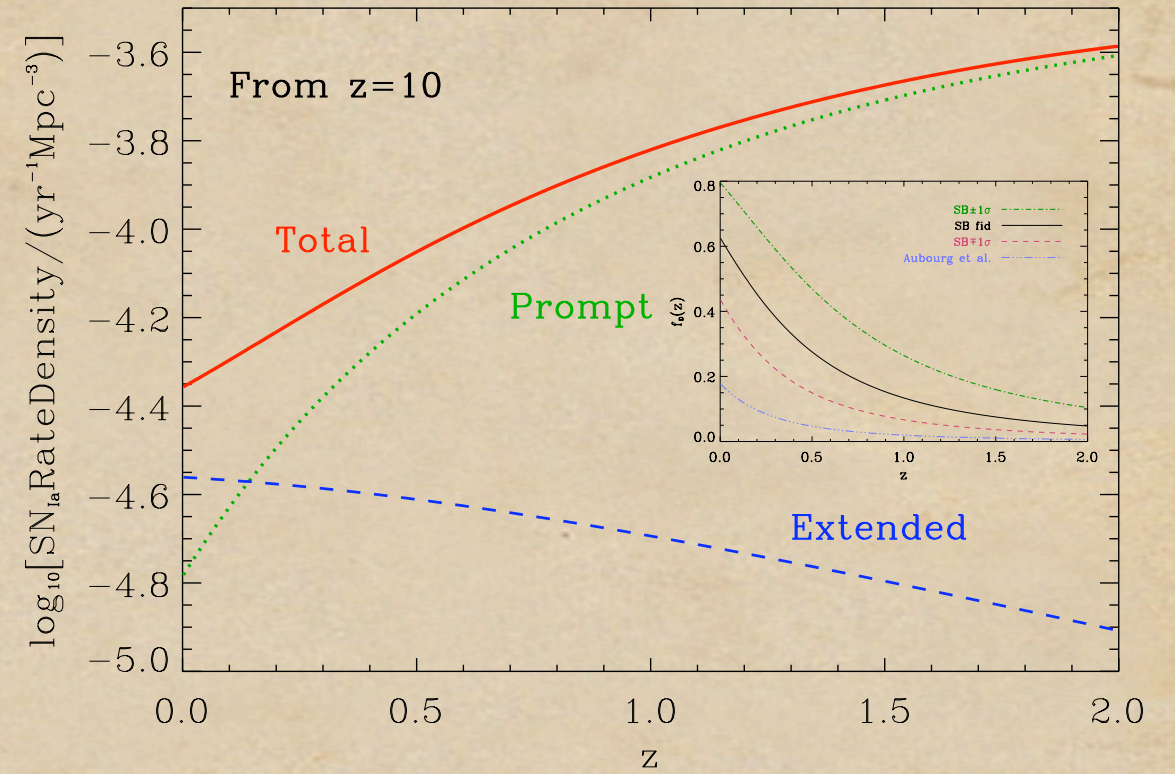
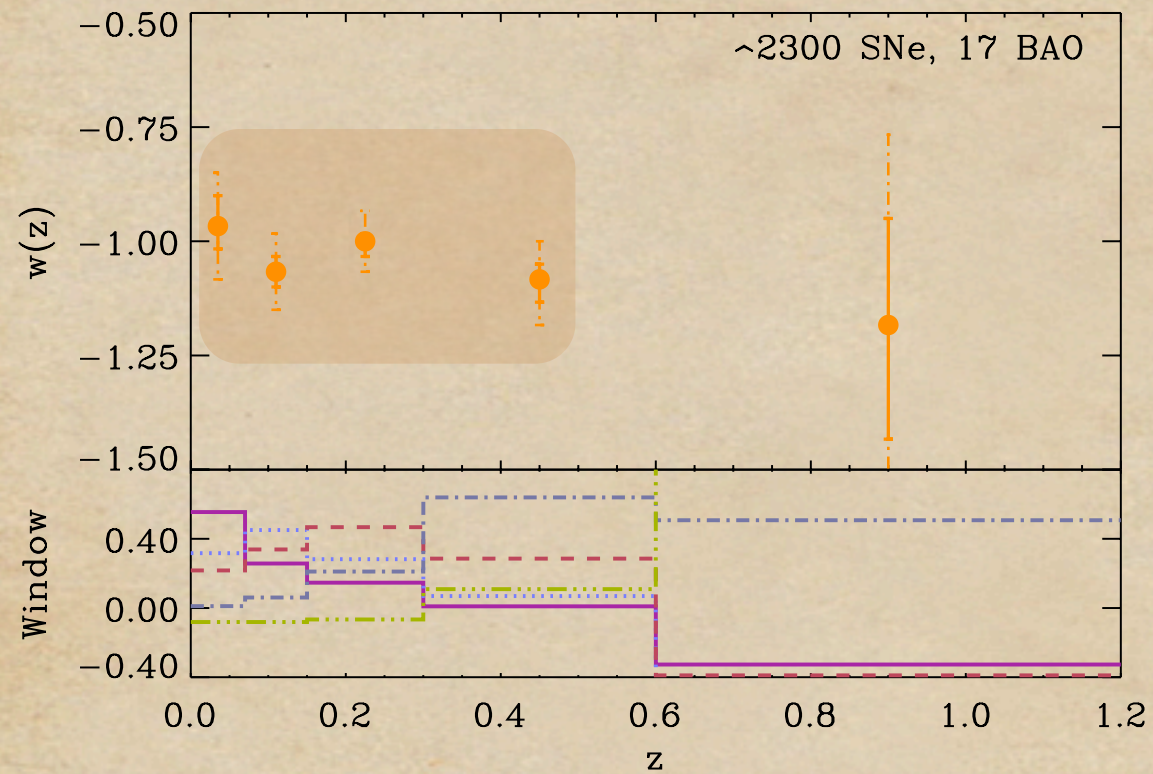
## Non-Gaussianíty

- . Beyond Gaussianíty
- . CMB Bíspectrum
- . Lensíng of CMB
- . Lensed Bíspectrum
- . S/N Reductíon & Bías

Gravity Waves vía  
Weak Gravítational Lensíng



# Summary







[dulissa.wordpress.com](http://dulissa.wordpress.com)

*DSARKAR.ORG*



# Summary

