

# At the Party with the Physicists (and some non-)...

- Coulomb got a real charge out of the whole thing.
- Einstein thought it was a relatively good time
- Cauchy, being the mathematician, still managed to integrate well with everyone.
- Thompson enjoyed the plum pudding.
- Pascal was under too much pressure to enjoy himself.
- Ohm spent most of the time resisting Ampere's opinions on current events.
- Volta thought the social had a lot of potential.
- Hilbert was pretty spaced out for most of it.
- Heisenberg may or may not have been there.
- Feynman got from the door to the buffet table by taking every possible path.
- van der Waals forced himself to mingle.
- Millikan dropped his Italian oil dressing.
- de Broglie mostly just stood in the corner and waved.
- Hollerith liked the hole idea.
- Stefan and Boltzman got into some hot debates.



# At the Party with the Physicists (and some non-)...

- Compton was a little scatter-brained at times.
- Watt turned out to be a powerful speaker.
- Hertz went back to the buffet table several times a minute.
- Faraday had quite a capacity for food.
- The microwave started radiating in the background when Penzias and Wilson showed up.
- Instead of coming through the front door Josephson tunnelled through.
- Shakespeare could not decide whether to be or not to be at the party.
- Witten bought a present all tied up with superstrings.
- The food was beautifully laid out by Mendeleyev on the periodic table.
- Maxwell's demon argued with Dawkin's friend, the selfish Gene.
- Rontgen saw through everybody.
- After one bite Chandrasekhar reached his limit.
- Gamow left the party early with a big bang while Hoyle stayed late in a steady state.



# Prospects for Probing Dark Energy & Non-Gaussianity: How Well Can We Do?

Devdeep Sarkar  
Center for Cosmology, UC Irvine

In collaboration with:

Scott Sullivan (UCI/UCLA), Shahab Joudaki (UCI), Alexandre Amblard (UCI),  
Paolo Serra (UCI), Daniel Holz (Los Alamos), Asantha Cooray (UCI).

UC Santa Barbara

Astrophysics Seminar

November 12, 2008



# Outline





# Outline

Start With...

## Dark Energy

- \* Why Pursue Dark Energy?
- \* DE Equation of State (EOS)
- \* DE from SNe Ia ++
- \* Beware of Systematics
  - Two Population Model
  - Gravitational Lensing



# Outline

Start With...

## Dark Energy

- \* Why Pursue Dark Energy?
- \* DE Equation of State (EOS)
- \* DE from SNe Ia ++
- \* Beware of Systematics
  - Two Population Model
  - Gravitational Lensing

And Then...

## CMB Bispectrum

- \* Why Non-Gaussianity?
- \* Why in CMB Bispectrum?
- \* The  $f_{NL}$
- \* WL of CMB Bispectrum
  - Analytic Sketch
  - Numerical Results



# Outline

Start With...

## Dark Energy

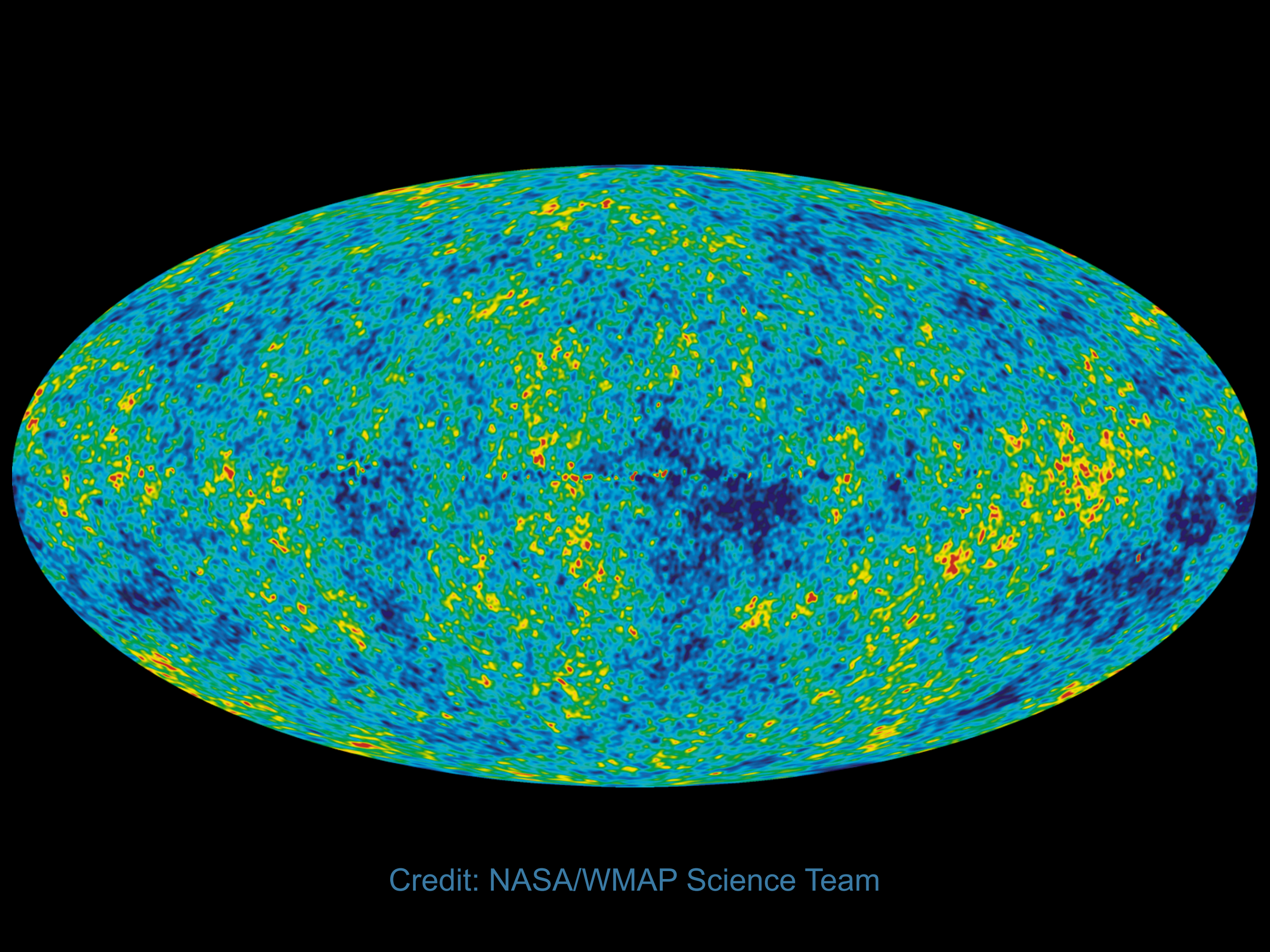
- \* Why Pursue Dark Energy?
- \* DE Equation of State (EOS)
- \* DE from SNe Ia ++
- \* Beware of Systematics
  - Two Population Model
  - Gravitational Lensing

And Then...

## CMB Bispectrum

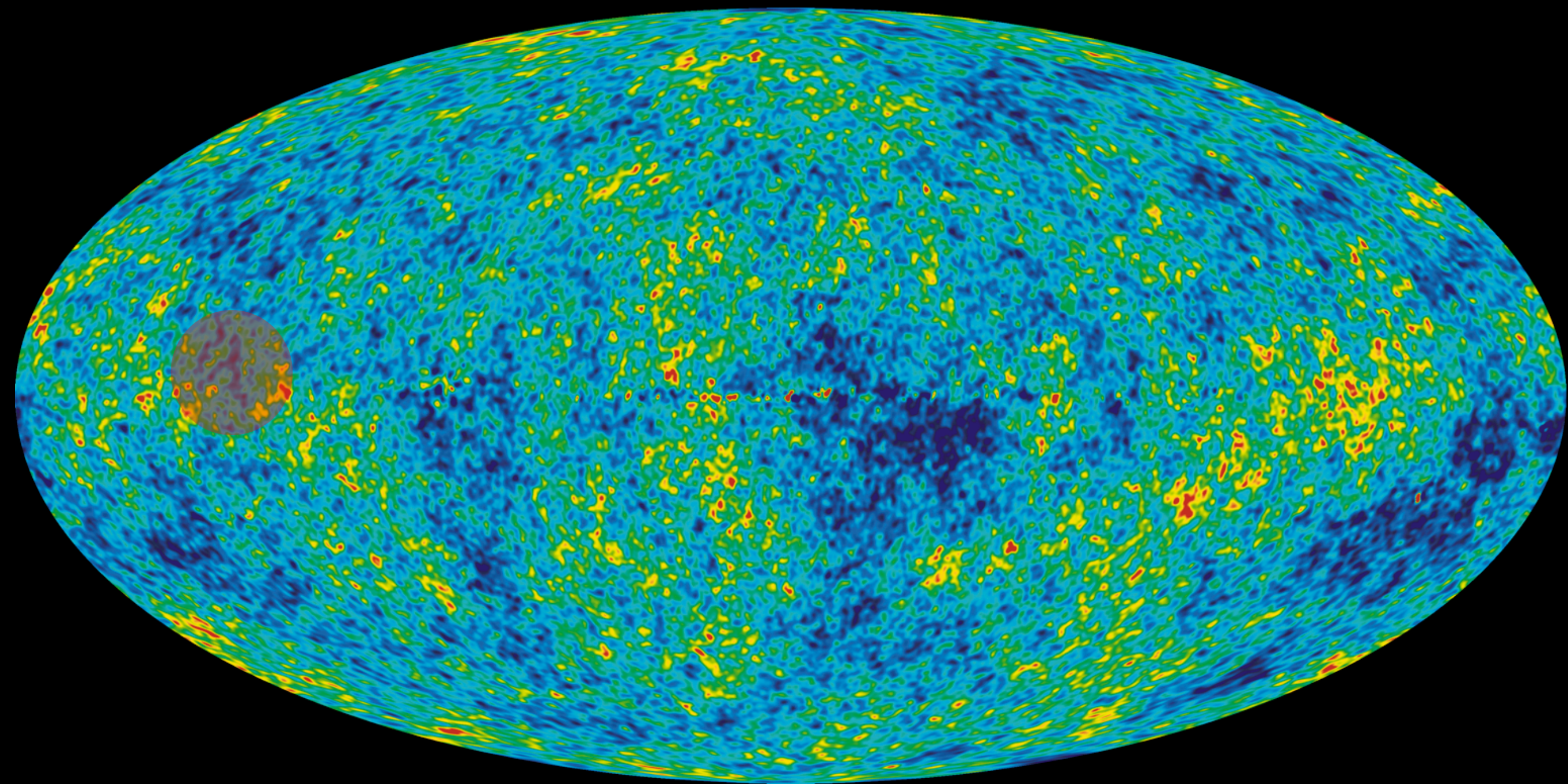
- \* Why Non-Gaussianity?
- \* Why in CMB Bispectrum?
- \* The  $f_{NL}$
- \* WL of CMB Bispectrum
  - ⊗ Analytical Sketch
  - ⊗ Numerical Results





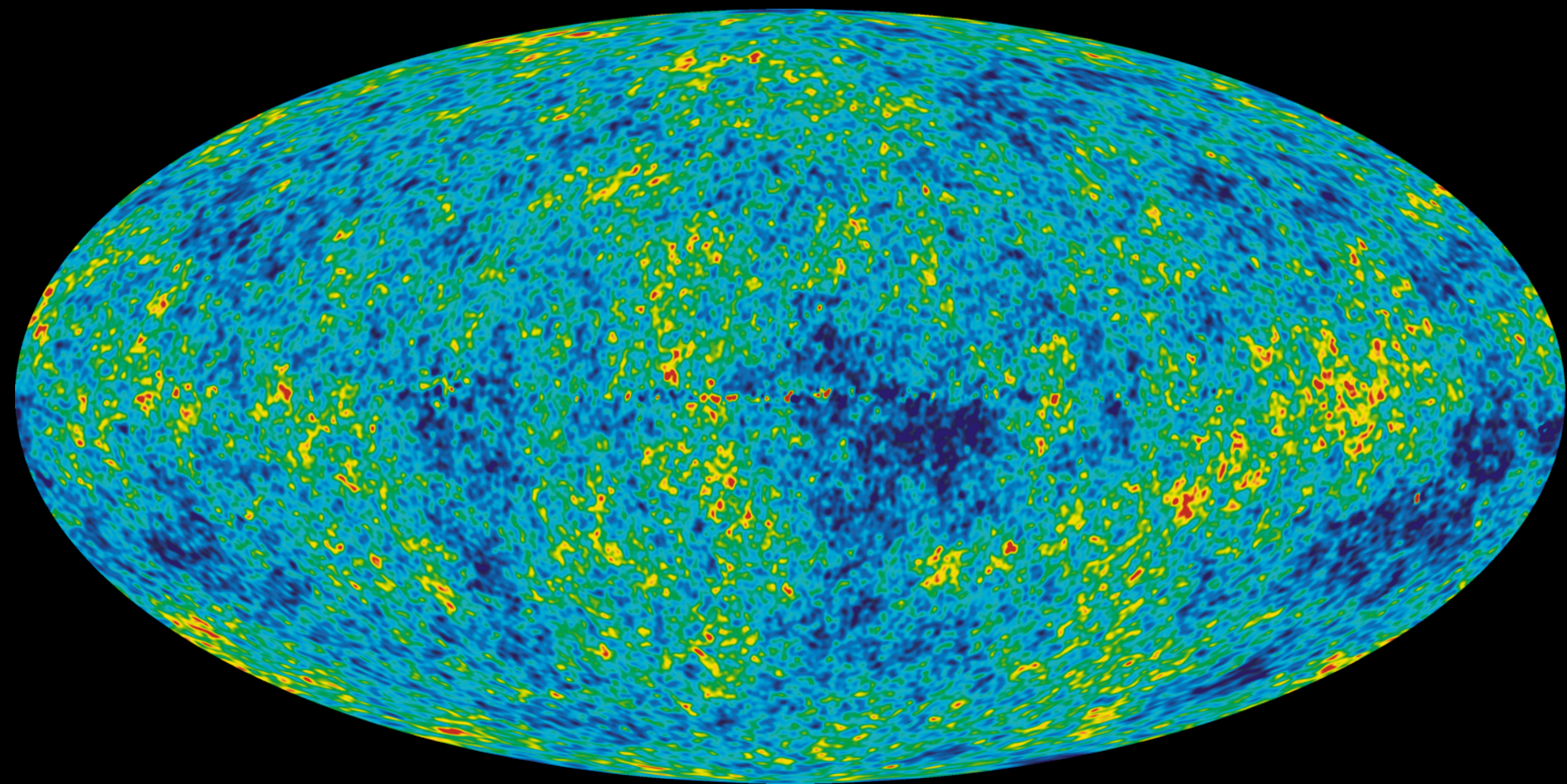
Credit: NASA/WMAP Science Team





Credit: NASA/WMAP Science Team





Credit: NASA/WMAP Science Team



## OBSERVATIONAL EVIDENCE FROM SUPERNOVAE FOR AN ACCELERATING UNIVERSE AND A COSMOLOGICAL CONSTANT

ADAM G. RIESS,<sup>1</sup> ALEXEI V. FILIPPENKO,<sup>1</sup> PETER CHALLIS,<sup>2</sup> ALEJANDRO CLOCCHIATTI,<sup>3</sup> ALAN DIERCKS,<sup>4</sup>  
PETER M. GARNAVICH,<sup>2</sup> RON L. GILLILAND,<sup>5</sup> CRAIG J. HOGAN,<sup>4</sup> SAURABH JHA,<sup>2</sup> ROBERT P. KIRSHNER,<sup>2</sup>  
B. LEIBUNDGUT,<sup>6</sup> M. M. PHILLIPS,<sup>7</sup> DAVID REISS,<sup>4</sup> BRIAN P. SCHMIDT,<sup>8,9</sup> ROBERT A. SCHOMMER,<sup>7</sup>  
R. CHRIS SMITH,<sup>7,10</sup> J. SPYROMILIO,<sup>6</sup> CHRISTOPHER STUBBS,<sup>4</sup>  
NICHOLAS B. SUNTZEFF,<sup>7</sup> AND JOHN TONRY<sup>11</sup>

*Received 1998 March 13; revised 1998 May 6*

Illustration: John Kascht





## MEASUREMENTS OF $\Omega$ AND $\Lambda$ FROM 42 HIGH-REDSHIFT SUPERNOVAE

S. PERLMUTTER,<sup>1</sup> G. ALDERING, G. GOLDBABER,<sup>1</sup> R. A. KNOP, P. NUGENT, P. G. CASTRO,<sup>2</sup> S. DEUSTUA, S. FABBRO,<sup>3</sup>  
A. GOOBAR,<sup>4</sup> D. E. GROOM, I. M. HOOK,<sup>5</sup> A. G. KIM,<sup>1,6</sup> M. Y. KIM, J. C. LEE,<sup>7</sup> N. J. NUNES,<sup>2</sup> R. PAIN,<sup>3</sup>  
C. R. PENNYPACKER,<sup>8</sup> AND R. QUIMBY

Institute for Nuclear and Particle Astrophysics, E. O. Lawrence Berkeley National Laboratory, Berkeley, CA 94720

C. LIDMAN

European Southern Observatory, La Silla, Chile

R. S. ELLIS, M. IRWIN, AND R. G. McMAHON

Institute of Astronomy, Cambridge, England, UK

P. RUIZ-LAPUENTE

Department of Astronomy, University of Barcelona, Barcelona, Spain

N. WALTON

Isaac Newton Group, La Palma, Spain

B. SCHAEFER

Department of Astronomy, Yale University, New Haven, CT

B. J. BOYLE

Anglo-Australian Observatory, Sydney, Australia

A. V. FILIPPENKO AND T. MATHESON

Department of Astronomy, University of California, Berkeley, CA

A. S. FRUCHTER AND N. PANAGIA<sup>9</sup>

Space Telescope Science Institute, Baltimore, MD

H. J. M. NEWBERG

Fermi National Laboratory, Batavia, IL

AND

W. J. COUCH

University of New South Wales, Sydney, Australia

(THE SUPERNOVA COSMOLOGY PROJECT)

*Received 1998 September 8; accepted 1998 December 17*



# TYPE Ia SUPERNOVA DISCOVERIES AT $z > 1$ FROM THE *HUBBLE SPACE TELESCOPE*: EVIDENCE FOR PAST DECELERATION AND CONSTRAINTS ON DARK ENERGY EVOLUTION<sup>1</sup>

ADAM G. RIESS,<sup>2</sup> LOUIS-GREGORY STROLGER,<sup>2</sup> JOHN TONRY,<sup>3</sup> STEFANO CASERTANO,<sup>2</sup> HENRY C. FERGUSON,<sup>2</sup> BAHRAM MOBASHER,<sup>2</sup>  
PETER CHALLIS,<sup>4</sup> ALEXEI V. FILIPPENKO,<sup>5</sup> SAURABH JHA,<sup>5</sup> WEIDONG LI,<sup>5</sup> RYAN CHORNOCK,<sup>5</sup> ROBERT P. KIRSHNER,<sup>4</sup>  
BRUNO LEIBUNDGUT,<sup>6</sup> MARK DICKINSON,<sup>2</sup> MARIO LIVIO,<sup>2</sup> MAURO GIAVALISCO,<sup>2</sup>  
CHARLES C. STEIDEL,<sup>7</sup> TXITXO BENÍTEZ,<sup>8</sup> AND ZLATAN TSVETANOV<sup>8</sup>

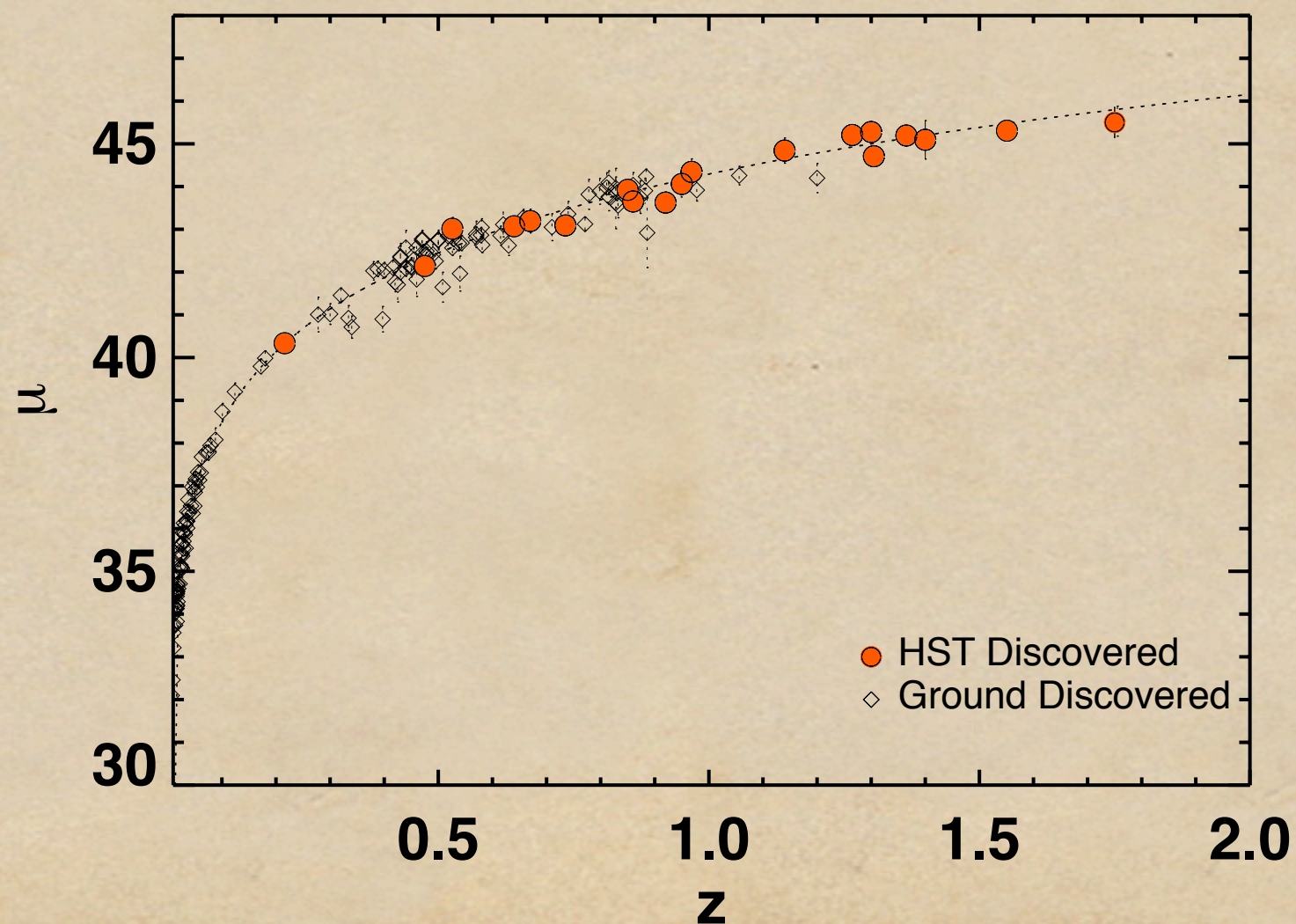
*Received 2004 January 20; accepted 2004 February 16*



# TYPE Ia SUPERNOVA DISCOVERIES AT $z > 1$ FROM THE *HUBBLE SPACE TELESCOPE*: EVIDENCE FOR PAST DECELERATION AND CONSTRAINTS ON DARK ENERGY EVOLUTION<sup>1</sup>

ADAM G. RIESS,<sup>2</sup> LOUIS-GREGORY STROLGER,<sup>2</sup> JOHN TONRY,<sup>3</sup> STEFANO CASERTANO,<sup>2</sup> HENRY C. FERGUSON,<sup>2</sup> BAHRAM MOBASHER,<sup>2</sup>  
 PETER CHALLIS,<sup>4</sup> ALEXEI V. FILIPPENKO,<sup>5</sup> SAURABH JHA,<sup>5</sup> WEIDONG LI,<sup>5</sup> RYAN CHORNOCK,<sup>5</sup> ROBERT P. KIRSHNER,<sup>4</sup>  
 BRUNO LEIBUNDGUT,<sup>6</sup> MARK DICKINSON,<sup>2</sup> MARIO LIVIO,<sup>2</sup> MAURO GIAVALISCO,<sup>2</sup>  
 CHARLES C. STEIDEL,<sup>7</sup> TXITXO BENÍTEZ,<sup>8</sup> AND ZLATAN TSVETANOV<sup>8</sup>

*Received 2004 January 20; accepted 2004 February 16*

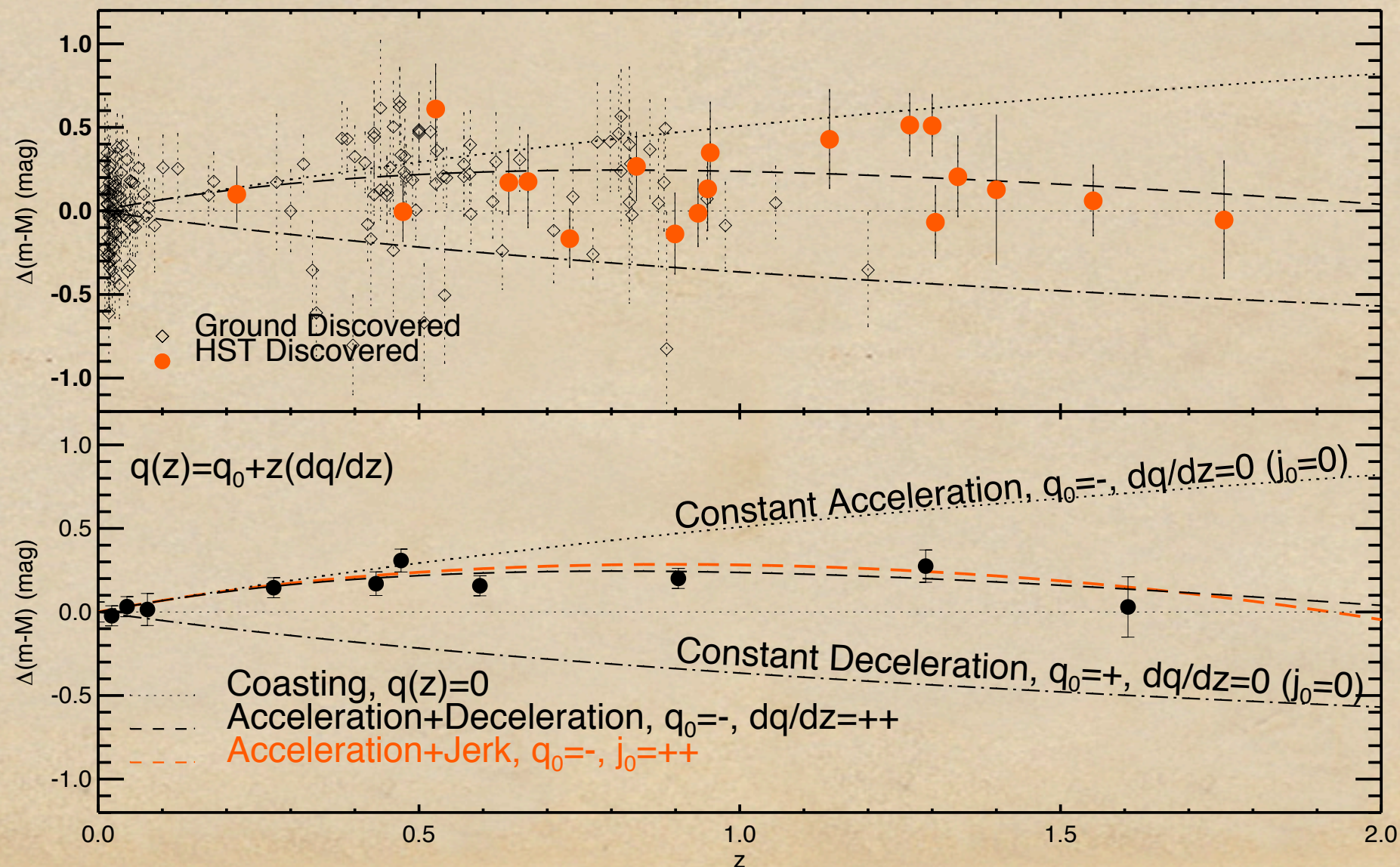




# TYPE Ia SUPERNOVA DISCOVERIES AT $z > 1$ FROM THE *HUBBLE SPACE TELESCOPE*: EVIDENCE FOR PAST DECELERATION AND CONSTRAINTS ON DARK ENERGY EVOLUTION<sup>1</sup>

ADAM G. RIESS,<sup>2</sup> LOUIS-GREGORY STOLGER,<sup>2</sup> JOHN TONRY,<sup>3</sup> STEFANO CASERTANO,<sup>2</sup> HENRY C. FERGUSON,<sup>2</sup> BAHRAM MOBASHER,<sup>2</sup>  
 PETER CHALLIS,<sup>4</sup> ALEXEI V. FILIPPENKO,<sup>5</sup> SAURABH JHA,<sup>5</sup> WEIDONG LI,<sup>5</sup> RYAN CHORNOCK,<sup>5</sup> ROBERT P. KIRSHNER,<sup>4</sup>  
 BRUNO LEIBUNDGUT,<sup>6</sup> MARK DICKINSON,<sup>2</sup> MARIO LIVIO,<sup>2</sup> MAURO GIAVALISCO,<sup>2</sup>  
 CHARLES C. STEIDEL,<sup>7</sup> TXITXO BENÍTEZ,<sup>8</sup> AND ZLATAN TSVETANOV<sup>8</sup>

Received 2004 January 20; accepted 2004 February 16





# Cosmic Acceleration

Modified Gravity

Dark Energy

$$H^2 - \frac{H}{r_c} = \frac{8\pi G}{3} (\rho + \rho_V)$$

Modification of Friedmann  
equation (5D Gravity)

Vacuum Energy  
(Cosmological Constant)

Phenomenological  
modification to the GR  
Lagrangian

Scalar Fields  
Evolving Equation of State

New Physics/Surprises?



# Where Do We Stand? After...

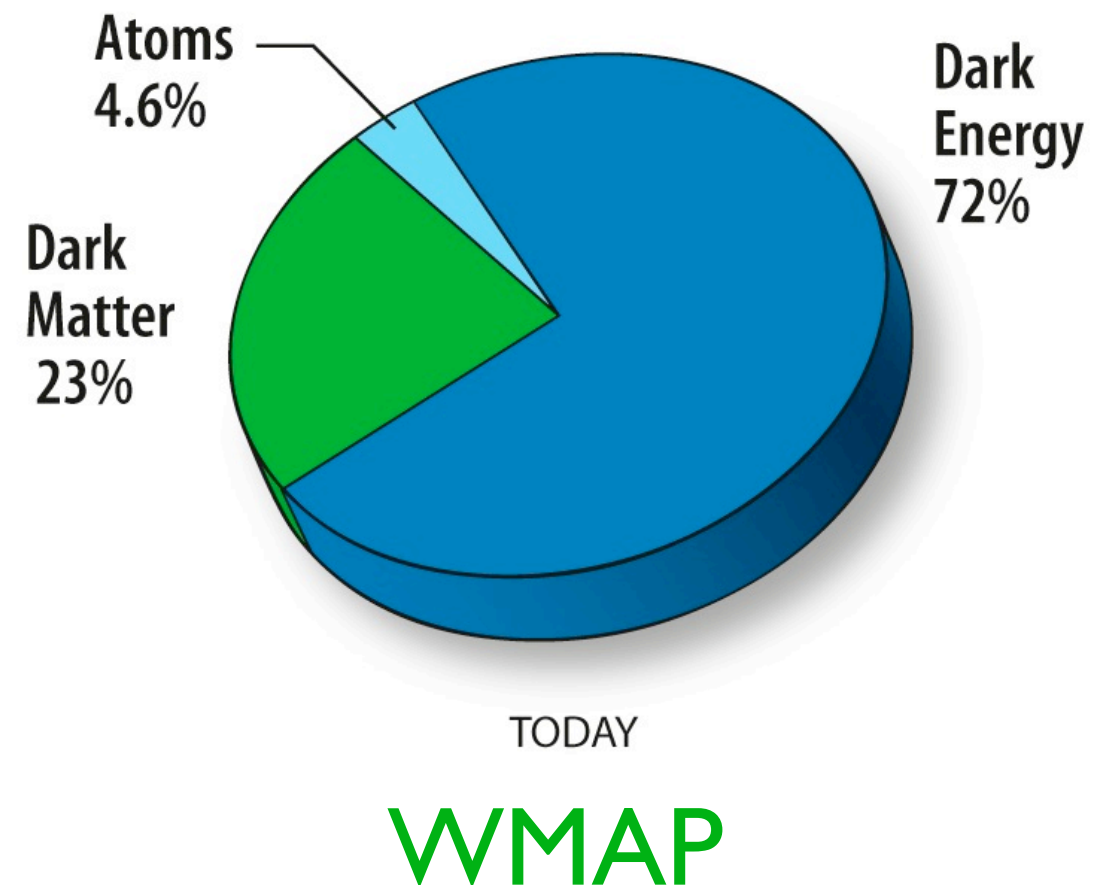
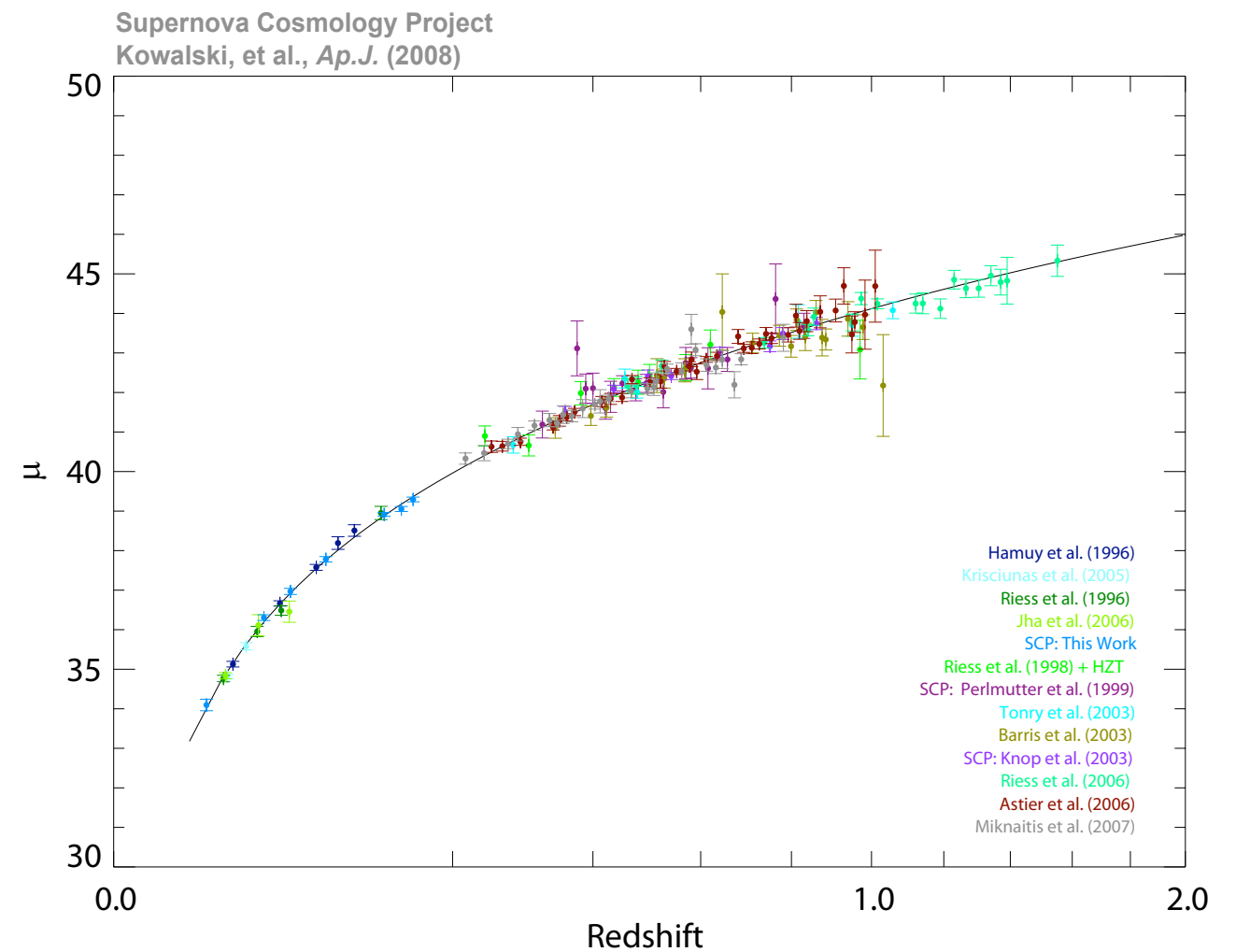
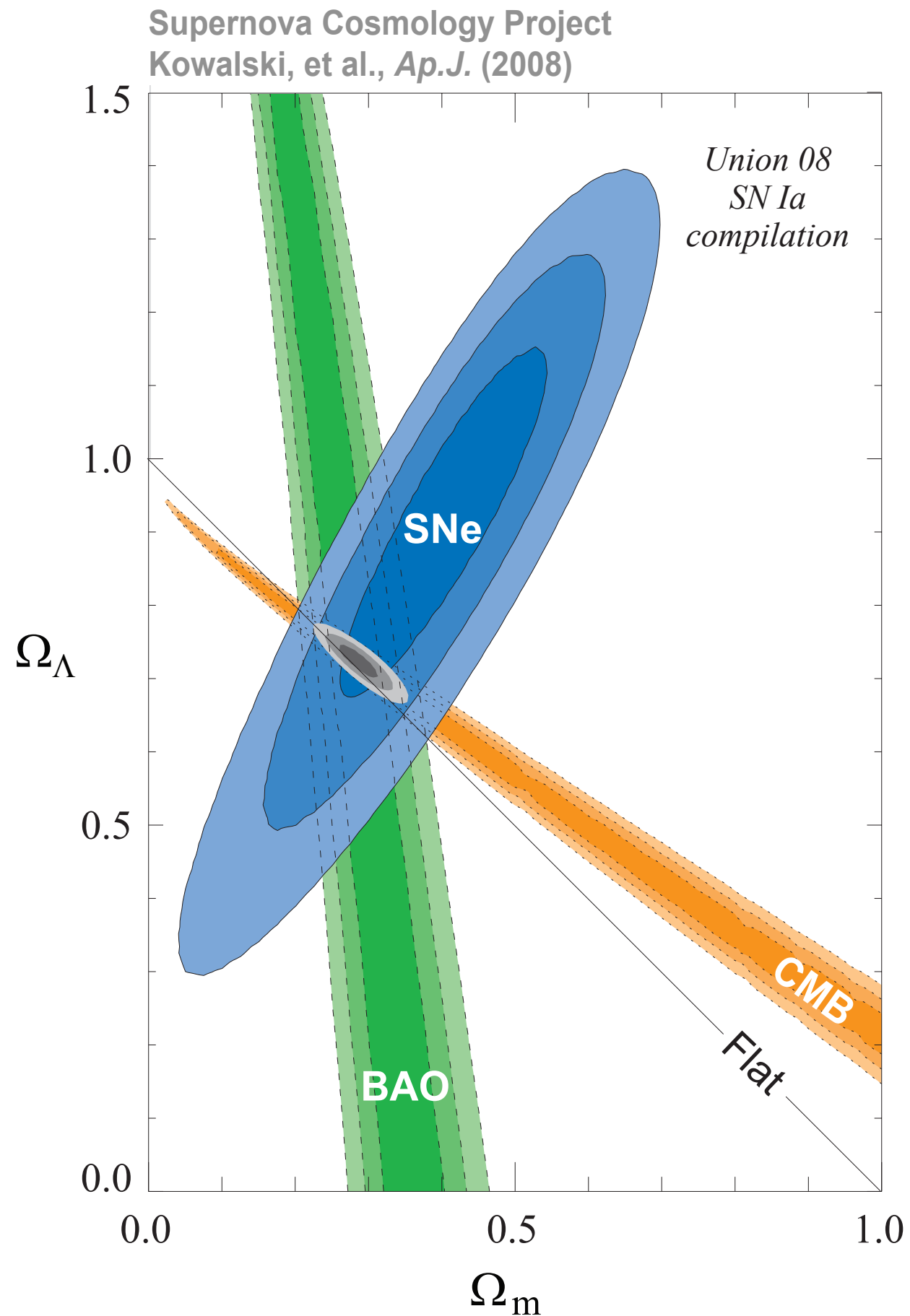
A DECADE OF  
**DARK ENERGY**

MAY 5-8, 2008

Space Telescope Science Institute, Baltimore, MD

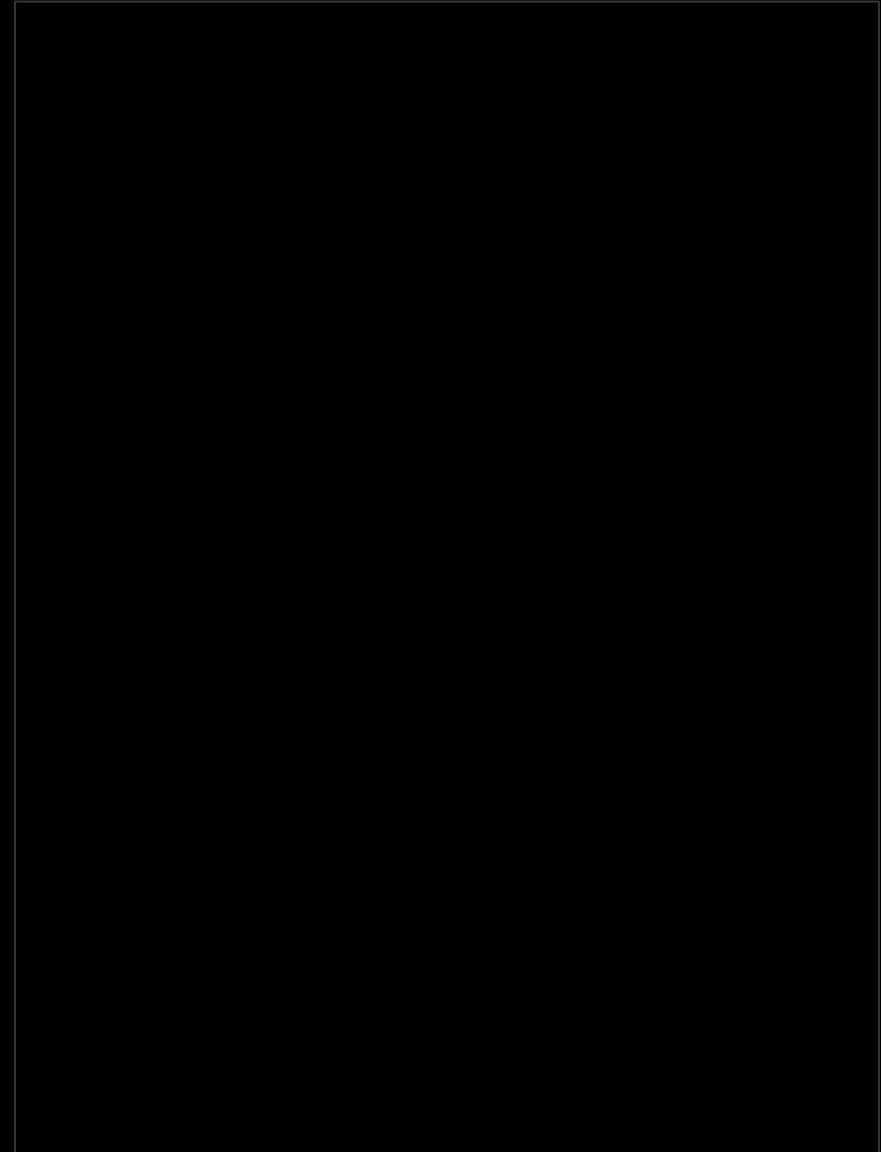


$$\Omega_{\Lambda} = 0.713^{+0.027}_{-0.029}(\text{stat})^{+0.036}_{-0.039}(\text{sys})$$





# What is Dark Energy?





# What is Dark Energy?

“Dark Energy is made from an exclusive blend of vital L-amino acids, beneficial vitamins and bionutrients that allows faster and greater ion penetration of the cell walls, visibly enhancing the rate of growth”

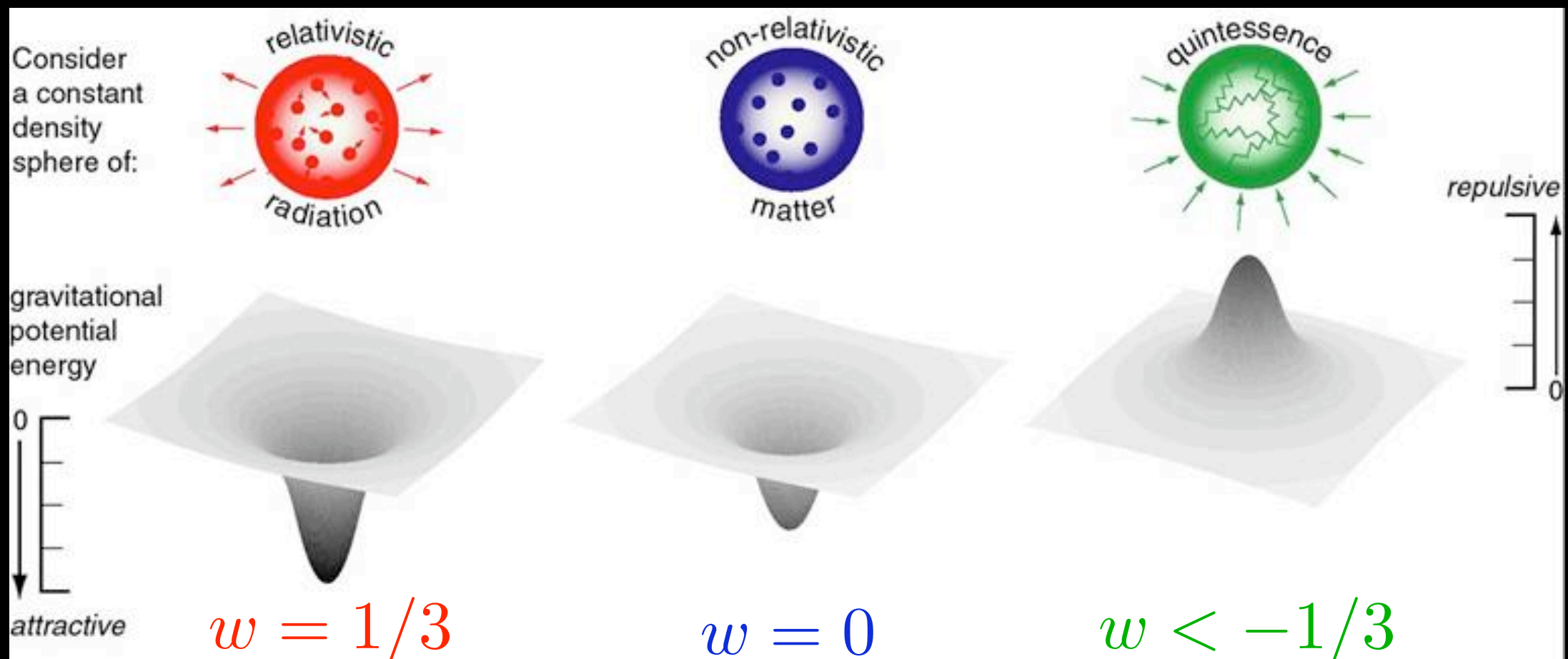


[GrowLightSource.com](http://GrowLightSource.com)



# Dark Energy Equation Of State

$$T_{\mu}^{\nu} = \text{diag}(\rho, -p, -p, -p) \quad p = w\rho$$



For Cosmological Constant...  $w = -1$



# “Seeing” The Dark Energy

...via its effect on the expansion of the Universe

$$H(z) = H_0 \left[ \Omega_m (1+z)^3 + \Omega_k (1+z)^2 + (1 - \Omega_k - \Omega_m) F(z) \right]^{1/2}$$



# “Seeing” The Dark Energy

...via its effect on the expansion of the Universe

$$H(z) = H_0 \left[ \Omega_m (1+z)^3 + \Omega_k (1+z)^2 + (1 - \Omega_k - \Omega_m) F(z) \right]^{1/2}$$

$$F(z) = \exp \left( 3 \int_0^z dz' \frac{1 + w(z')}{1 + z'} \right)$$





# “Seeing” The Dark Energy

...via its effect on the expansion of the Universe

$$H(z) = H_0 \left[ \Omega_m (1+z)^3 + \Omega_k (1+z)^2 + (1 - \Omega_k - \Omega_m) F(z) \right]^{1/2}$$

$$F(z) = \exp \left( 3 \int_0^z dz' \frac{1+w(z')}{1+z'} \right)$$



Approaches...

🌀 Standard Candles: Luminosity Distance of SNe

🌀 Standard Rulers:

➤ Angular Diameter Distance via BAO

➤ Distance to the Last Scattering Surface

🌀 Weak Lensing Tomography



# DE EOS Revisited: Different Approaches...

(A) Parameterize  $w(z)$

[Adopted by the DETF]

$$w(a) = w_0 + (1 - a)w_a$$

*Chevallier & Polarski (2001)*  
*(Linder 2003)*



# DE EOS Revisited: Different Approaches...

(A) Parameterize  $w(z)$

[Adopted by the DETF]

$$w(z) = w_0 + w_a z / (1 + z)$$

*Chevallier & Polarski (2001)*  
*(Linder 2003)*



# DE EOS Revisited: Different Approaches...

(A) Parameterize  $w(z)$

[Adopted by the DETF]

$$w(z) = w_0 + w_a z / (1 + z)$$

*Chevallier & Polarski (2001)*  
*(Linder 2003)*

(B) Non-Parametric  $w(z)$

- ✓ Unbiased Estimate of DE Density (Wang & Lovelace 2001)
- ✓ Principal Component Approach (Huterer & Starkman 2003)
- ✓ Uncorrelated Estimates (Huterer & Cooray 2005)

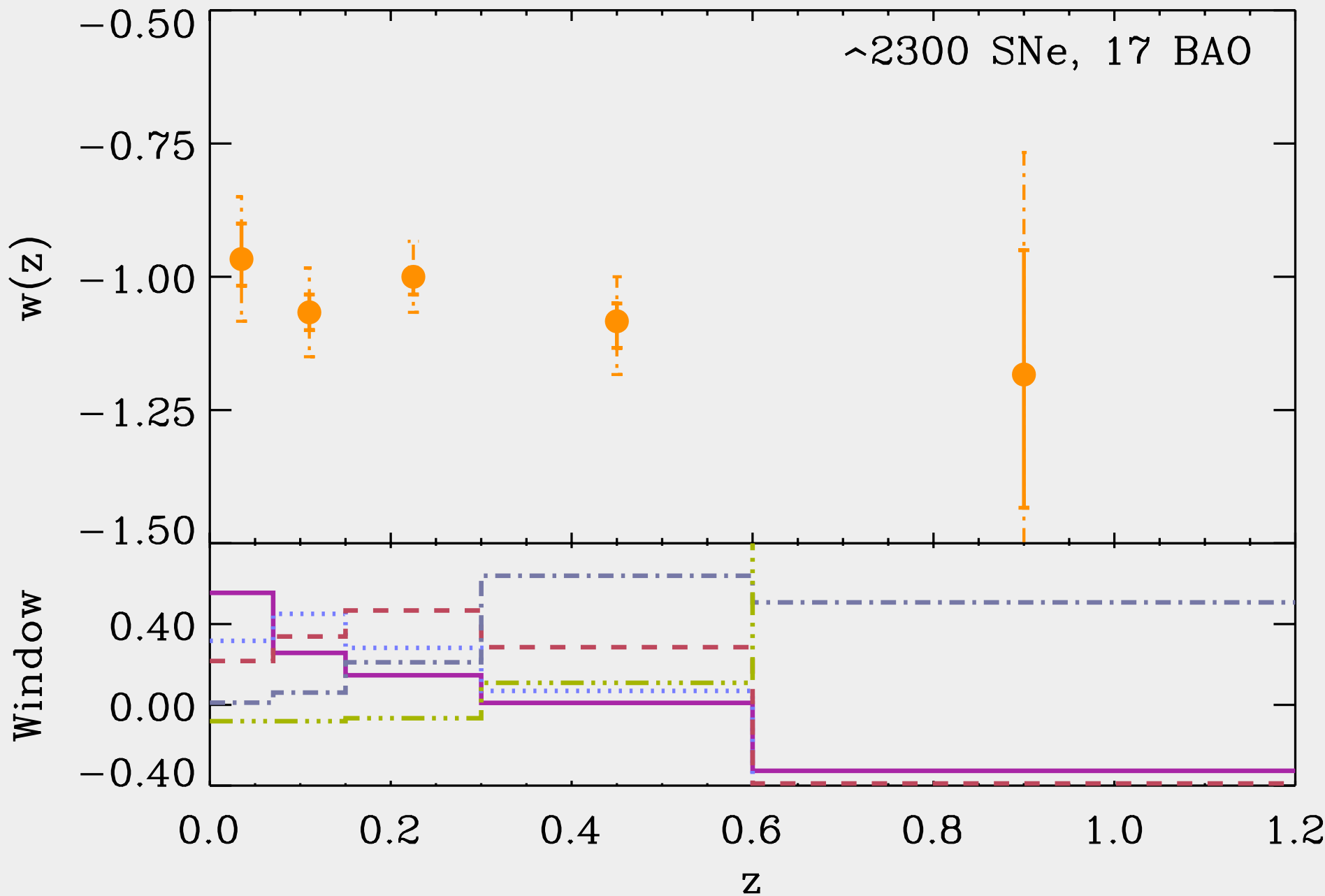
✓ ...

For a review: Please see Sahni and Starobinsky (2006) [arXiv:astro-ph/0610026]



# Binned Estimates: Future

$$F(z_n > z > z_{n-1}) = (1+z)^{3(1+w_n)} \prod_{i=0}^{n-1} (1+z_i)^{3(w_i-w_{i+1})}$$

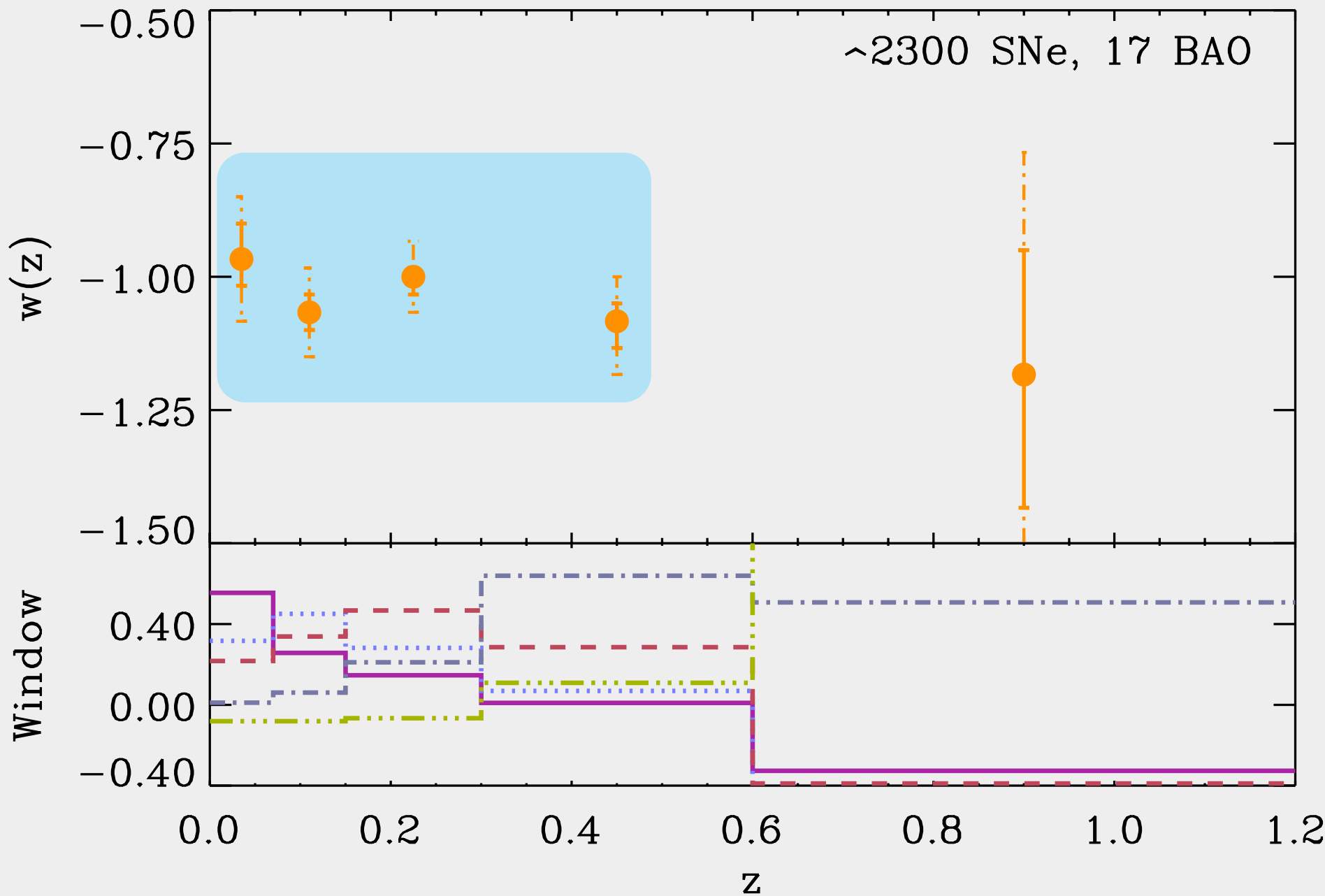


$w_1$	0-.07
$w_2$	.07-.15
$w_3$	0.15-.3
$w_4$	0.3-0.6
$w_5$	0.6-1.2
$w_6$	1.2-2.0



# Binned Estimates: Future

$$F(z_n > z > z_{n-1}) = (1+z)^{3(1+w_n)} \prod_{i=0}^{n-1} (1+z_i)^{3(w_i-w_{i+1})}$$



$w_1$	0-.07
$w_2$	.07-.15
$w_3$	0.15-.3
$w_4$	0.3-0.6
$w_5$	0.6-1.2
$w_6$	1.2-2.0



## center for cosmology, uc irvine

- ### wzBinned Code

## Other Resources

- 
- Figure 1 shows a plot of the weight function  $w(x)$  versus  $x$  for Case C. The plot displays a step function with four distinct colored segments: orange, cyan, green, and purple. The y-axis ranges from -1.5 to -0.5, and the x-axis ranges from 0 to 1. Above the plot, five data points with error bars are shown, labeled with 'x' and 'y' coordinates.



# Outline

## Dark Energy

- \* Why Pursue Dark Energy?
- \* DE Equation of State (EOS)
- \* DE from SNe Ia ++
- \* Beware of Systematics
  - Two Population Model
  - Gravitational Lensing

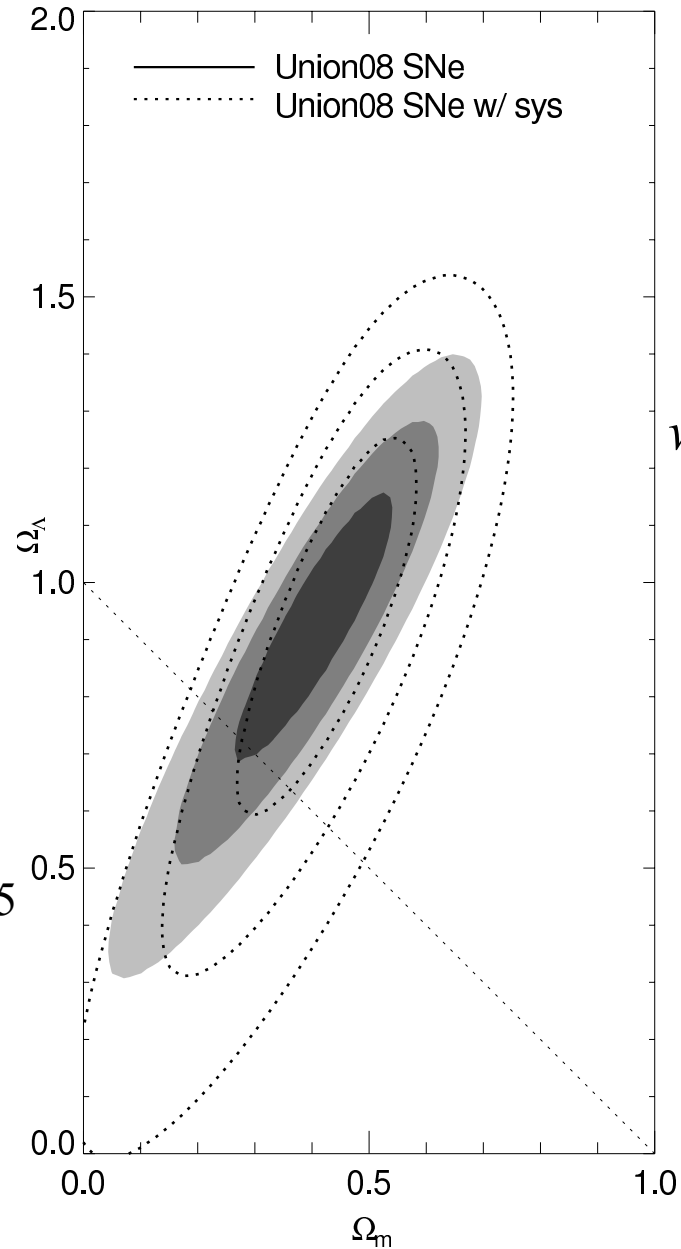
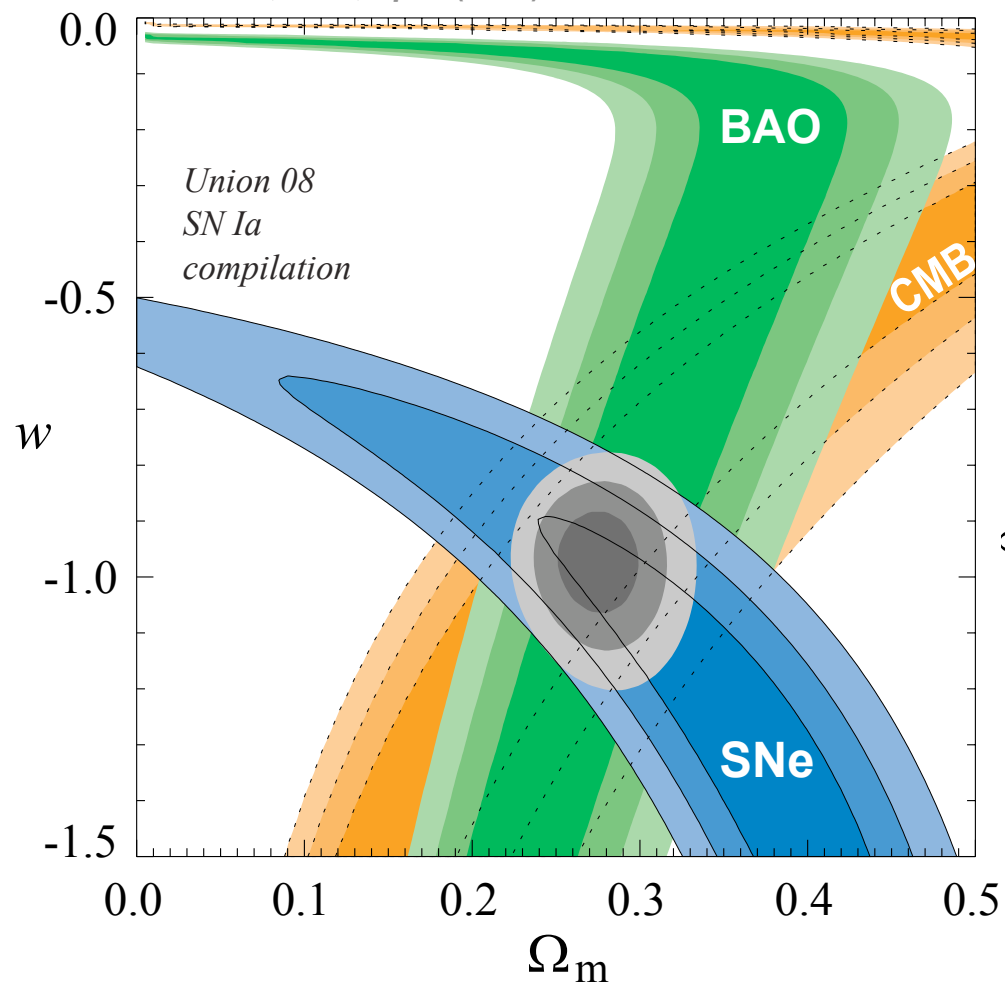
## CMB Bispectrum

- \* Why Non-Gaussianity?
- \* Why in CMB Bispectrum?
- \* The  $f_{\text{NL}}$
- \* WL of CMB Bispectrum
  - ⊗ Analytical Sketch
  - ⊗ Numerical Results

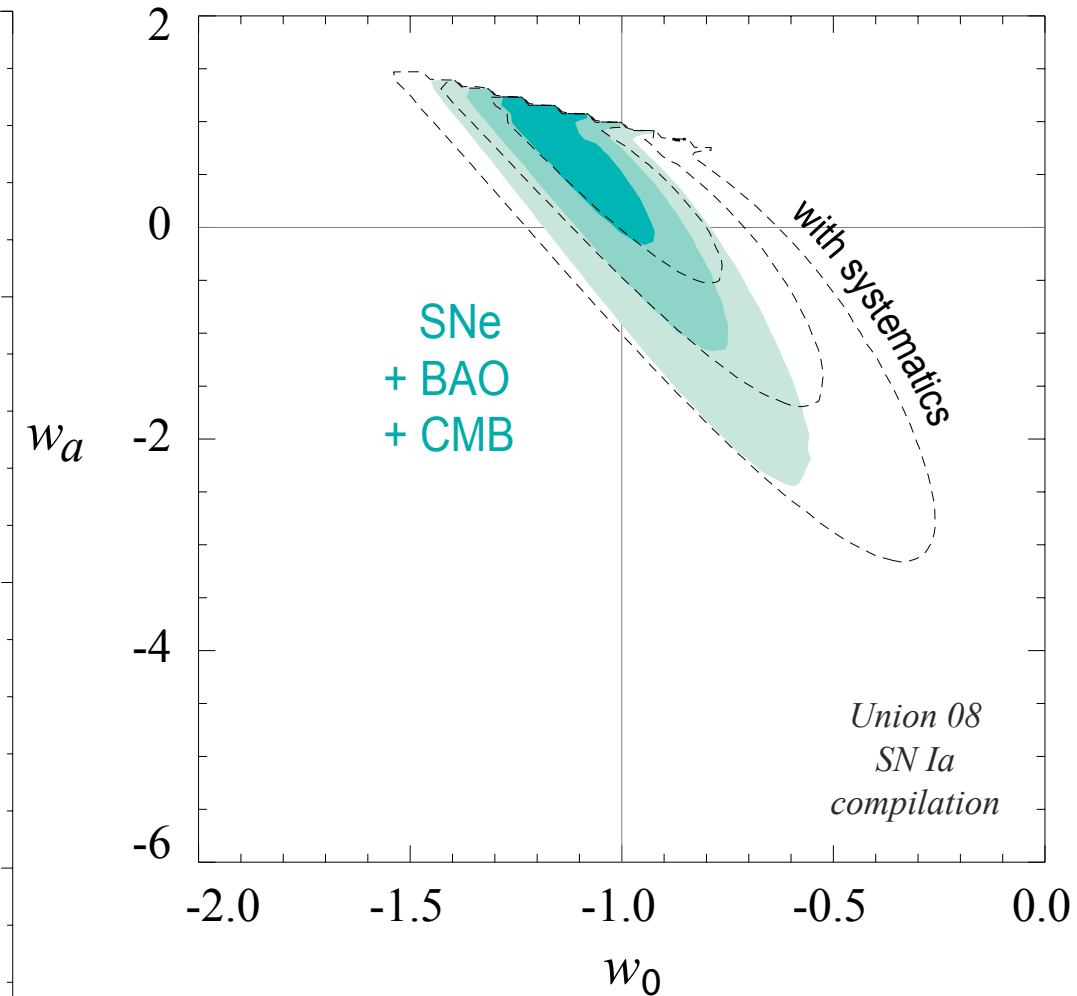


# Systematic Matters!

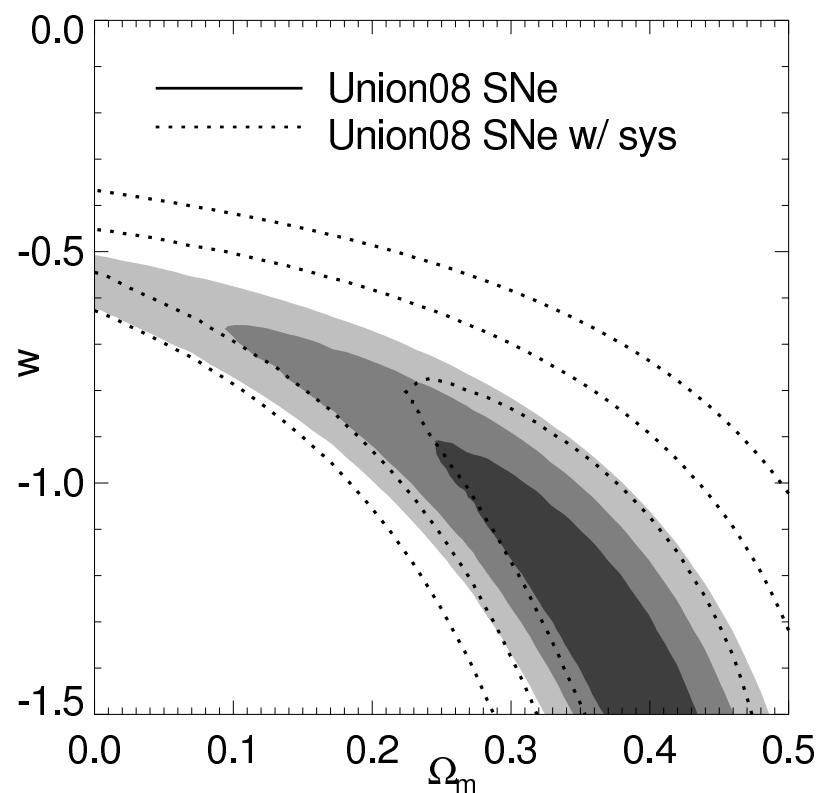
Supernova Cosmology Project  
Kowalski, et al., *Ap.J.* (2008)



Supernova Cosmology Project  
Kowalski, et al., *Ap.J.* (2008)



Kowalski et al. (2008)



$$\Omega_\Lambda = 0.713^{+0.027}_{-0.029}(\text{stat})^{+0.036}_{-0.039}(\text{sys})$$

$$w = -0.969^{+0.059}_{-0.063}(\text{stat})^{+0.063}_{-0.066}(\text{sys})$$

# Outline

## Dark Energy

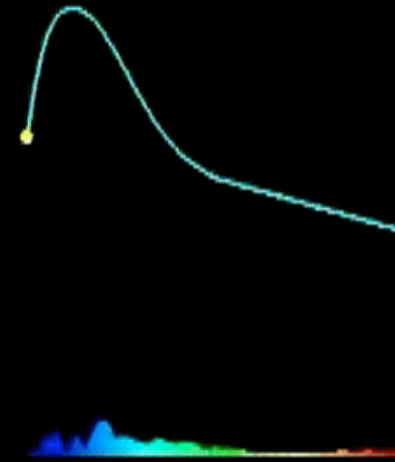
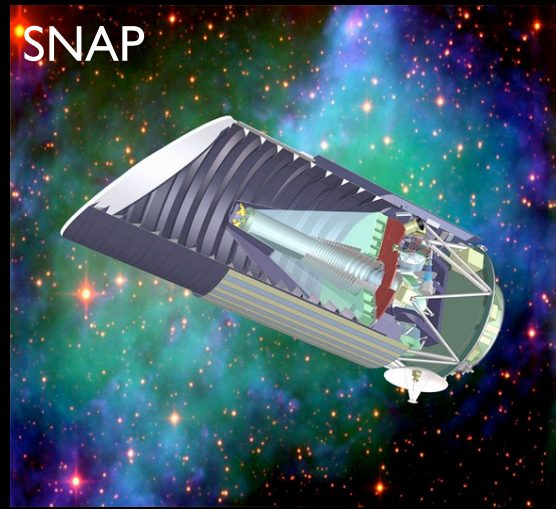
- \* Why Pursue Dark Energy?
- \* DE Equation of State (EOS)
- \* DE from SNe Ia ++
- \* Beware of Systematics
  - Two Population Model
  - Gravitational Lensing

## CMB Bispectrum

- \* Why Non-Gaussianity?
- \* Why in CMB Bispectrum?
- \* The  $f_{\text{NL}}$
- \* WL of CMB Bispectrum
  - ⊗ Analytical Sketch
  - ⊗ Numerical Results

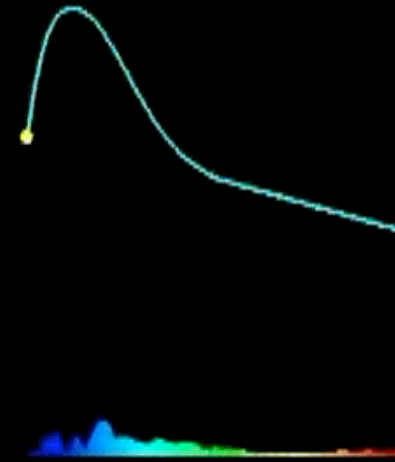
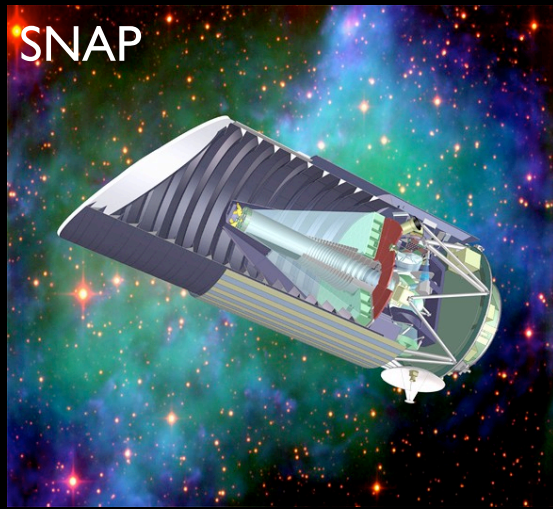


# Cosmology with SNe Ia: Revisited



Credit: This clip was prepared by the [Supernova Cosmology Project](#) (P. Nugent: spectral sequence; A. Conley: image sequence) with the help of Lawrence Berkeley National Laboratory's Computer Visualization Laboratory (N. Johnston: animation) at the National Energy Research Scientific Computing Center.

# Cosmology with SNe Ia: Revisited

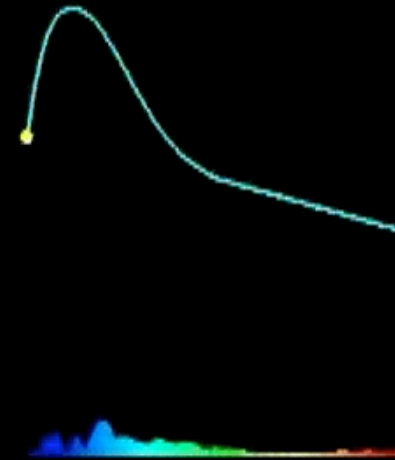
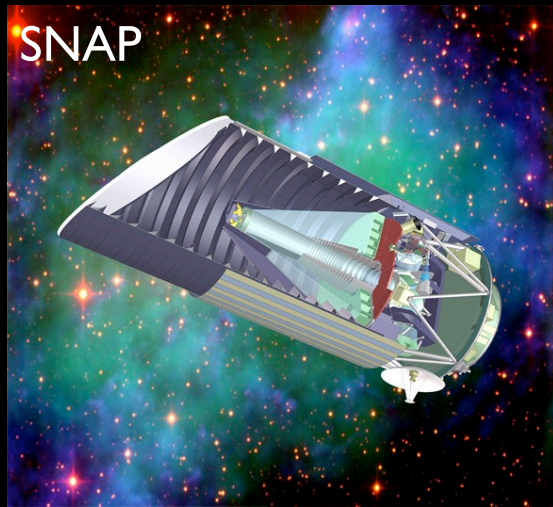


## Advantages

- ✓ Direct measure of accl.
- ✓ Small dispersion
- ✓ Single objects (easier!)
- ✓ Can be observed over wide  $z$
- ✓ Not cosmic variance limited
- ✓ Straightforward tests of sys.



# Cosmology with SNe Ia: Revisited



## Advantages

- ✓ Direct measure of accl.
- ✓ Small dispersion
- ✓ Single objects (easier!)
- ✓ Can be observed over wide  $z$
- ✓ Not cosmic variance limited
- ✓ Straightforward tests of sys.

## Challenges

- 📌 Dust extinction
- 📌 Photometric calibration (Vega)
- 📌 Malmquist bias
- 📌 K-corrections
- 📌 Evolution, chemical comp.
- 📌 Population bias + Grav. Lensing

# Challenges: Systematic Uncertainties

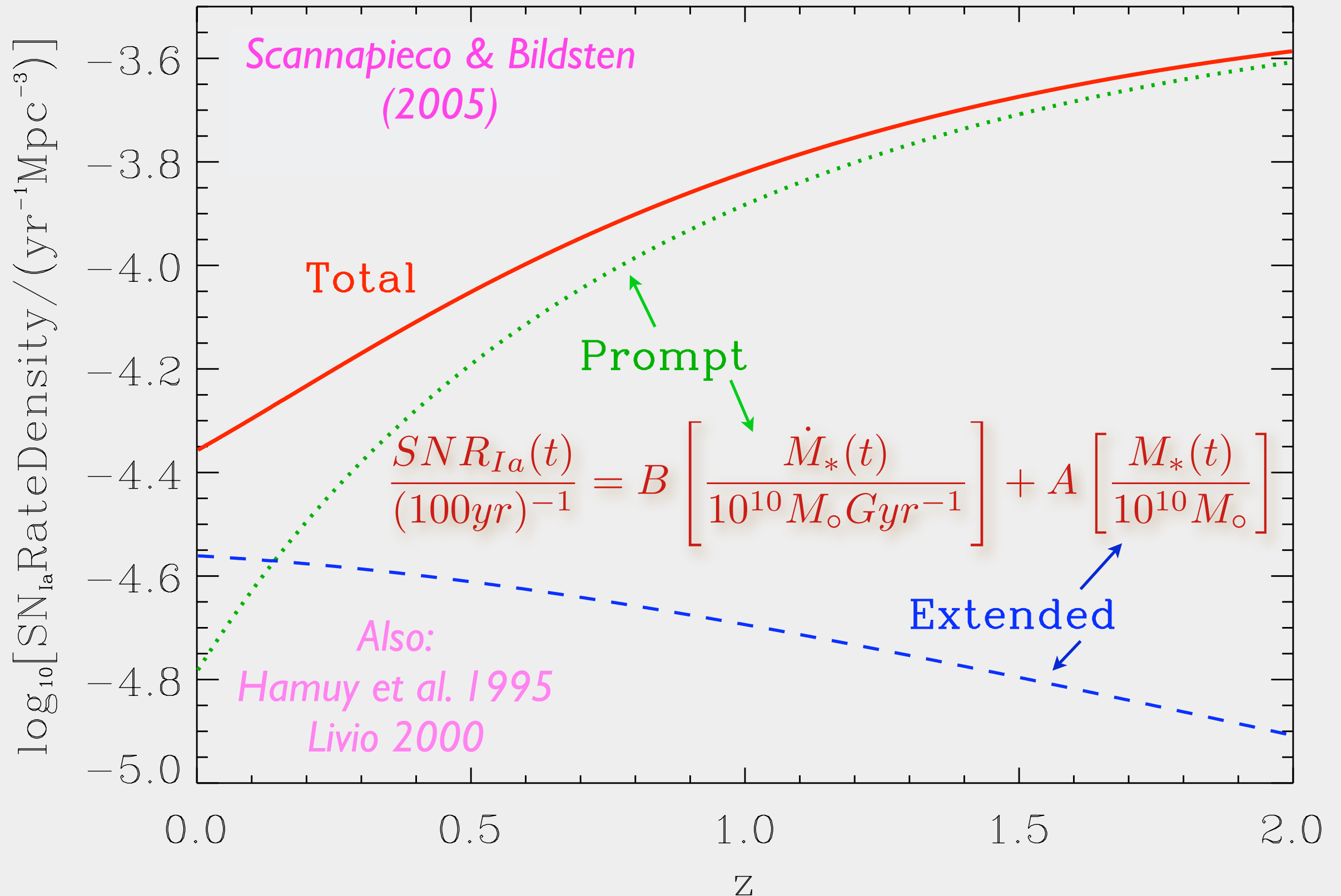
source of uncertainty	common (mag)	sample-dep.(mag)	treatment
Extinction	0.013	-	Multi-band photometry including near-IR
Calibration	0.021	0.021	Calibration of standard stars (optical thru near-IR) to <1%
Malmquist	-	0.020	High S/N lightcurves & spectra; requirement of pre-rise data
Lightcurve	0.028	-	SN spectra with broad $\lambda$ , temporal coverage
Evolution	0.015	-	High-resolution spectroscopy

Kowalski et al. (2008), Carnegie Supernova Project: W. Freedman

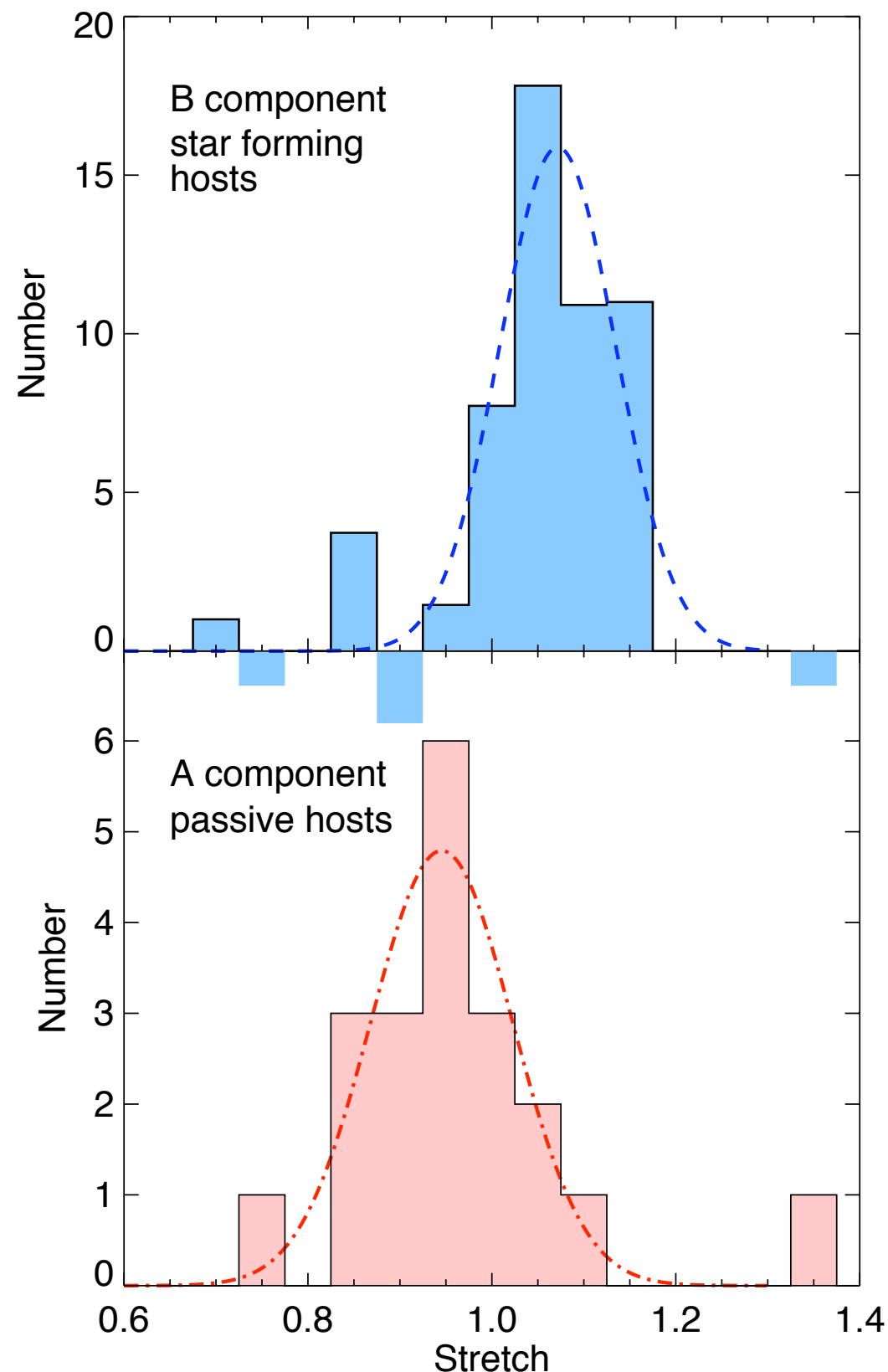
2-Population	
Lensing	



# Evolution based on Two SN Populations

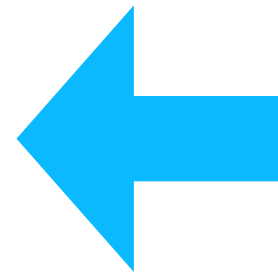


# Evolution based on Two SN Populations



$$\mu_B = m_B^* - M + \alpha(s - 1) - \beta c$$

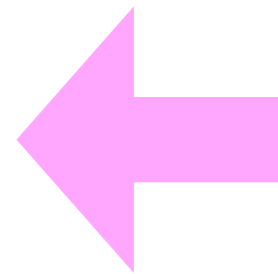
Tripp (1998), Guy et al. (2005)



PROMPT

12% Difference  
in  
Intrinsic Luminosity

$$\mathcal{L}_P = \mathcal{L}_E + \Delta\mathcal{L}$$



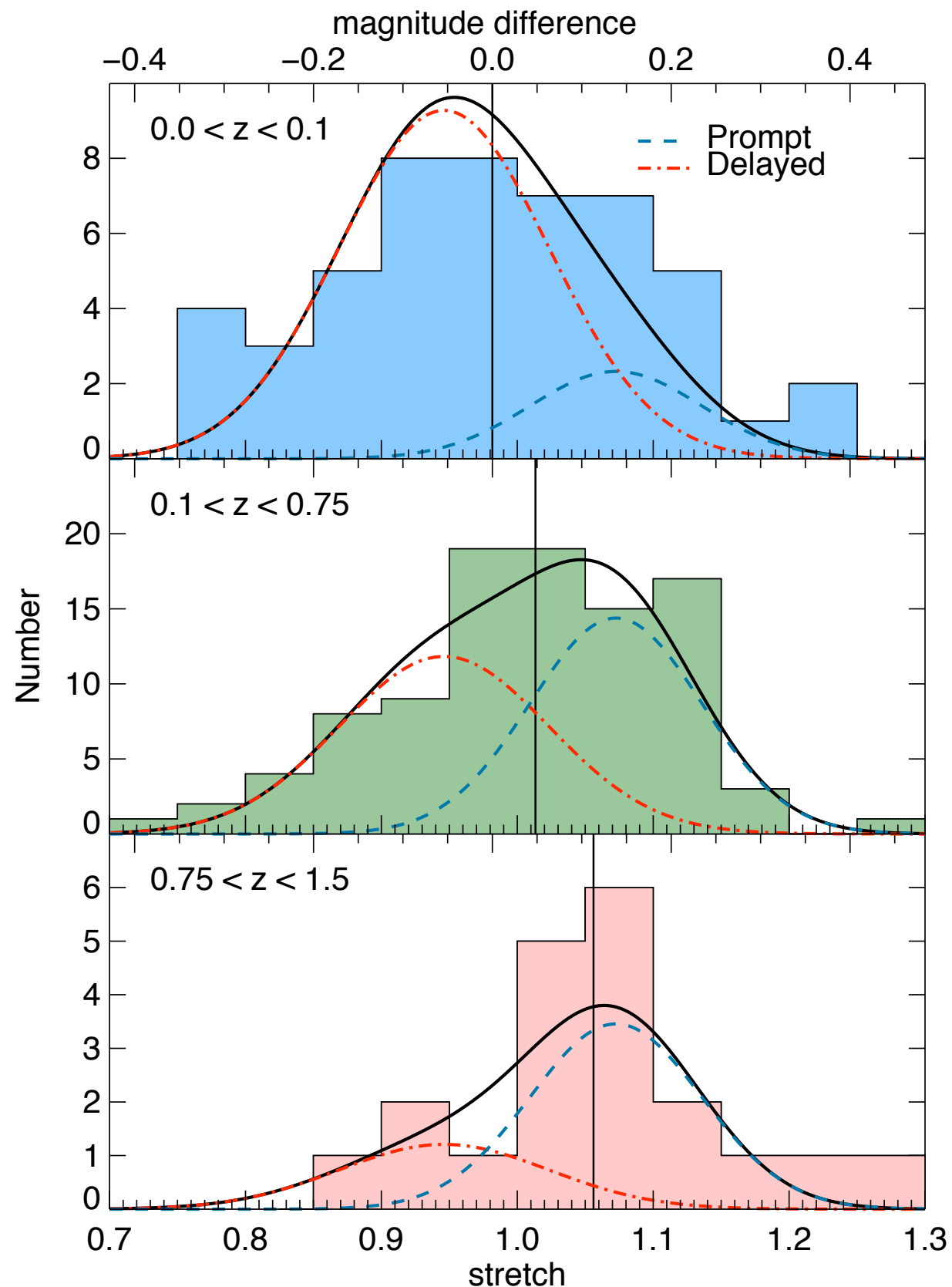
DELAYED

*Howell et al. 2007*

*Data Source: Sullivan et al. 2006 (SNLS)*



# Evolution based on Two SN Populations



Median Redshift: 0.026  
N=50

Median Redshift: 0.55  
N=99

Median Redshift: 1.12  
N=20

*Howell et al. 2007*

# Is there a Signature in the Hubble Diagram?

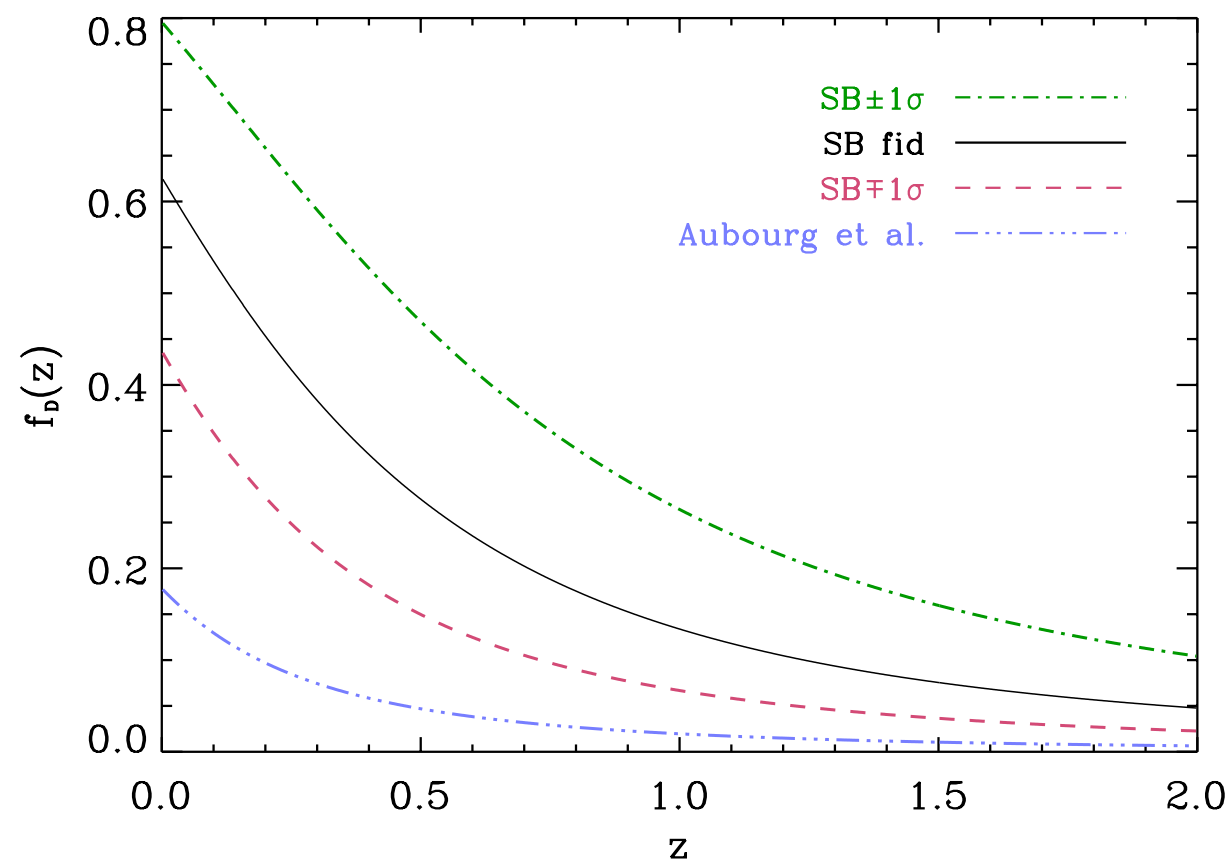


# Is there a Signature in the Hubble Diagram?

$$m - M = 5 \log \left( \frac{d_L}{\text{Mpc}} \right) + 25 + \mathcal{M}$$

# Is there a Signature in the Hubble Diagram?

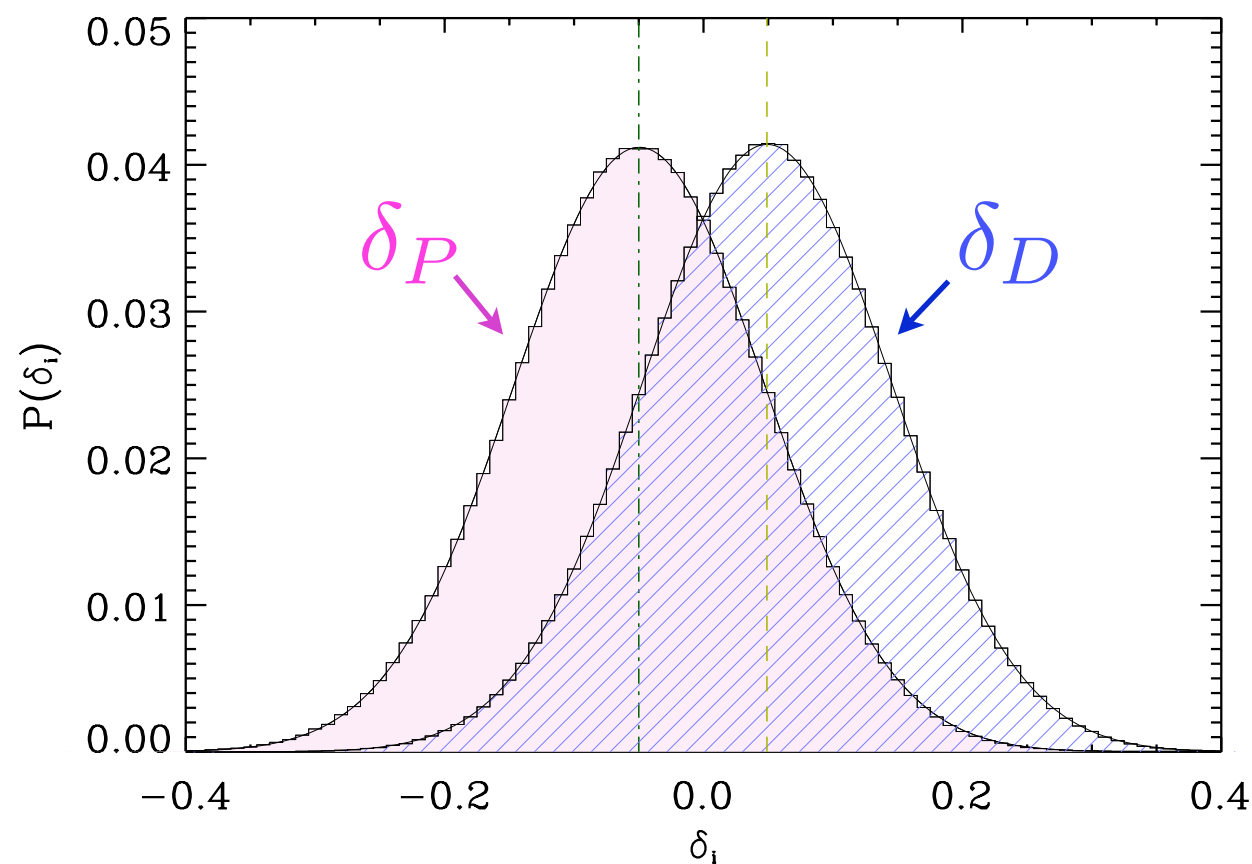
$$m - M = 5 \log \left( \frac{d_L}{\text{Mpc}} \right) + 25 + \mathcal{M} + \delta_D * f_D(z)$$





# Is there a Signature in the Hubble Diagram?

$$m - M = 5 \log \left( \frac{d_L}{\text{Mpc}} \right) + 25 + \mathcal{M} + \delta_D * f_D(z)$$



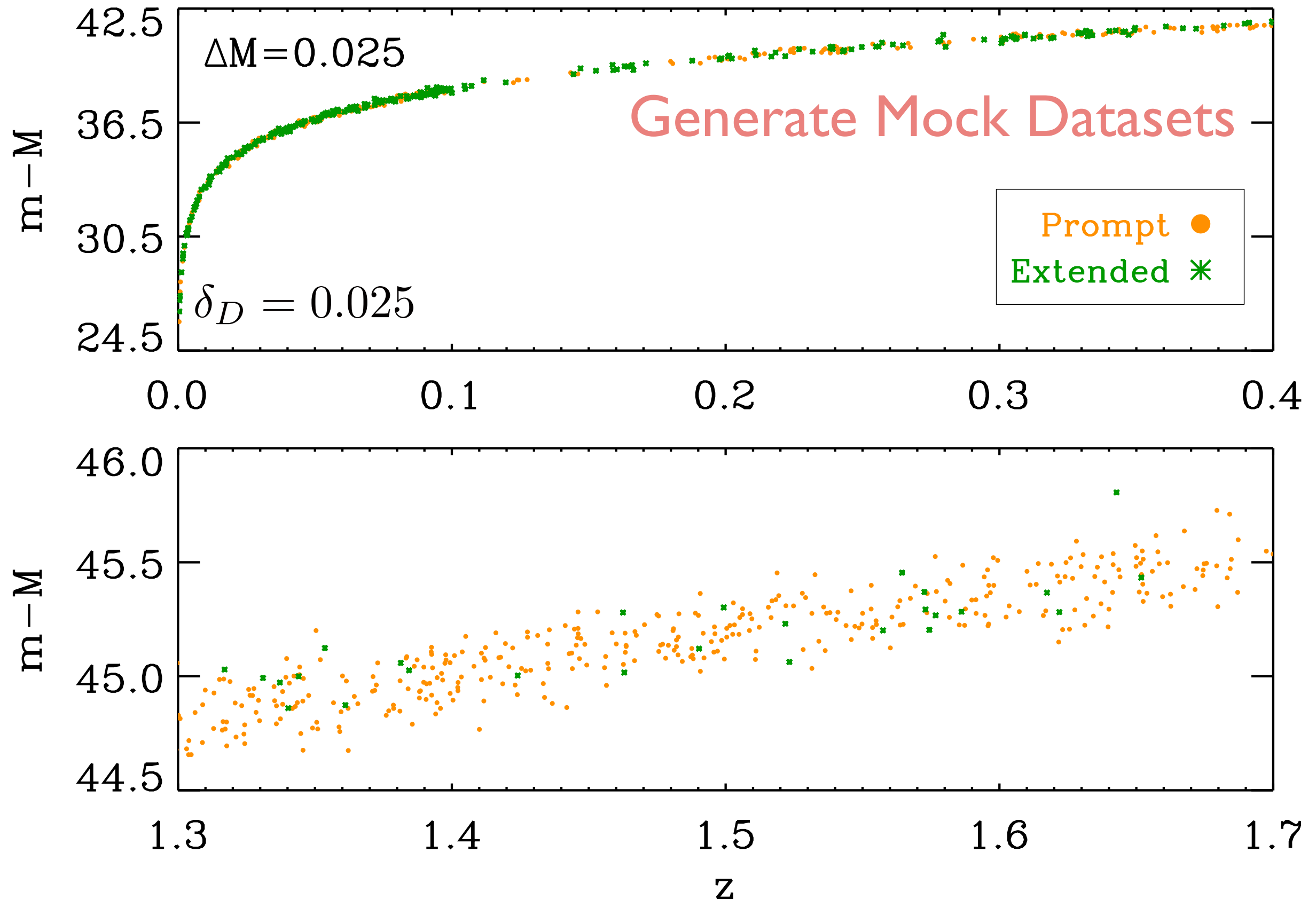
With current data (192 SNe from Davis et al. 2007), the residual is consistent with zero:

$$\delta_D \sim (5 \pm 9)\%$$

With future data, one will be able to constrain the residual much better.

*D.S., A. Amblard, A. Cooray, and D. Holz; ApJL, 684, L13 (2008)*

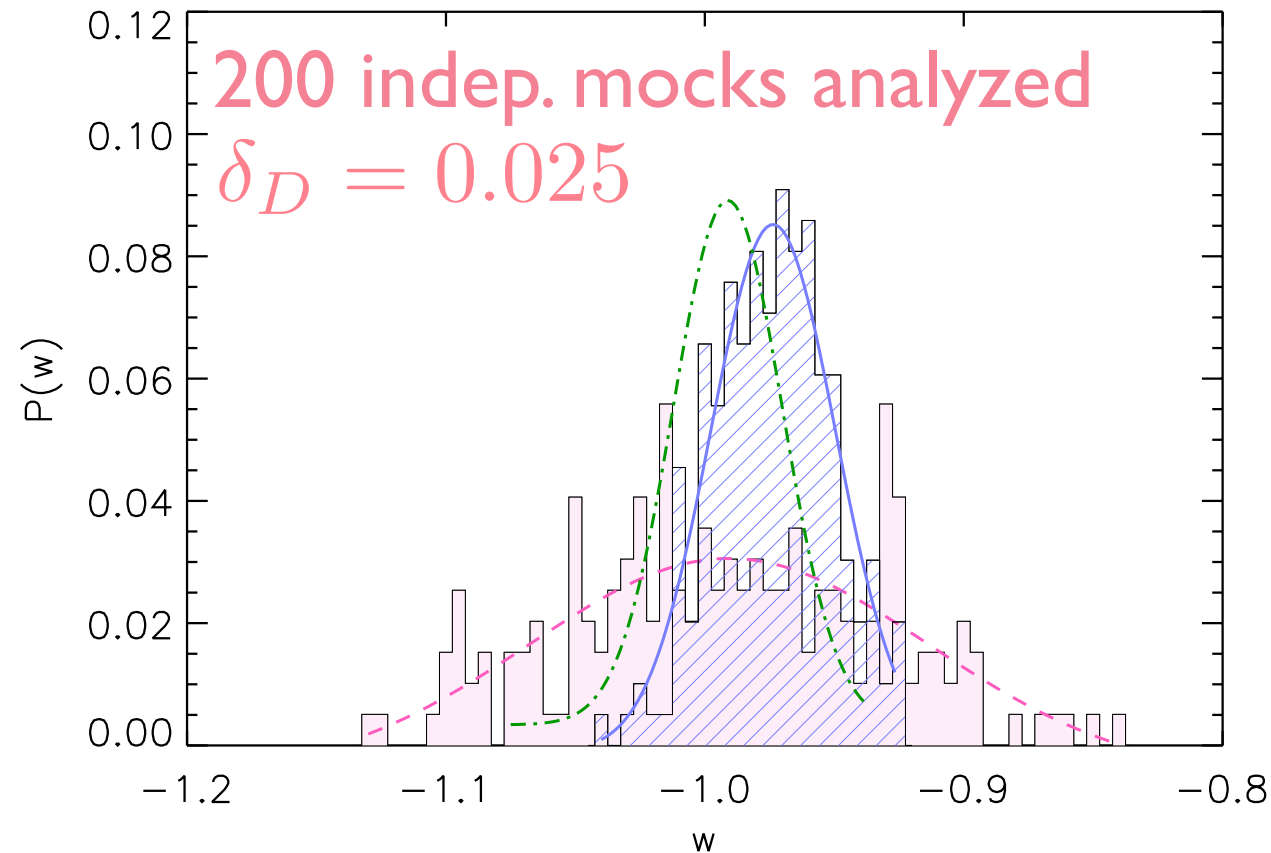
# Effect on the EOS Estimates: Bias in “w”



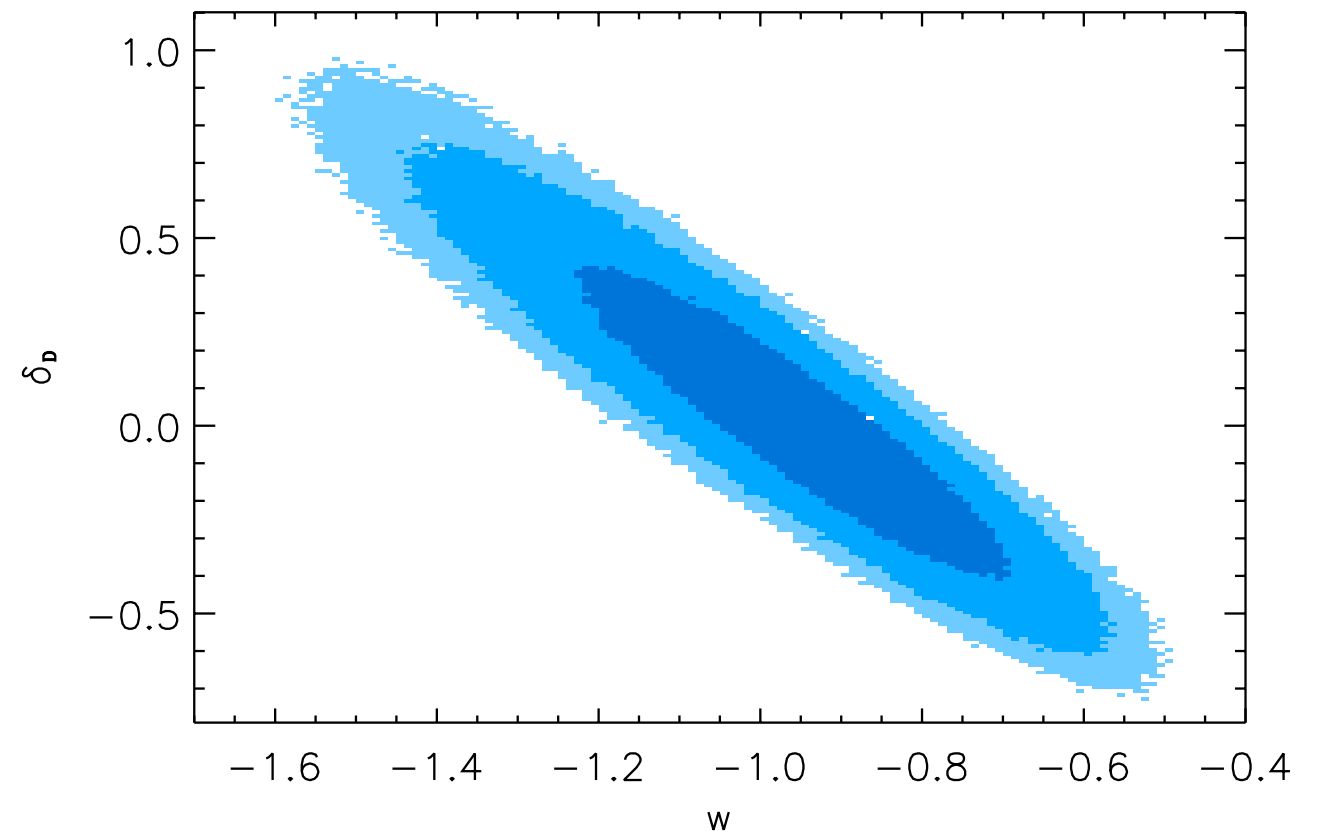
*D.S., A. Amblard, A. Cooray, and D. Holz; ApJL, 684, L13 (2008)*



# Effect on the EOS Estimates: Bias in “w”



~1-sigma bias in “w”



Correlation

While model-fitting the data:

$\delta_D = 0 \Rightarrow \sim 1\sigma$  bias in  $w$

$\delta_D = \text{FREE} \Rightarrow$  NO bias in  $w$ , BUT Error bar increased by 2.5 times

Best situation: Constrain  $\delta_D \leq 2\%$  with confidence

*D.S., A. Amblard, A. Cooray, and D. Holz; ApJL, 684, L13 (2008)*

# Challenges: Systematic Uncertainties

source of uncertainty	common (mag)	sample-dep.(mag)	treatment
Extinction	0.013	-	Multi-band photometry including near-IR
Calibration	0.021	0.021	Calibration of standard stars (optical thru near-IR) to <1%
Malmquist	-	0.020	High S/N lightcurves & spectra; requirement of pre-rise data
Lightcurve	0.028	-	SN spectra with broad $\lambda$ , temporal coverage
Evolution	0.015	-	High-resolution spectroscopy

Kowalski et al. (2008), Carnegie Supernova Project: W. Freedman

2-Population	Constrain the systematics to < 2% level to have the bias on “w” less than 1-sigma level without increasing error bar!
Lensing	

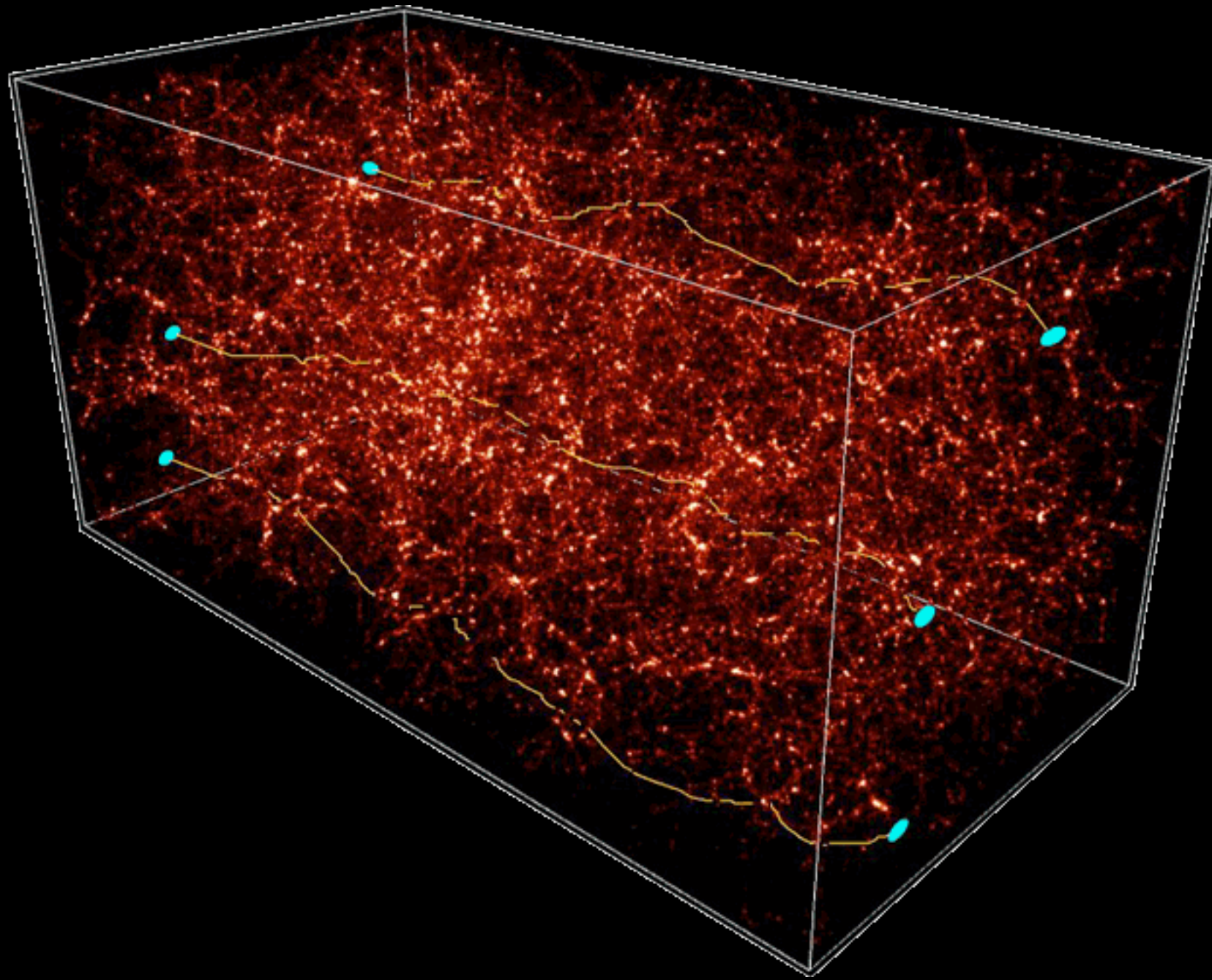


# Influence of Gravitational Lensing?

Lensing Galaxy

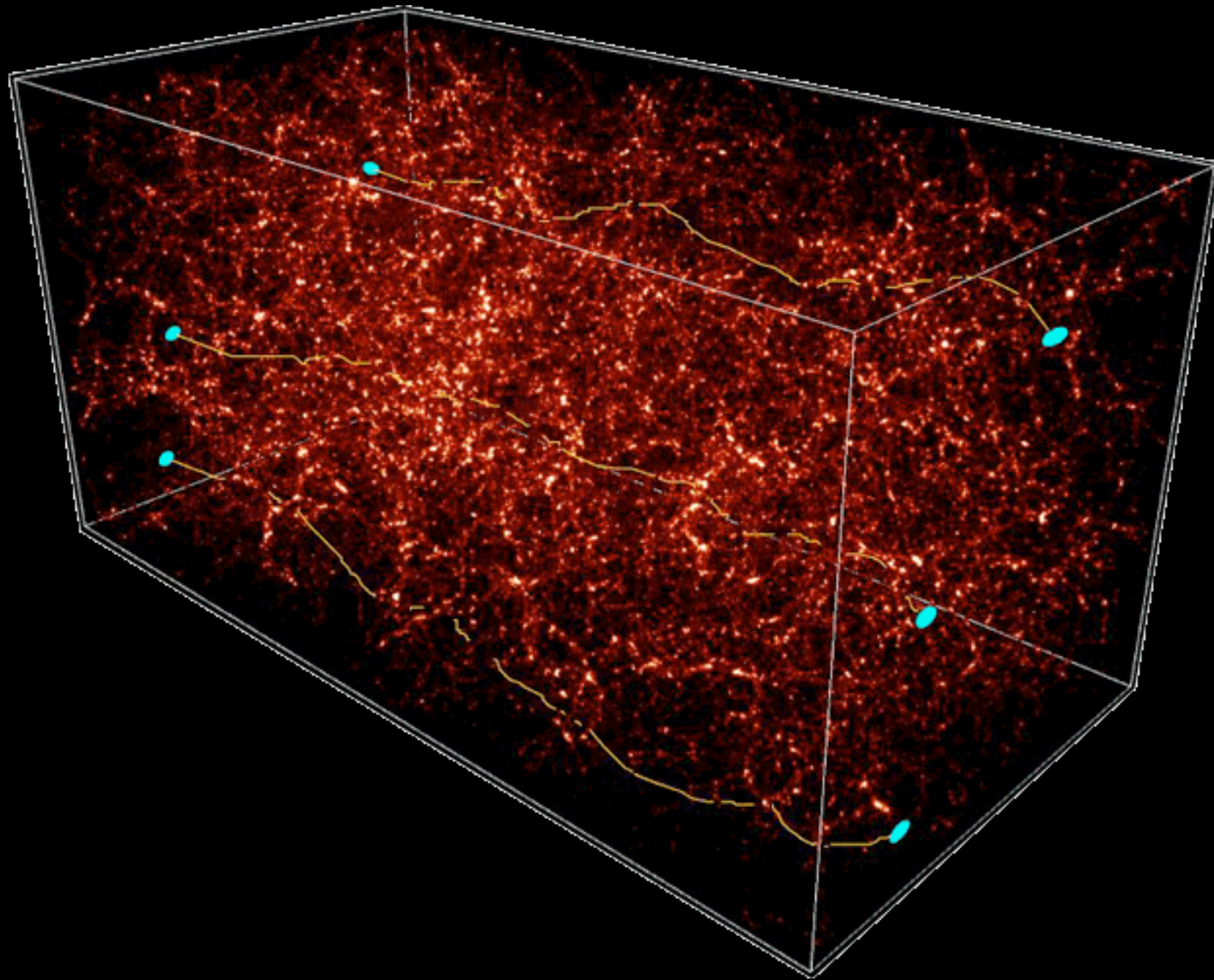


# Influence of Gravitational Lensing?





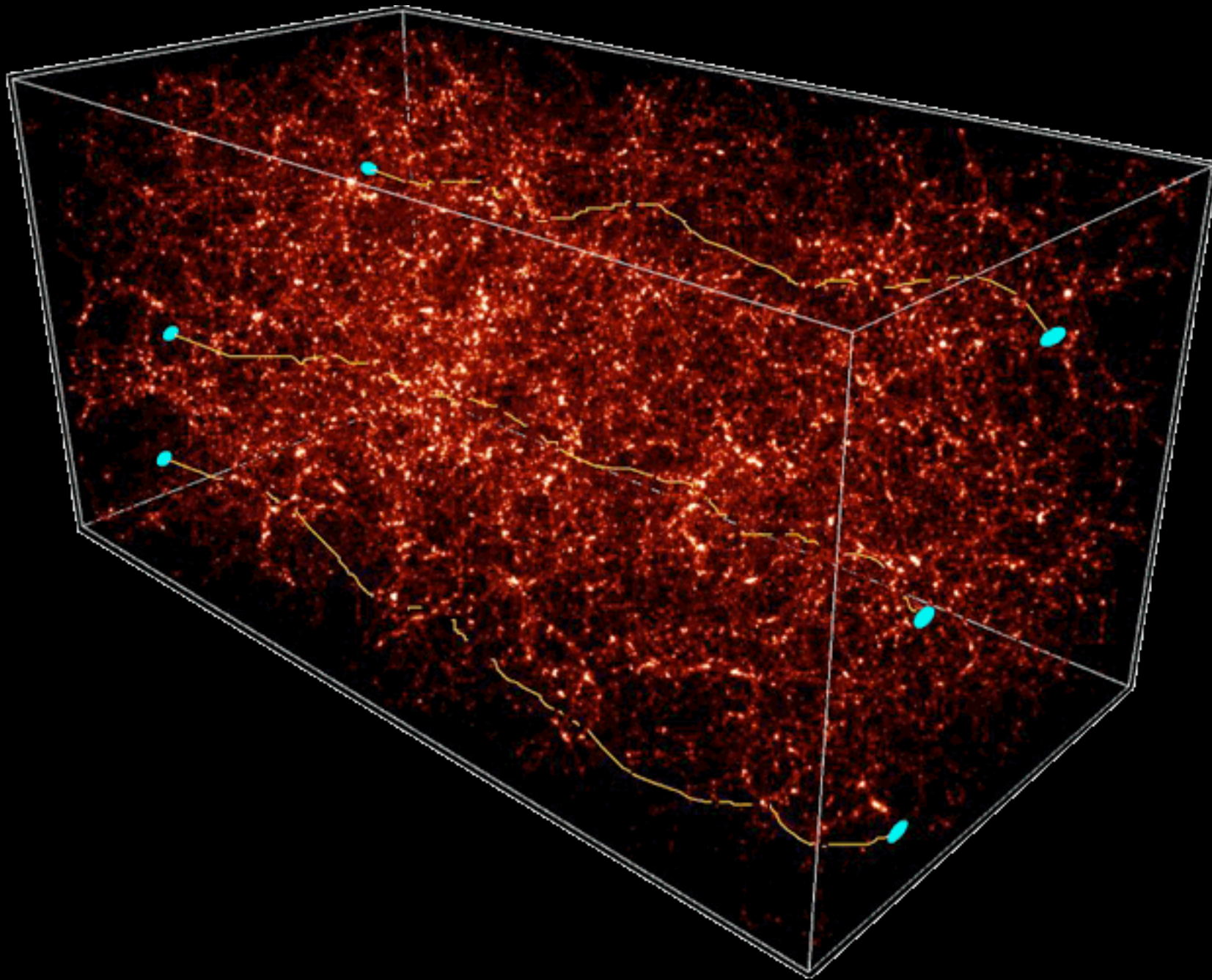
# Influence of Gravitational Lensing?



$$\mathcal{F}^{\text{obs,lensed}}(z, \hat{\mathbf{n}}) = \mu(z, \hat{\mathbf{n}}) \mathcal{F}^{\text{obs,true}}(z)$$



# Influence of Gravitational Lensing?

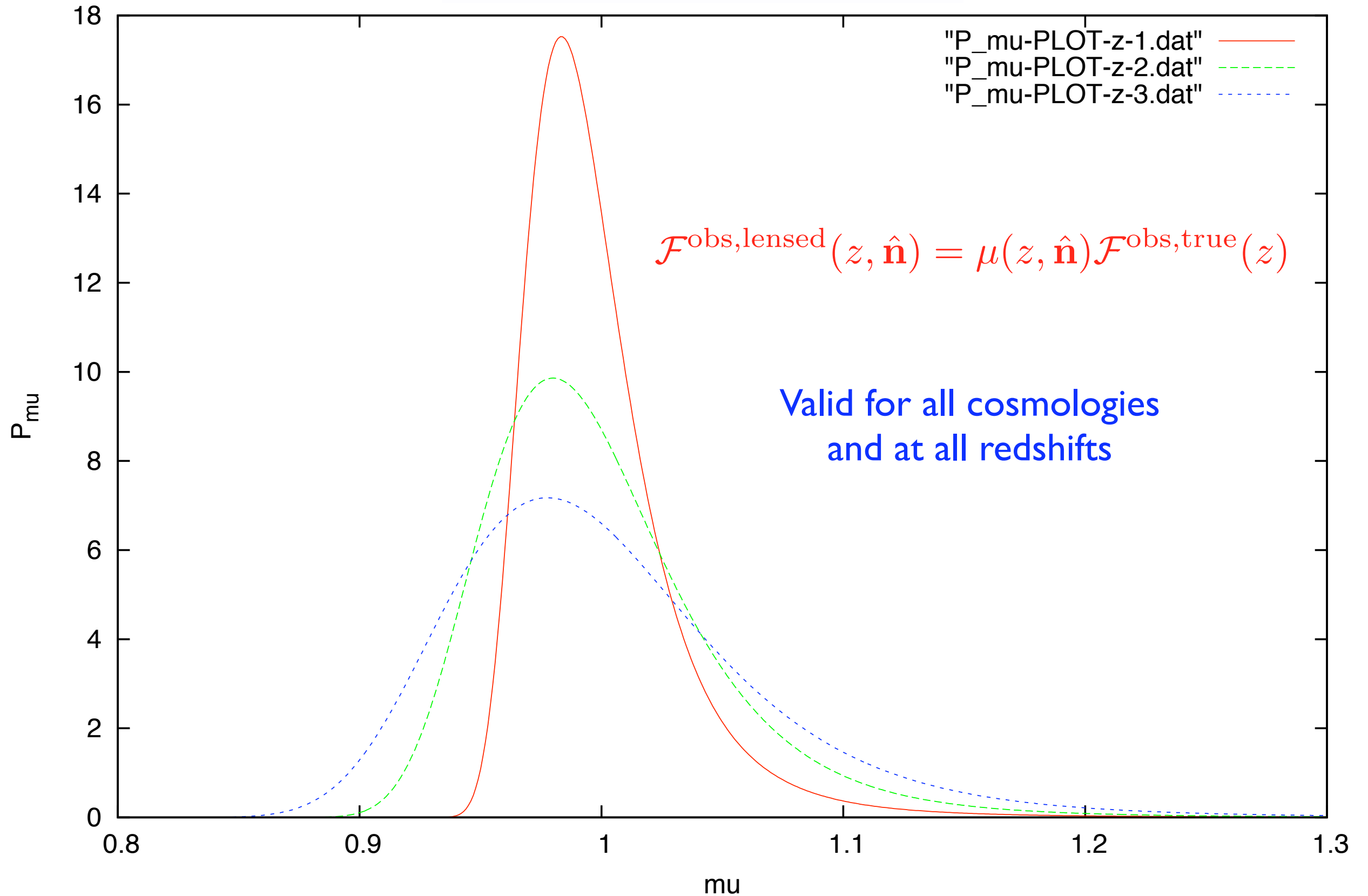


$$\mathcal{F}^{\text{obs,lensed}}(z, \hat{\mathbf{n}}) = \mu(z, \hat{\mathbf{n}}) \mathcal{F}^{\text{obs,true}}(z)$$

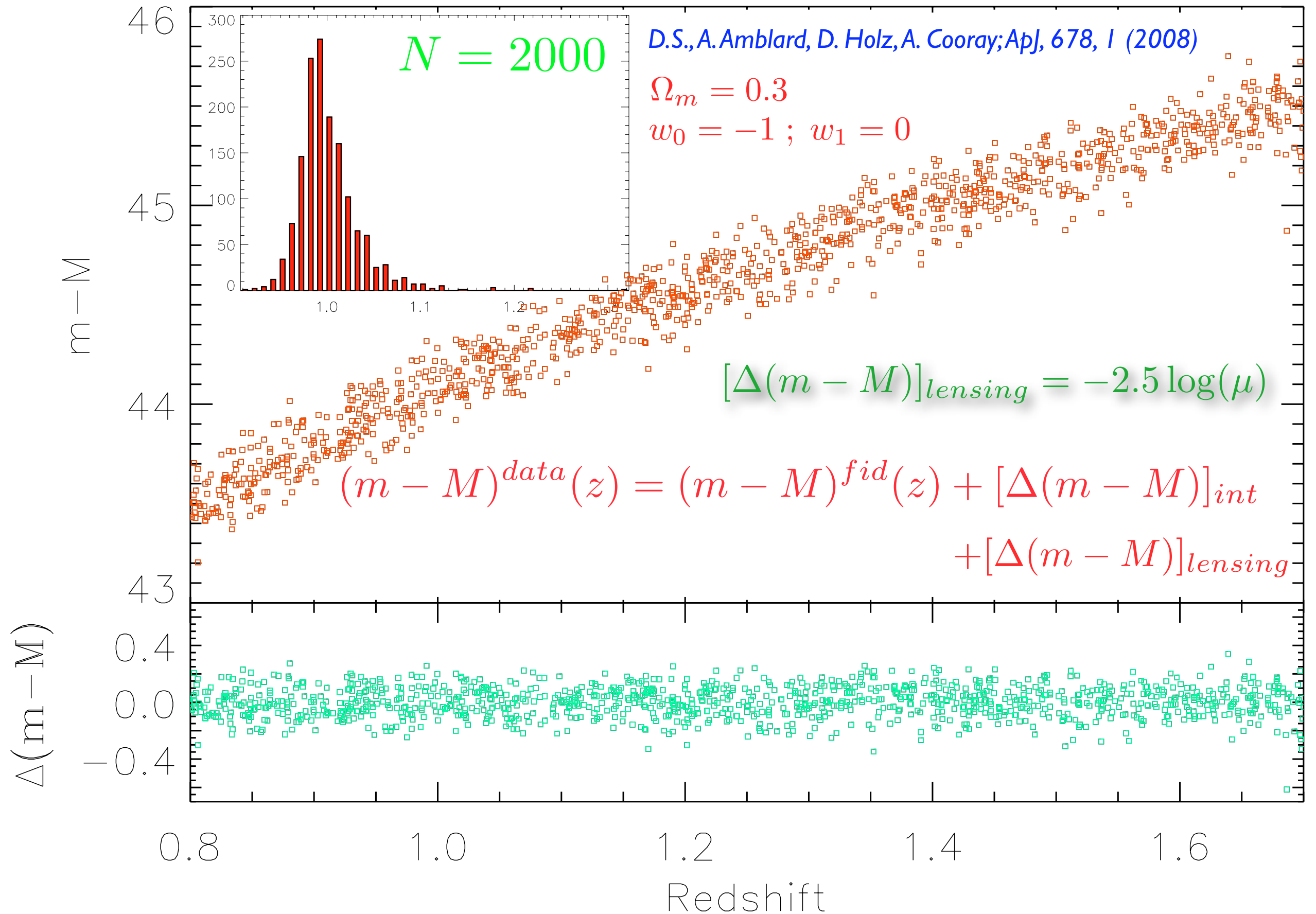
Weak lensing can modify the SNa flux & bias estimates of  $w$



# Amplification Probability Distribution

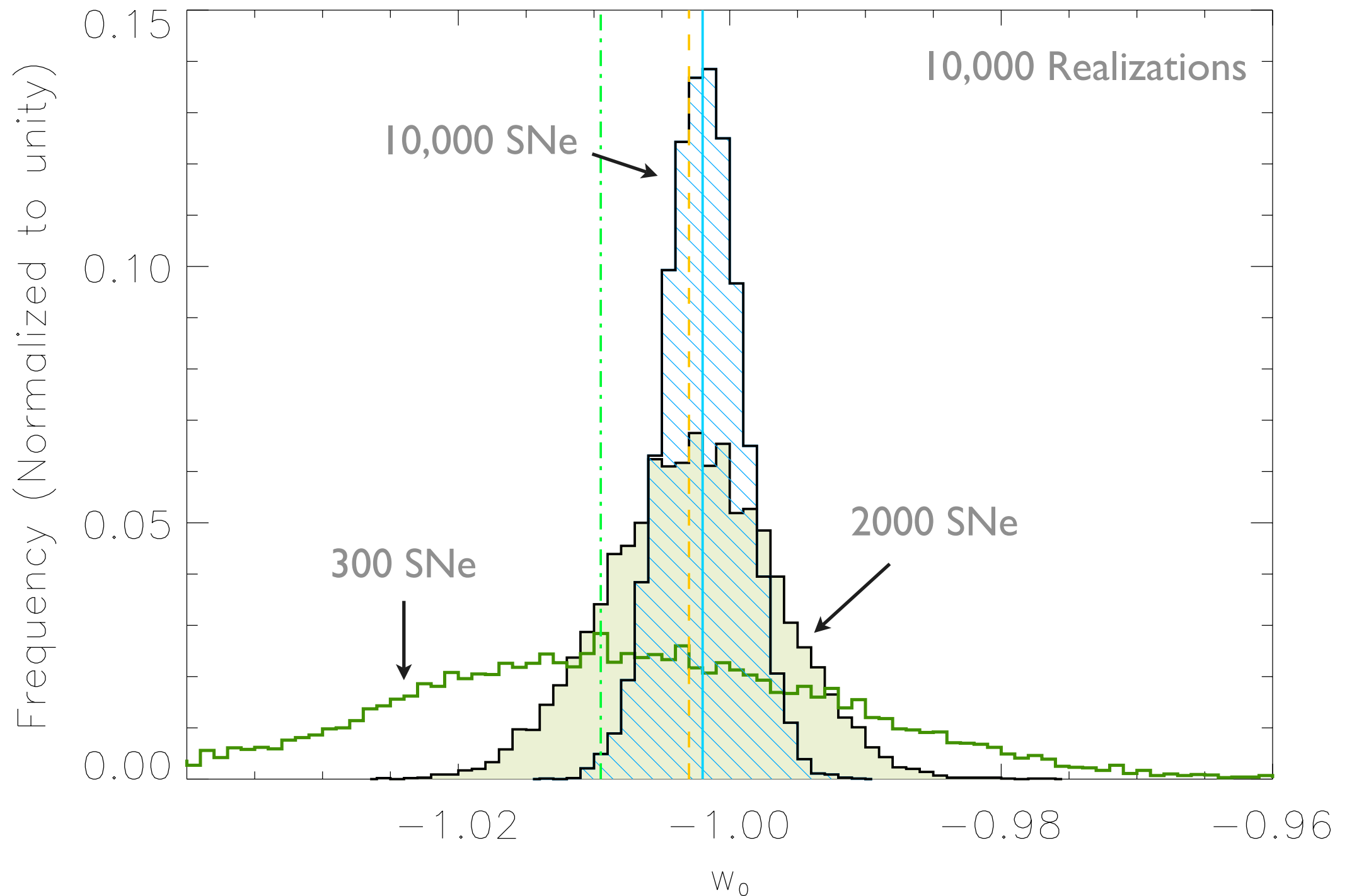


# Our Analysis with Mock Catalogs



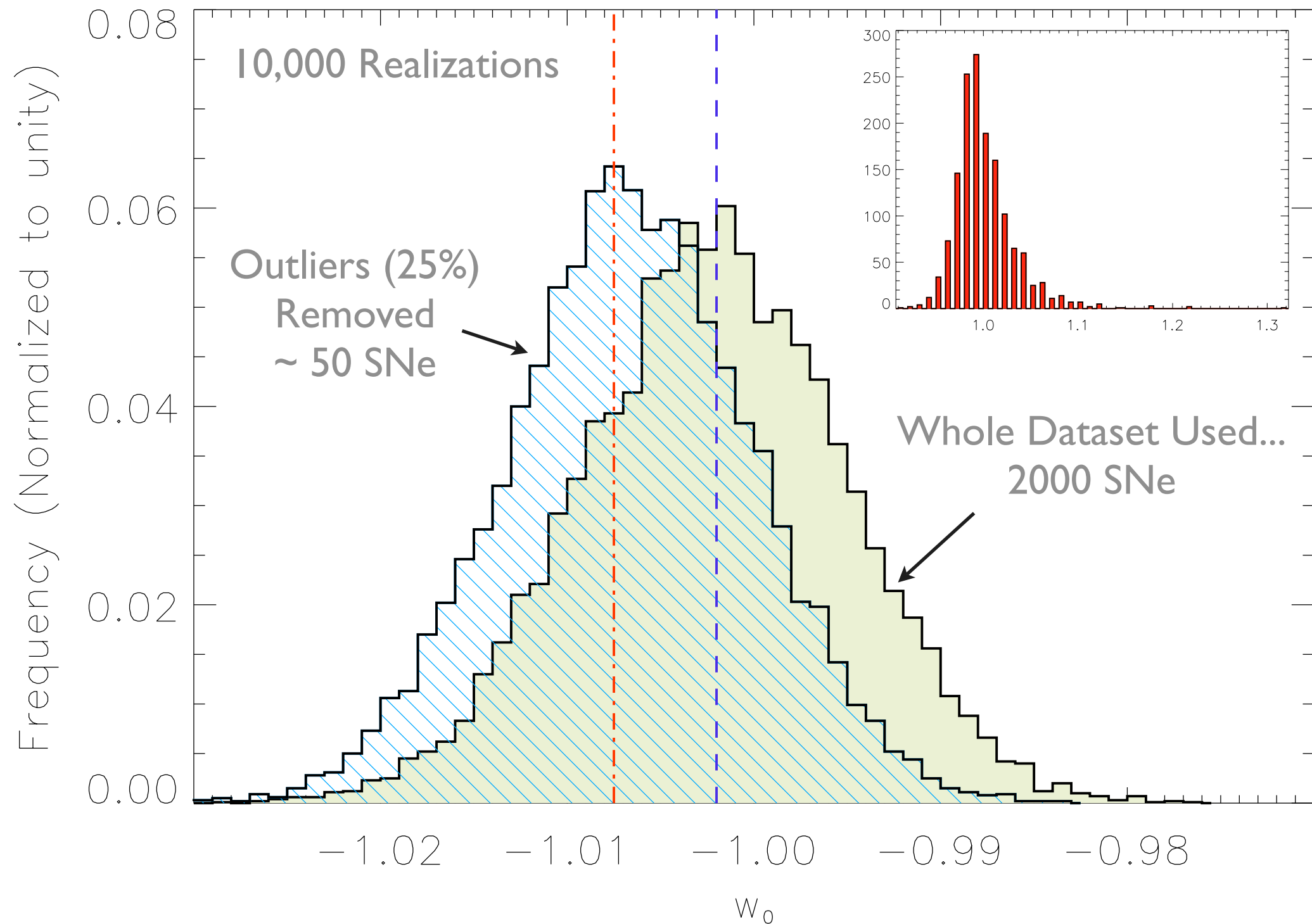


# Effect of Weak Lensing on Estimates of “w”



*D.S., A. Amblard, D. Holz, A. Cooray; ApJ, 678, 1 (2008)*

# Effect of Removing the Outliers



*D.S., A. Amblard, D. Holz, A. Cooray; ApJ, 678, 1 (2008)*



# Challenges: Systematic Uncertainties

source of uncertainty	common (mag)	sample-dep.(mag)	treatment
Extinction	0.013	-	Multi-band photometry including near-IR
Calibration	0.021	0.021	Calibration of standard stars (optical thru near-IR) to $<1\%$
Malmquist	-	0.020	High S/N lightcurves & spectra; requirement of pre-rise data
Lightcurve	0.028	-	SN spectra with broad $\lambda$ , temporal coverage
Evolution	0.015	-	High-resolution spectroscopy

Kowalski et al. (2008), Carnegie Supernova Project: W. Freedman

2-Population	Constrain the systematics to $< 2\%$ level to have the bias on “w” less than 1-sigma level without increasing error bar!
Lensing	Need a large # of SNe per redshift bin to keep bias $< 1\%$

# Outline

## Dark Energy

- \* Why Pursue Dark Energy?
- \* DE Equation of State (EOS)
- \* DE from SNe Ia ++
- \* Beware of Systematics
  - Two Population Model
  - Gravitational Lensing

## CMB Bispectrum

- \* Why Non-Gaussianity?
- \* Why in CMB Bispectrum?
- \* The  $f_{\text{NL}}$
- \* WL of CMB Bispectrum
  - ⊗ Analytical Sketch
  - ⊗ Numerical Results



# Outline

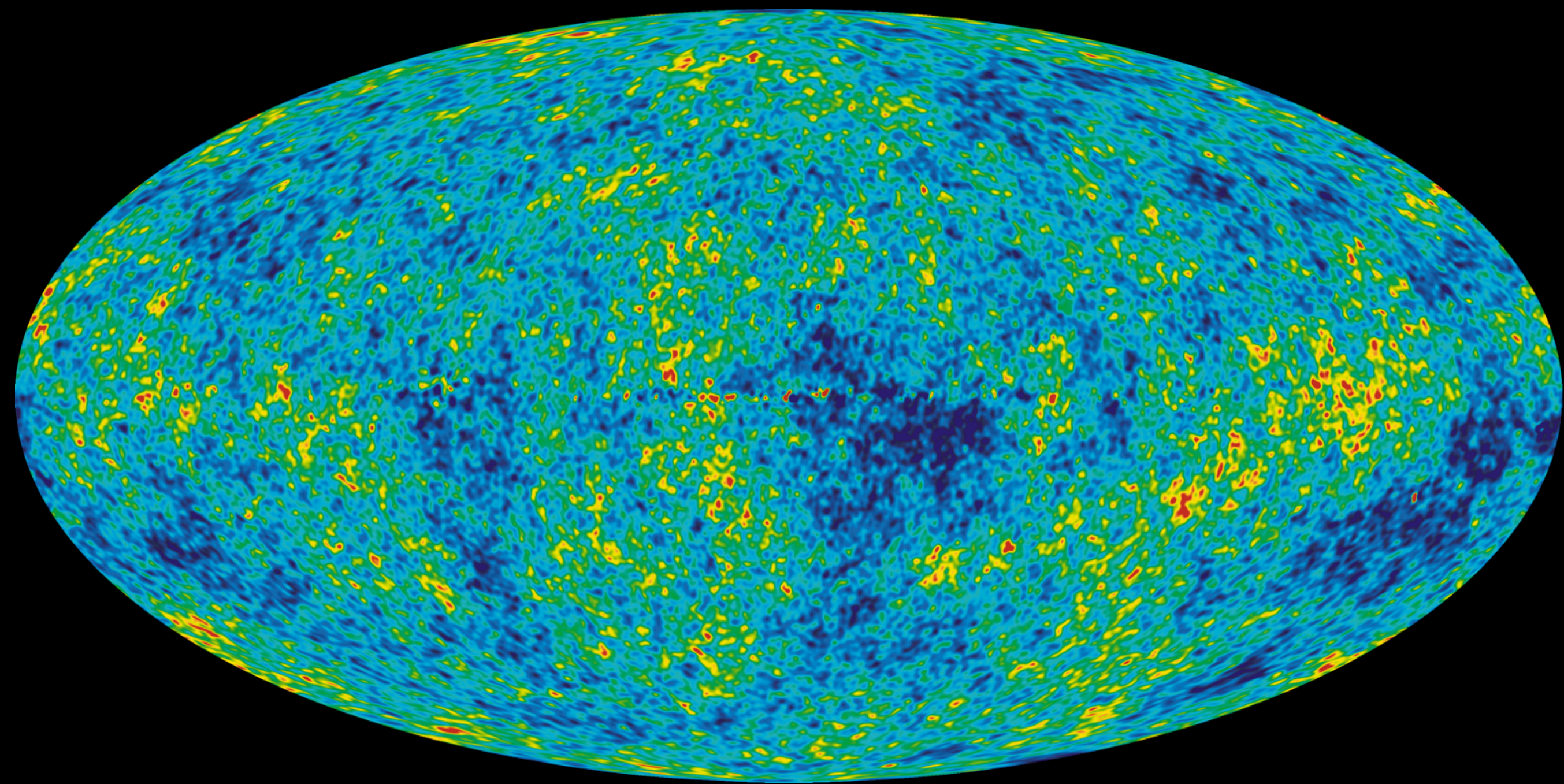
## Dark Energy

- \* Why Pursue Dark Energy?
- \* DE Equation of State (EOS)
- \* DE from SNe Ia ++
- \* Beware of Systematics
  - Two Population Model
  - Gravitational Lensing

## CMB Bispectrum

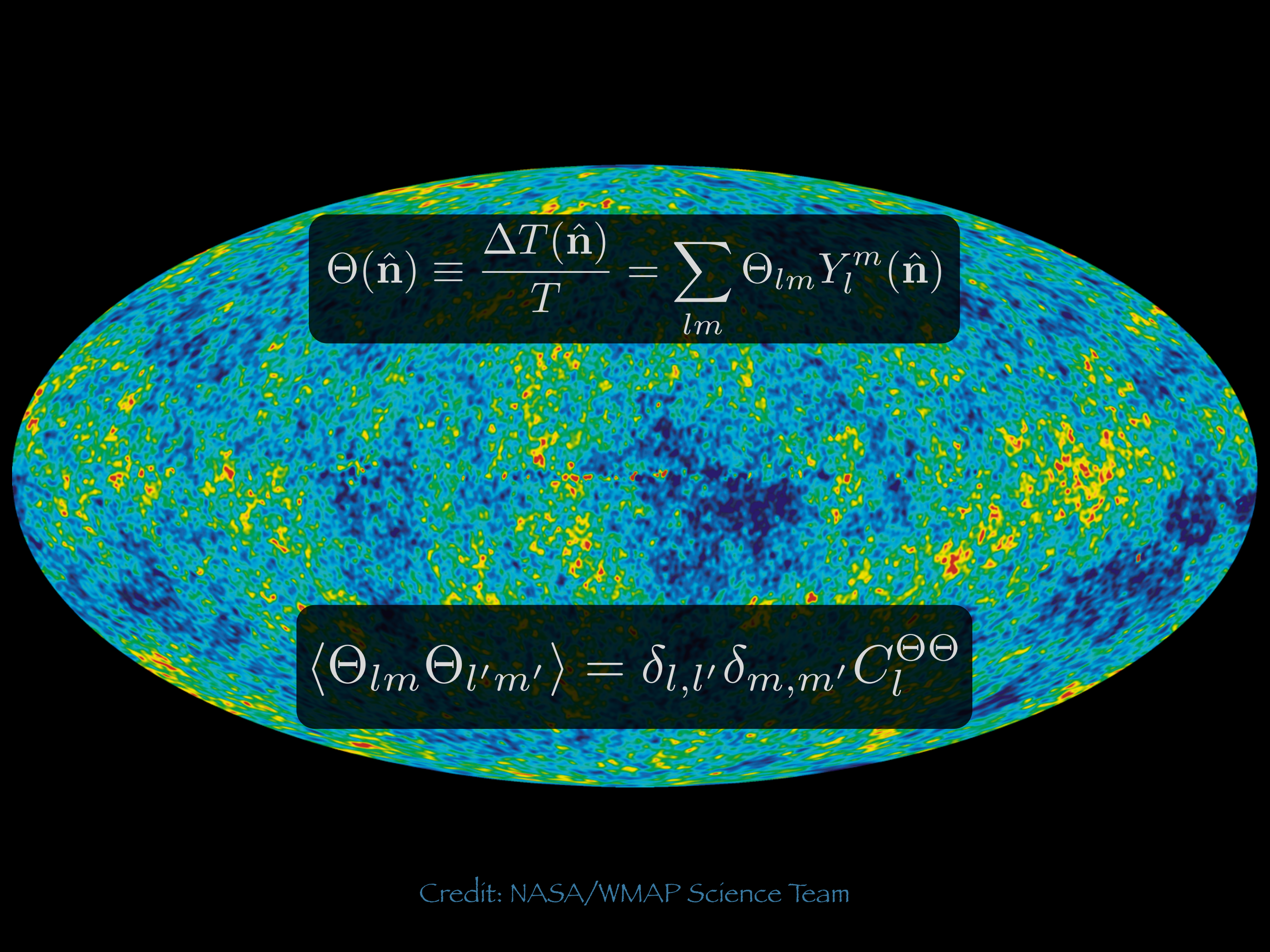
- \* Why Non-Gaussianity?
- \* Why in CMB Bispectrum?
- \* The  $f_{\text{NL}}$
- \* WL of CMB Bispectrum
  - ⊗ Analytical Sketch
  - ⊗ Numerical Results





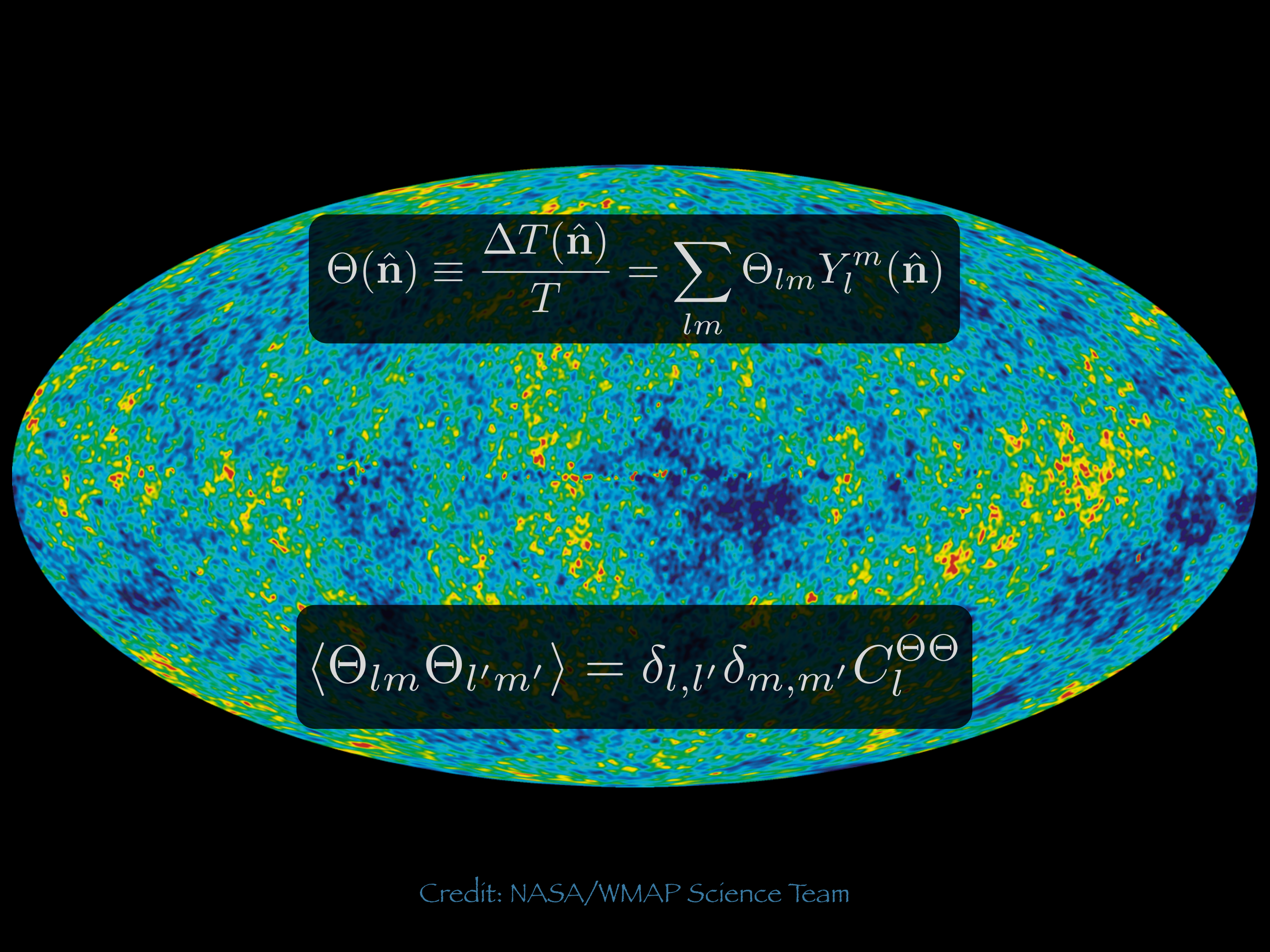
Credit: NASA/WMAP Science Team




$$\Theta(\hat{\mathbf{n}}) \equiv \frac{\Delta T(\hat{\mathbf{n}})}{T} = \sum_{lm} \Theta_{lm} Y_l^m(\hat{\mathbf{n}})$$

Credit: NASA/WMAP Science Team

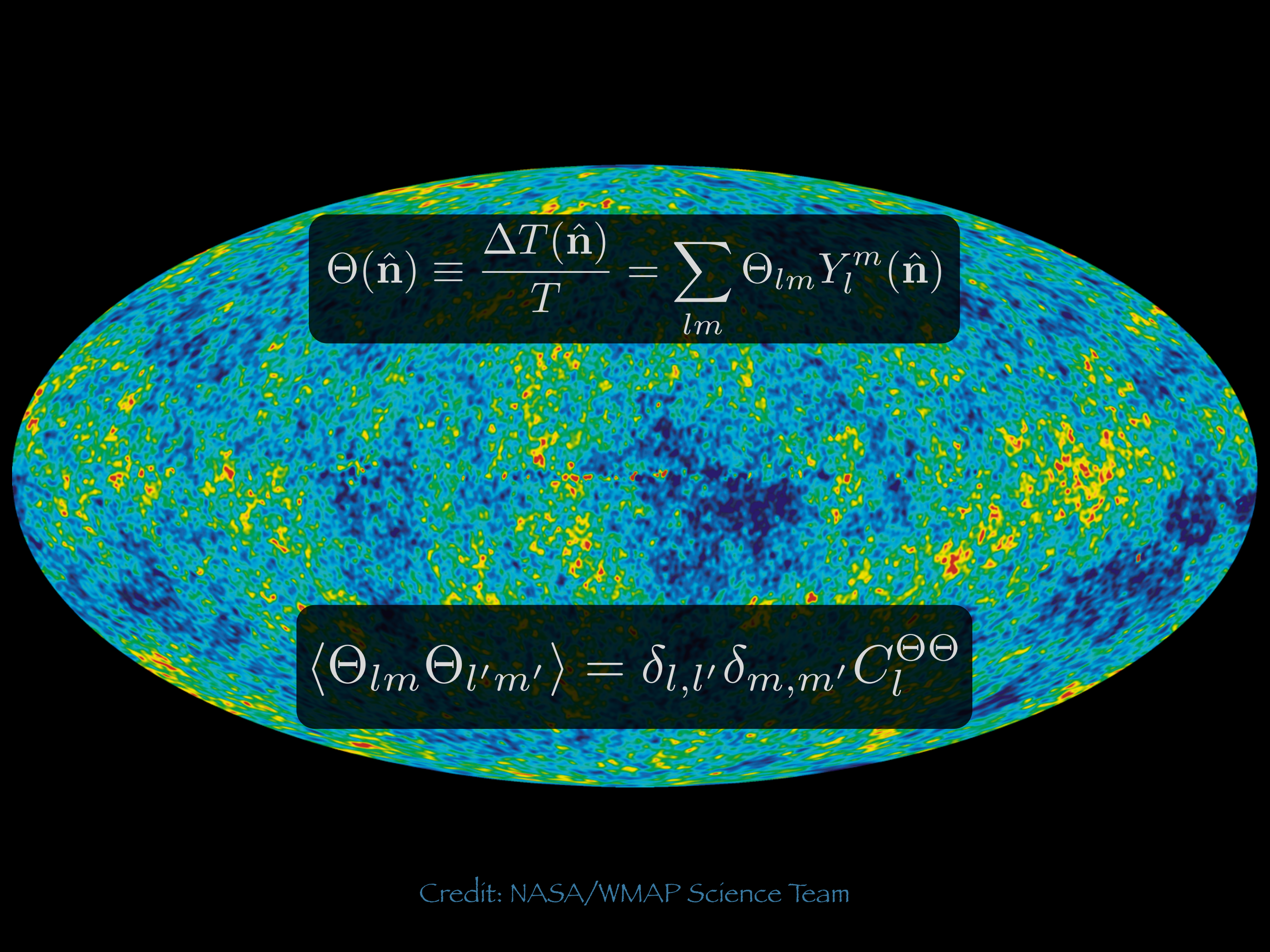



$$\Theta(\hat{\mathbf{n}}) \equiv \frac{\Delta T(\hat{\mathbf{n}})}{T} = \sum_{lm} \Theta_{lm} Y_l^m(\hat{\mathbf{n}})$$

$$\langle \Theta_{lm} \Theta_{l'm'} \rangle = \delta_{l,l'} \delta_{m,m'} C_l^{\Theta\Theta}$$

Credit: NASA/WMAP Science Team



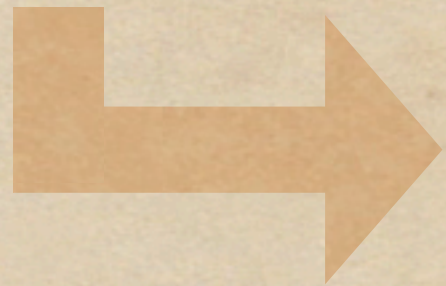

$$\Theta(\hat{\mathbf{n}}) \equiv \frac{\Delta T(\hat{\mathbf{n}})}{T} = \sum_{lm} \Theta_{lm} Y_l^m(\hat{\mathbf{n}})$$

$$\langle \Theta_{l_1 m_1} \Theta_{l_2 m_2} \Theta_{l_3 m_3} \rangle = \begin{pmatrix} l_1 & l_2 & l_3 \\ m_1 & m_2 & m_3 \end{pmatrix} B_{l_1 l_2 l_3}^{\Theta}$$

$$\langle \Theta_{lm} \Theta_{l'm'} \rangle = \delta_{l,l'} \delta_{m,m'} C_l^{\Theta\Theta}$$



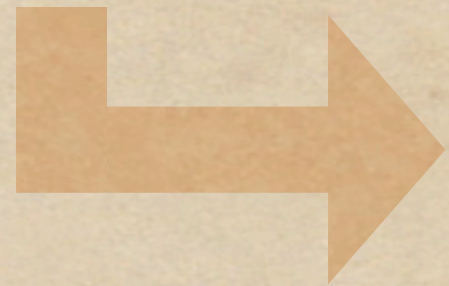
Primordial non-Gaussianity



Primary CMB Bispectrum



# Primordial non-Gaussianity



## Primary CMB Bispectrum

Gaussian Quantum Fluctuation



Non-Gaussian Inflation Fluctuation



Non-Gaussian Curvature Perturbation

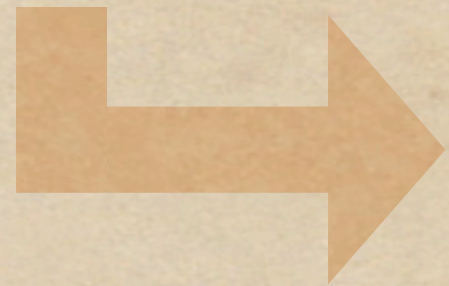


Non-Gaussian CMB Anisotropy





# Primordial non-Gaussianity

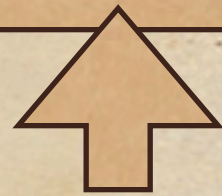


Primary CMB Bispectrum

$$\frac{\Delta T(\mathbf{x})}{T} \sim \Phi(\mathbf{x})$$



$$\Phi(\mathbf{x}) = \Phi_L(\mathbf{x}) + f_{NL} [\Phi_L^2(\mathbf{x}) - \langle \Phi_L^2(\mathbf{x}) \rangle]$$

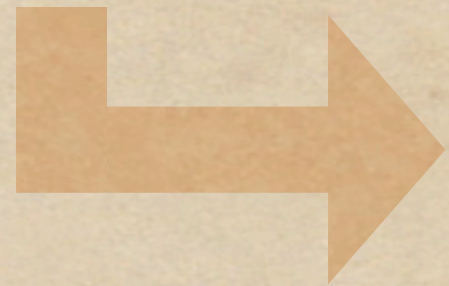


Non-Linear Coupling Parameter

Measurement of non-Gaussian CMB anisotropies can potentially constrain non-linearity, “slow-rollness”, and “adiabaticity” in inflation.



# Primordial non-Gaussianity



## Primary CMB Bispectrum

Non-Gaussianity from the simplest inflation model is very small:

$$f_{NL} \sim 0.01 - 1$$

Much higher level of primordial non-Gaussianity is predicted by:

- Models with Multiple Scalar Fields
- Non-Adiabatic Fluctuations
- Features in the Inflation Potential
- Non-Canonical Kinetic Terms
- ...



# Evidence of Primordial Non-Gaussianity ( $f_{\text{NL}}$ ) in the Wilkinson Microwave Anisotropy Probe 3-Year Data at $2.8\sigma$

Amit P. S. Yadav<sup>1</sup> and Benjamin D. Wandelt<sup>1,2</sup>

<sup>1</sup>*Department of Astronomy, University of Illinois at Urbana-Champaign, 1002 W. Green Street, Urbana, Illinois 61801, USA*

<sup>2</sup>*Department of Physics, University of Illinois at Urbana-Champaign, 1110 W. Green Street, Urbana, Illinois 61801, USA*

(Received 7 December 2007; revised manuscript received 6 March 2008; published 7 May 2008)

We present evidence for primordial non-Gaussianity of the local type ( $f_{\text{NL}}$ ) in the temperature anisotropy of the cosmic microwave background. Analyzing the bispectrum of the Wilkinson Microwave Anisotropy Probe 3-year data up to  $\ell_{\text{max}} = 750$  we find  $27 < f_{\text{NL}} < 147$  (95% C.L.). This amounts to a rejection of  $f_{\text{NL}} = 0$  at  $2.8\sigma$ , disfavoring canonical single-field slow-roll inflation. The signal is robust to variations in  $\ell_{\text{max}}$ , frequency and masks. No known foreground, instrument systematic, or secondary anisotropy explains it. We explore the impact of several analysis choices on the quoted significance and find  $2.5\sigma$  to be conservative.

---

## FIVE-YEAR WILKINSON MICROWAVE ANISOTROPY PROBE (WMAP<sup>1</sup>) OBSERVATIONS: COSMOLOGICAL INTERPRETATION

E. KOMATSU<sup>1</sup>, J. DUNKLEY<sup>2,3,4</sup>, M. R. NOLTA<sup>5</sup>, C. L. BENNETT<sup>6</sup>, B. GOLD<sup>6</sup>, G. HINSHAW<sup>7</sup>, N. JAROSIK<sup>2</sup>, D. LARSON<sup>6</sup>, M. LIMON<sup>8</sup>, L. PAGE<sup>2</sup>, D. N. SPERGEL<sup>3,9</sup>, M. HALPERN<sup>10</sup>, R. S. HILL<sup>11</sup>, A. KOGUT<sup>7</sup>, S. S. MEYER<sup>12</sup>, G. S. TUCKER<sup>13</sup>, J. L. WEILAND<sup>10</sup>, E. WOLLACK<sup>7</sup>, AND E. L. WRIGHT<sup>14</sup>

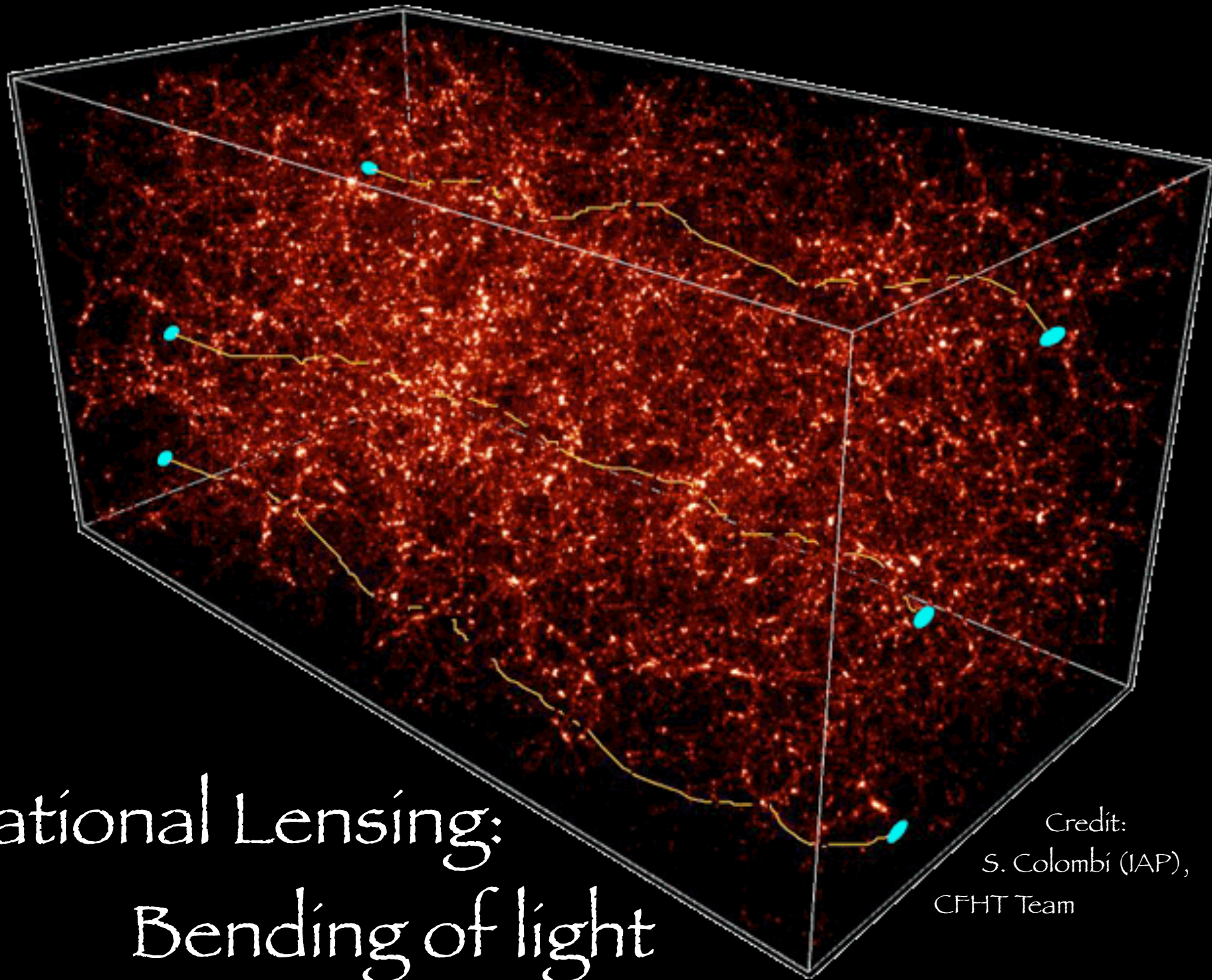
*Submitted to the Astrophysical Journal Supplement Series*

### ABSTRACT

$$-9 < f_{\text{NL}}^{\text{local}} < 111 \text{ and } -151 < f_{\text{NL}}^{\text{equil}} < 253 (95\% \text{ CL})$$



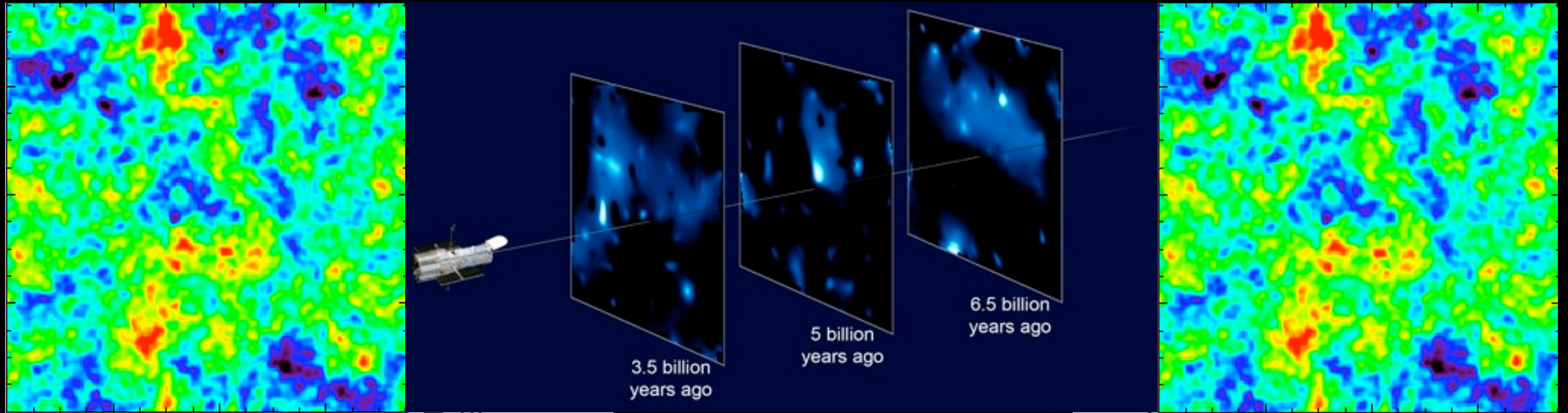
# Journey Through the “Clumpy” Universe



Weak  
Gravitational Lensing:  
Bending of light

Credit:  
S. Colombi (IAP),  
CFHT Team

# Weak Lensing of the Primary Bispectrum



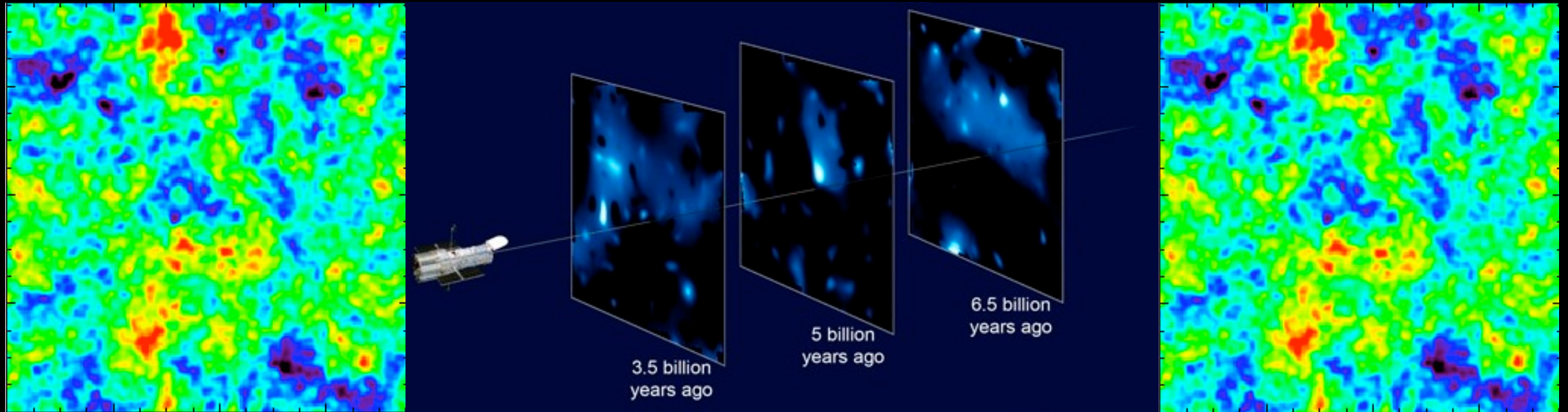
Credit: Vale, Amblard, White (2004)

NASA, ESA, and R. Massey (CalTech)

Credit: Vale, Amblard, White (2004)



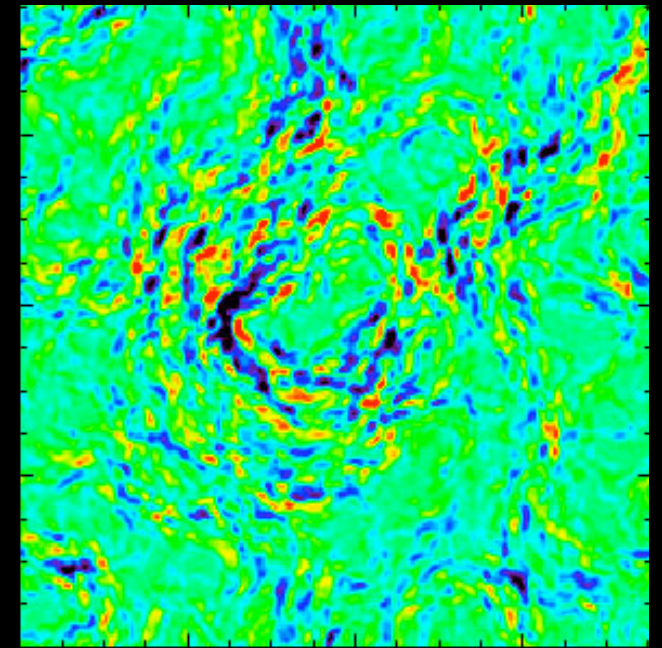
# Weak Lensing of the Primary Bispectrum



Credit: Vale, Amblard, White (2004)

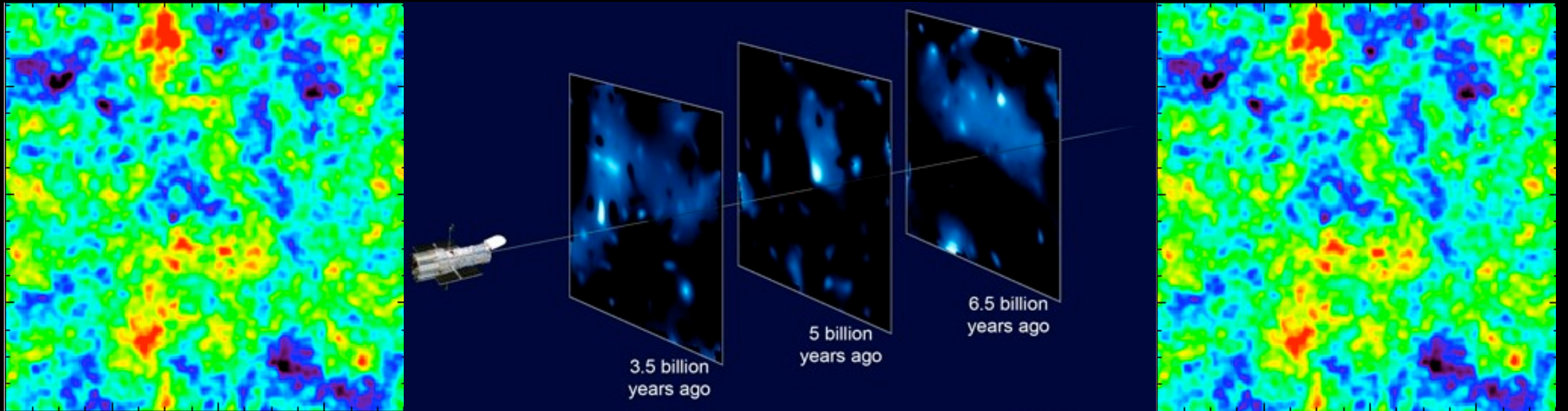
NASA, ESA, and R. Massey (CalTech)

Credit: Vale, Amblard, White (2004)





# Weak Lensing of the Primary Bispectrum

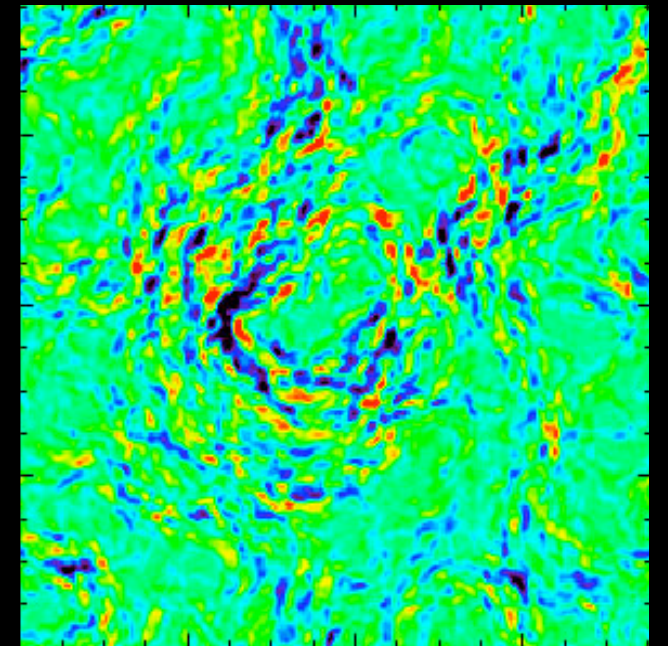


Credit: Vale, Amblard, White (2004)

NASA, ESA, and R. Massey (CalTech)

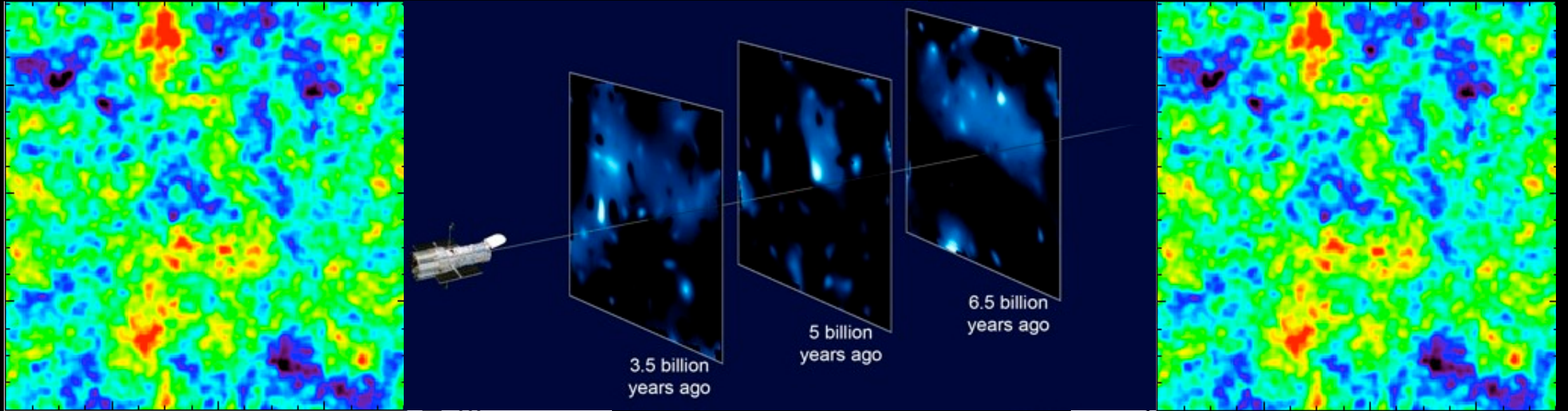
Credit: Vale, Amblard, White (2004)

$$\begin{aligned}
 \tilde{\Theta}(\hat{\mathbf{n}}) &= \Theta[\hat{\mathbf{n}} + \hat{\alpha}] \\
 &= \Theta[\hat{\mathbf{n}} + \nabla\phi(\hat{\mathbf{n}})] \\
 &\approx \Theta(\hat{\mathbf{n}}) + \nabla_i\phi(\hat{\mathbf{n}})\nabla^i\Theta(\hat{\mathbf{n}}) \\
 &\quad + \frac{1}{2}\nabla_i\phi(\hat{\mathbf{n}})\nabla_j\phi(\hat{\mathbf{n}})\nabla^i\nabla^j\Theta(\hat{\mathbf{n}})
 \end{aligned}$$





# Weak Lensing of the Primary Bispectrum

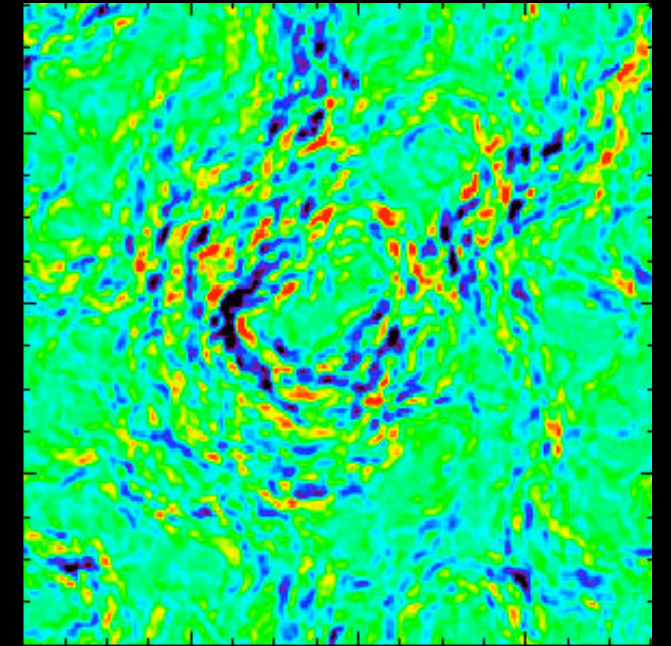


Credit: Vale, Amblard, White (2004)

NASA, ESA, and R. Massey (CalTech)

Credit: Vale, Amblard, White (2004)

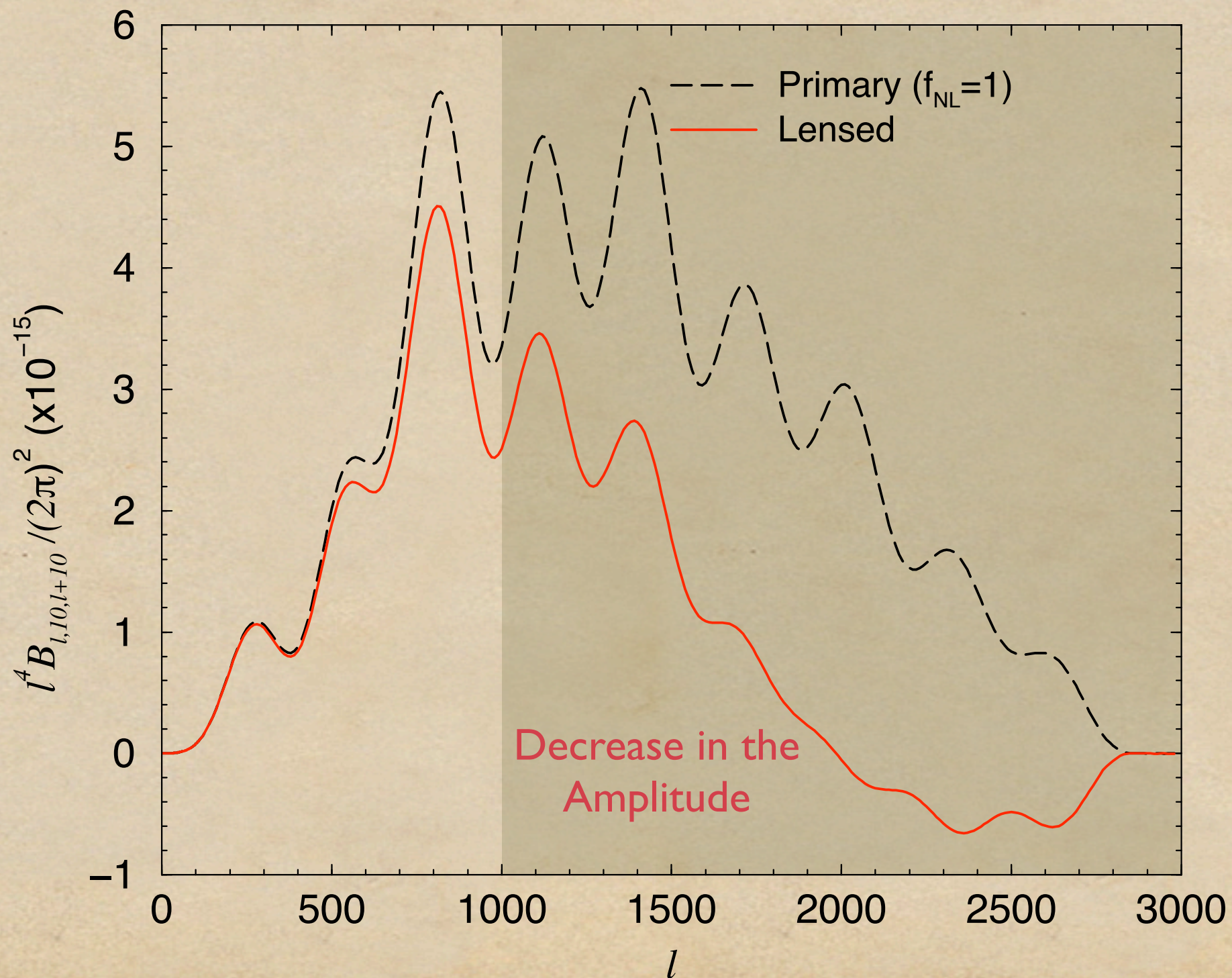
$$\begin{aligned}
 \tilde{\Theta}(\hat{\mathbf{n}}) &= \Theta[\hat{\mathbf{n}} + \hat{\alpha}] \\
 &= \Theta[\hat{\mathbf{n}} + \nabla\phi(\hat{\mathbf{n}})] \\
 &\approx \Theta(\hat{\mathbf{n}}) + \nabla_i\phi(\hat{\mathbf{n}})\nabla^i\Theta(\hat{\mathbf{n}}) \\
 &\quad + \frac{1}{2}\nabla_i\phi(\hat{\mathbf{n}})\nabla_j\phi(\hat{\mathbf{n}})\nabla^i\nabla^j\Theta(\hat{\mathbf{n}})
 \end{aligned}$$



$$\tilde{B}_{l_1 l_2 l_3}^{\Theta} = \sum_{m_1 m_2 m_3} \begin{pmatrix} l_1 & l_2 & l_3 \\ m_1 & m_2 & m_3 \end{pmatrix} \langle \tilde{\Theta}_{l_1 m_1} \tilde{\Theta}_{l_2 m_2} \tilde{\Theta}_{l_3 m_3} \rangle$$

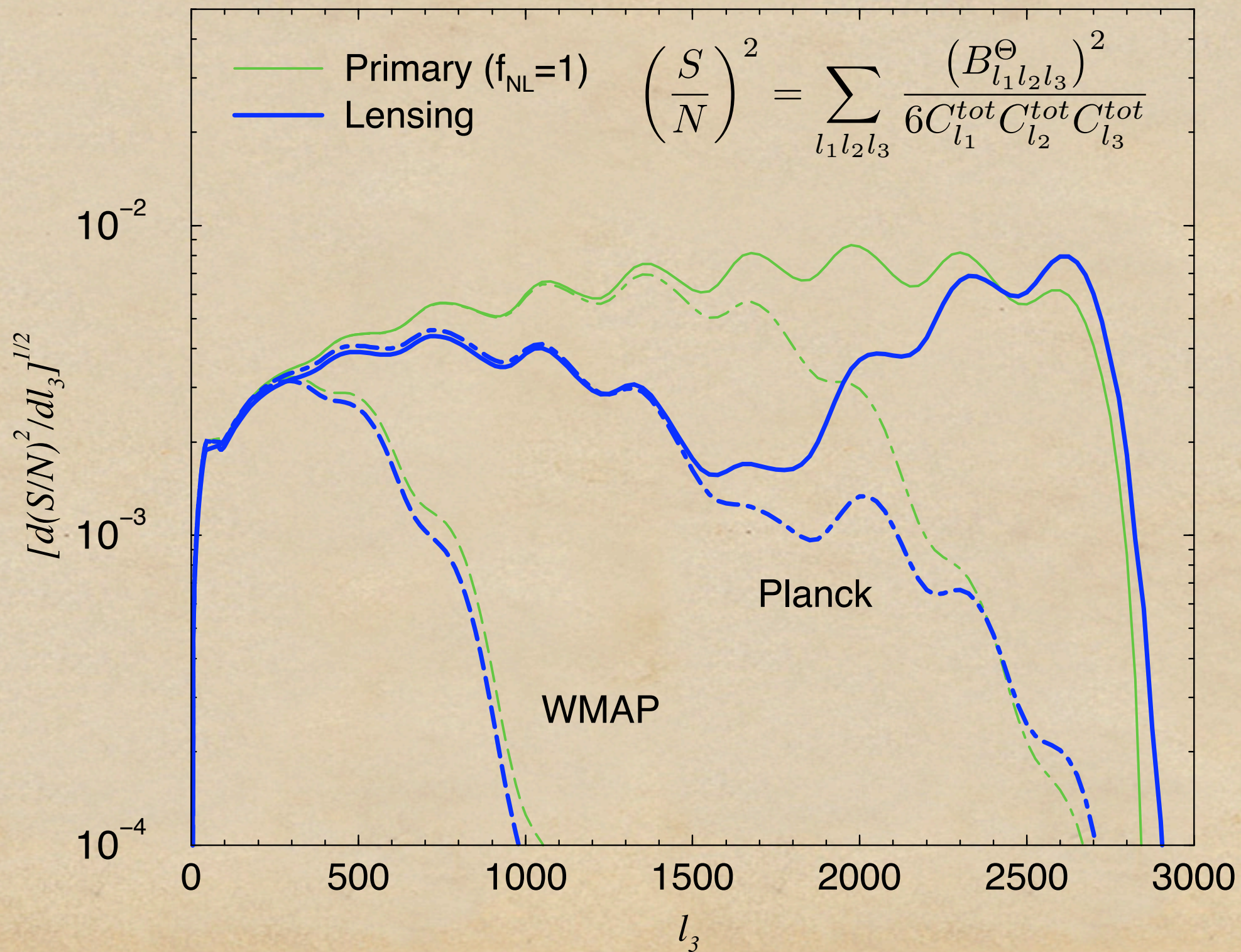


# The Effect of Lensing on the Bispectrum



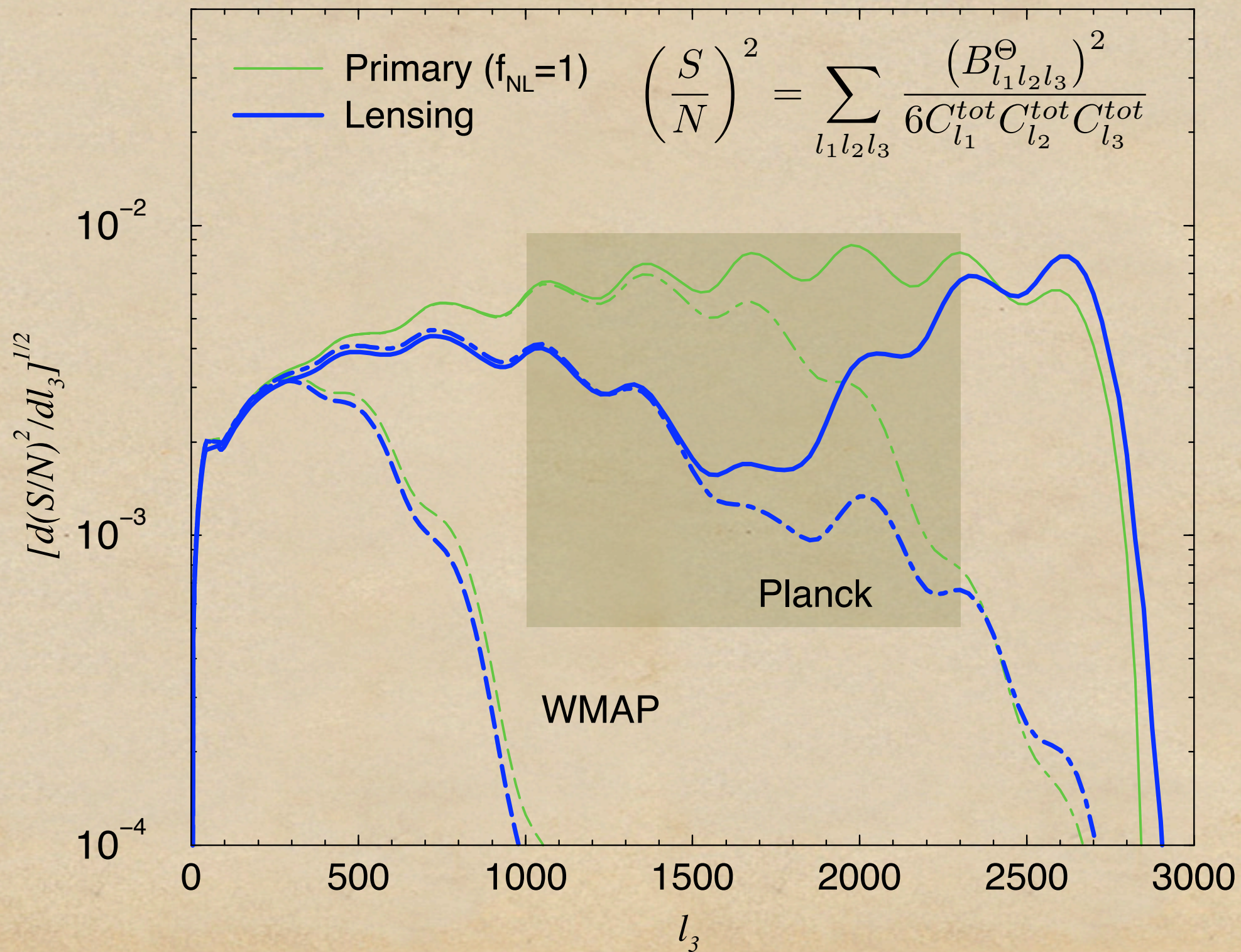


# Reduction in the S/N due to Lensing



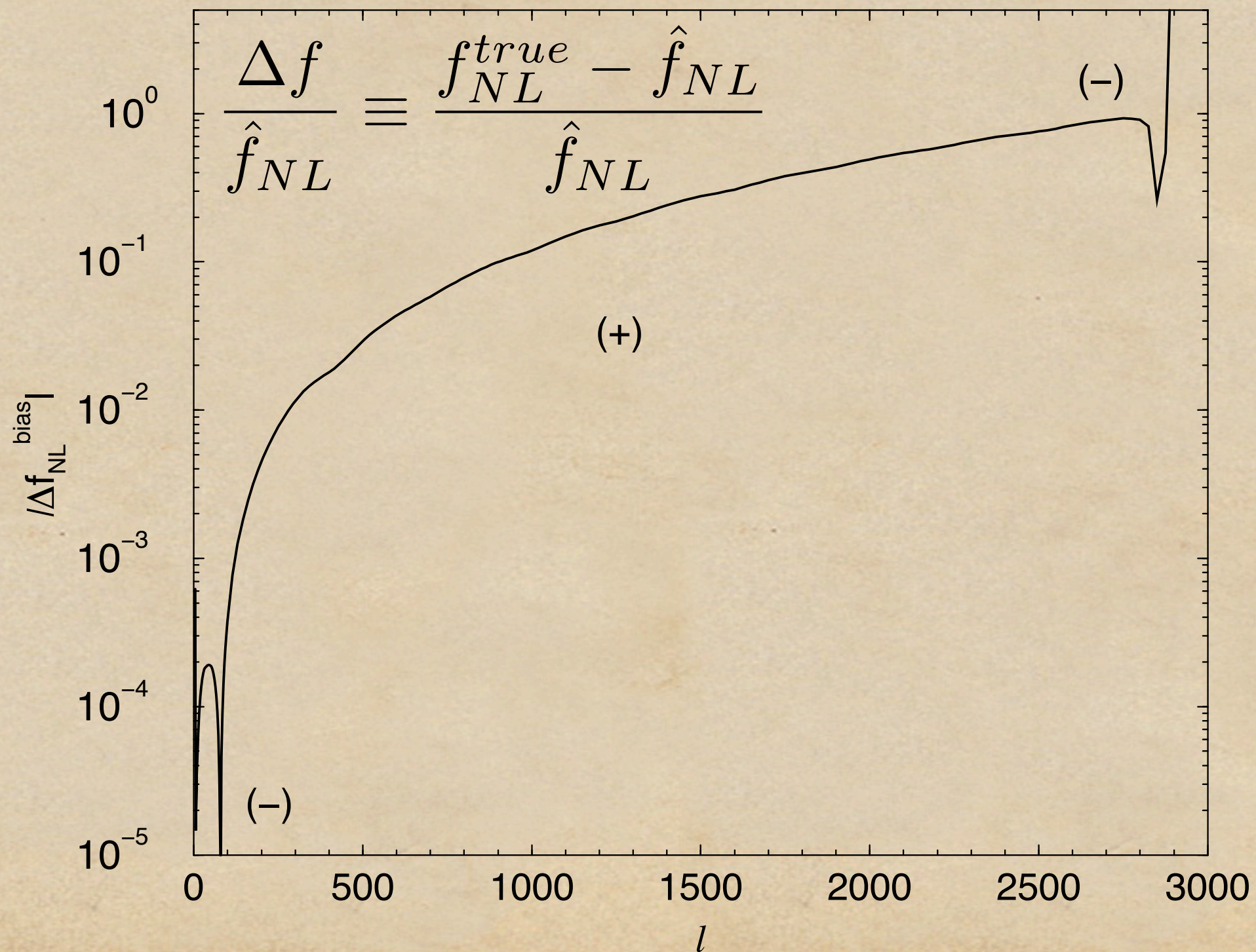


# Reduction in the S/N due to Lensing



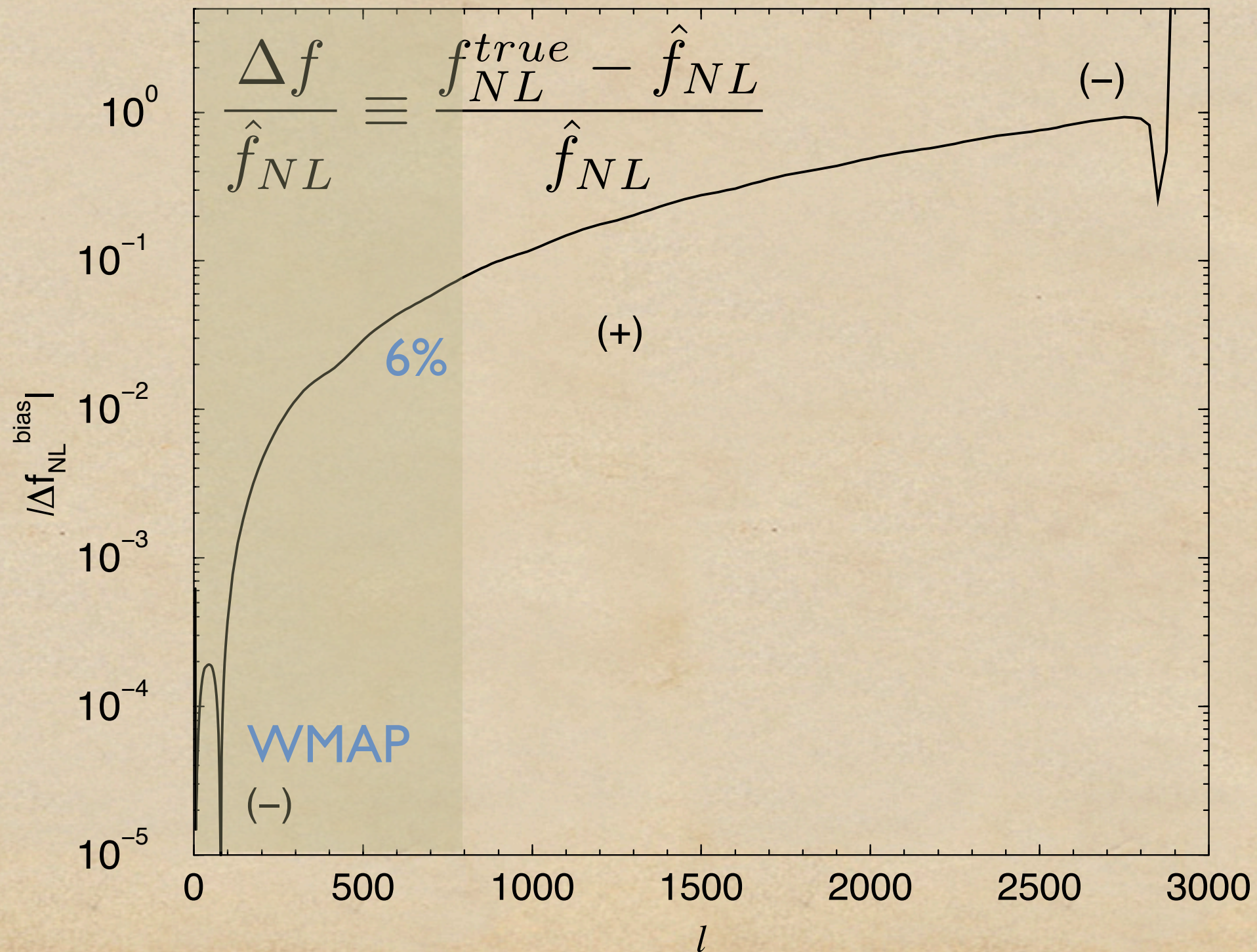


# Bias in the non-Gaussian Parameter



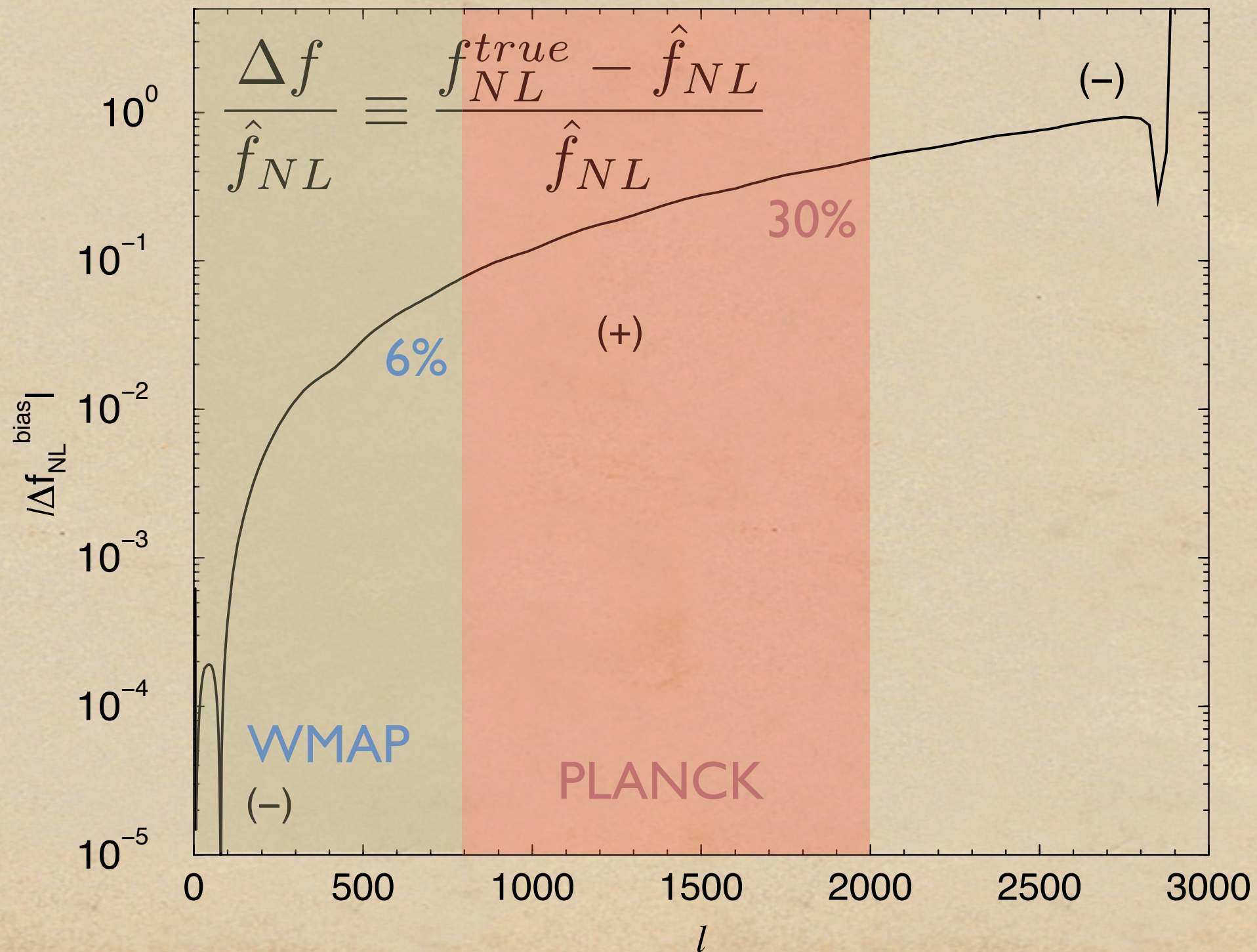


# Bias in the non-Gaussian Parameter



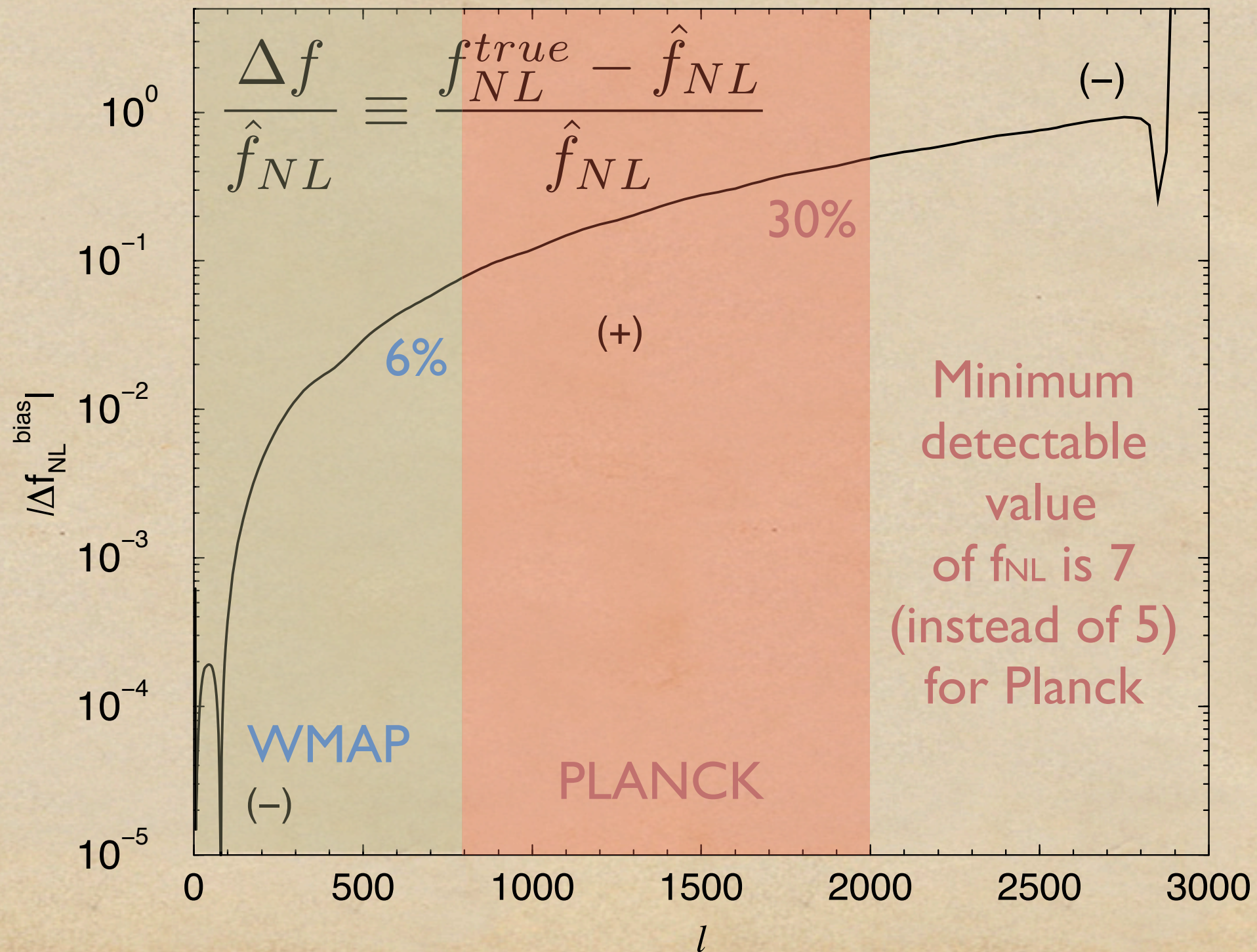


# Bias in the non-Gaussian Parameter





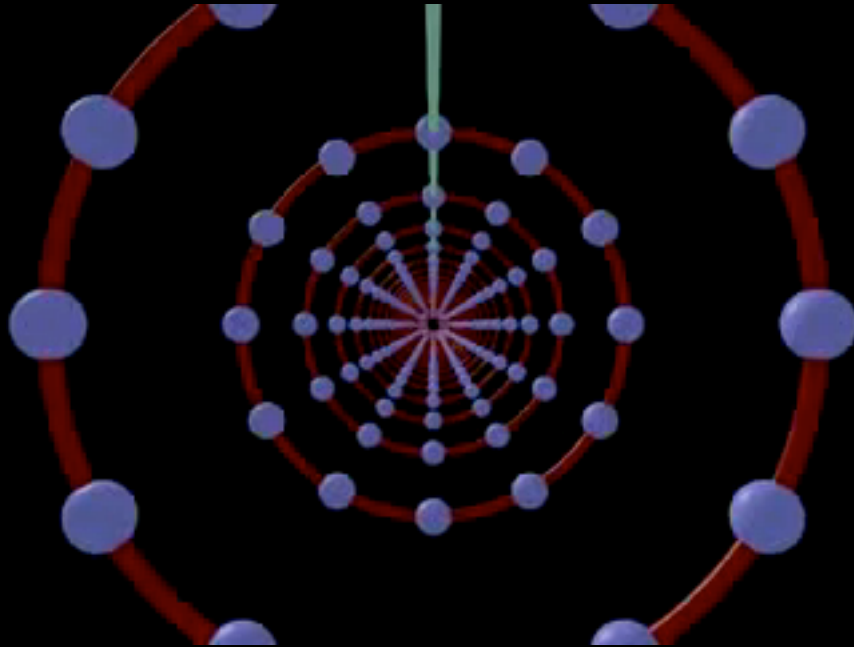
# Bias in the non-Gaussian Parameter





# Gravitational Waves

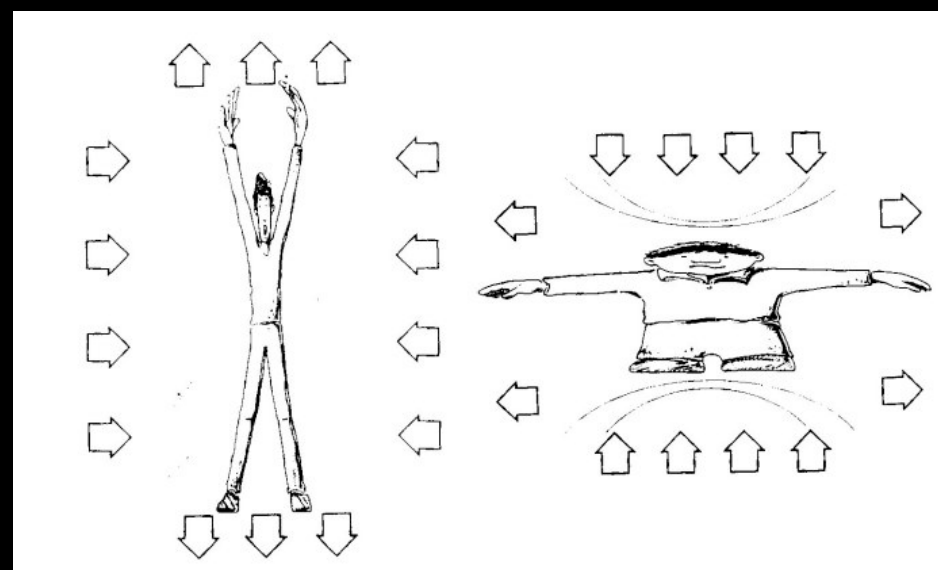
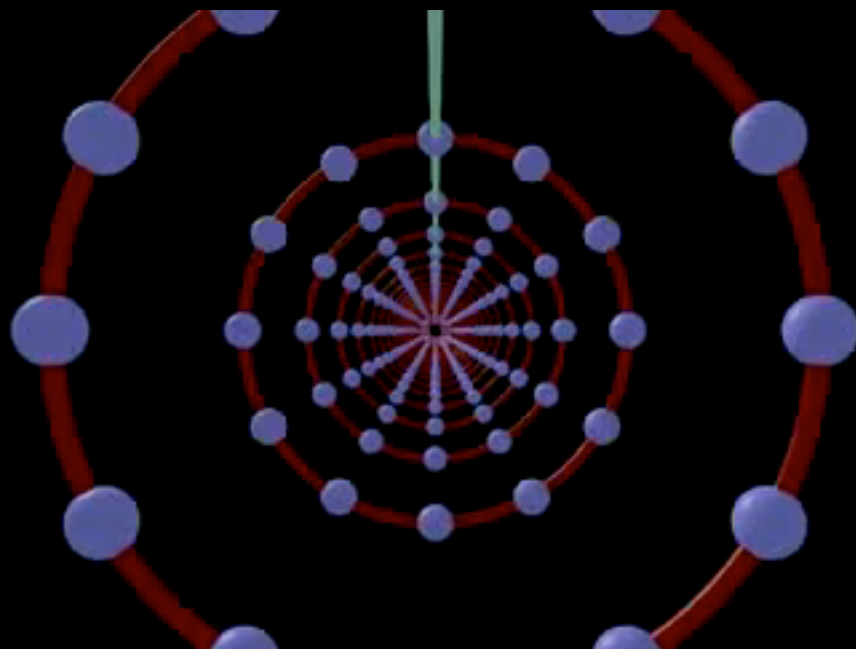
Credit: Michael  
Penn State Schuykill





# Gravitational Waves

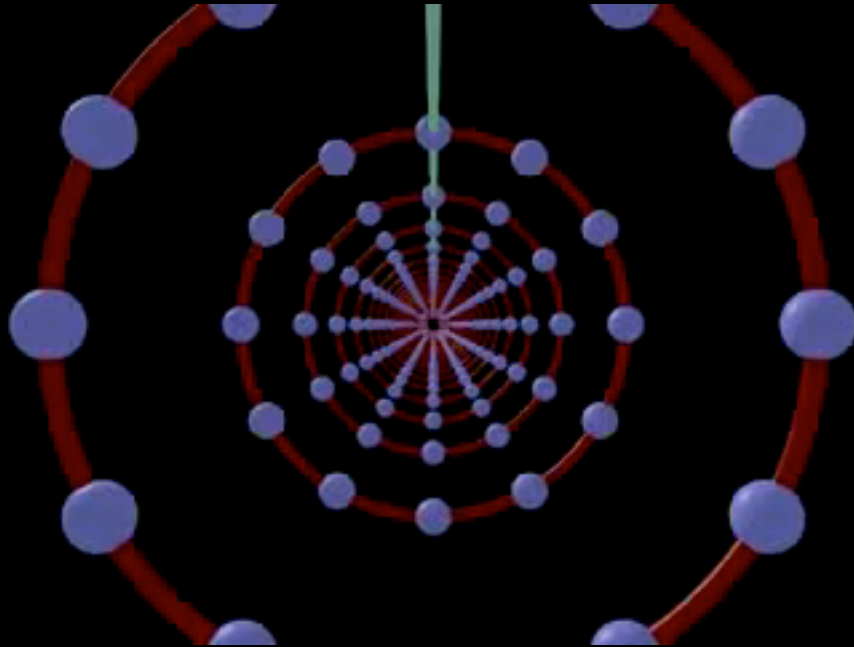
Credit: Michael  
Penn State Schuykill



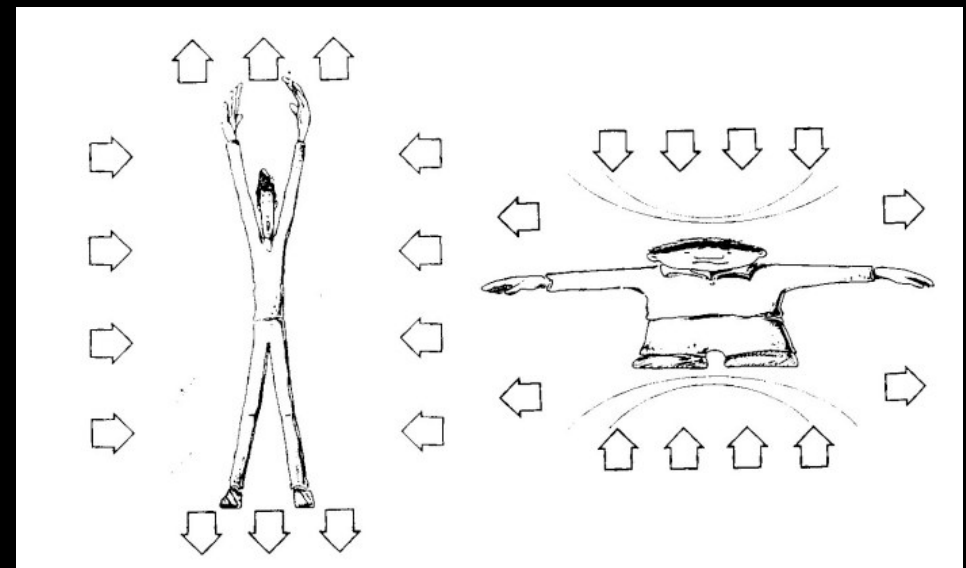
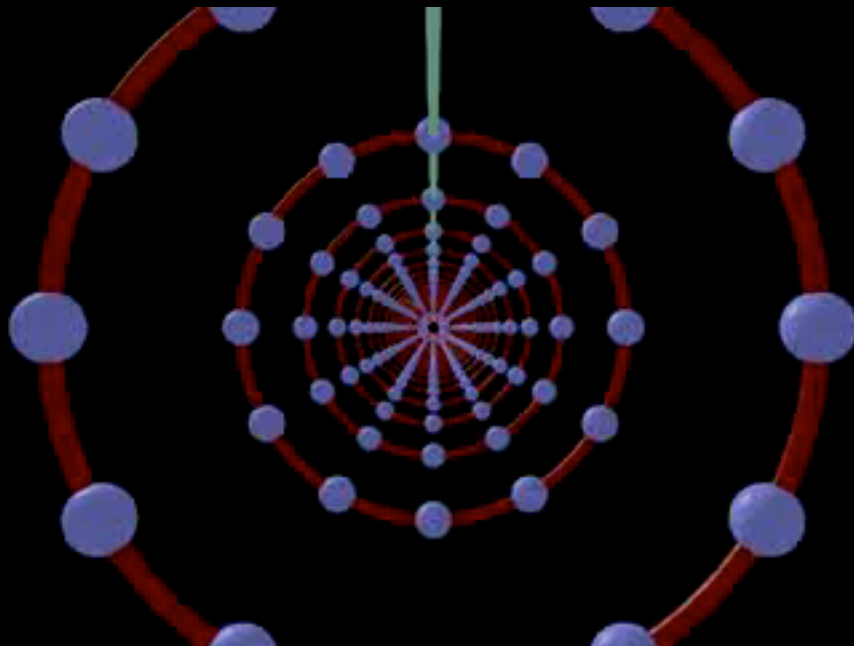
credit: <http://www.inl.infn.it/~auriga/>

# Gravitational Waves

Credit: Michael  
Penn State Schuykill



Credit: Michael  
Penn State Schuykill

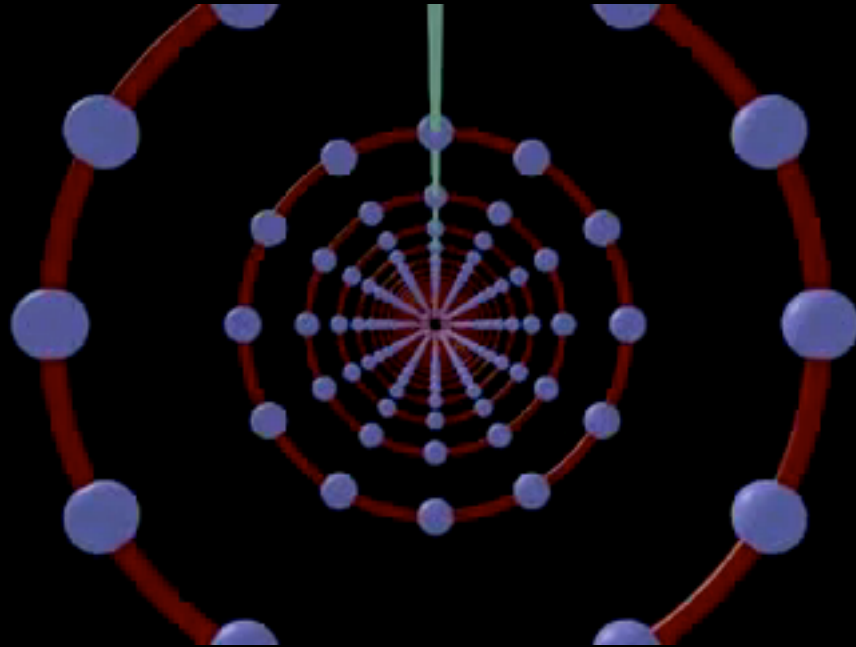


credit: <http://www.inl.infn.it/~auriga/>

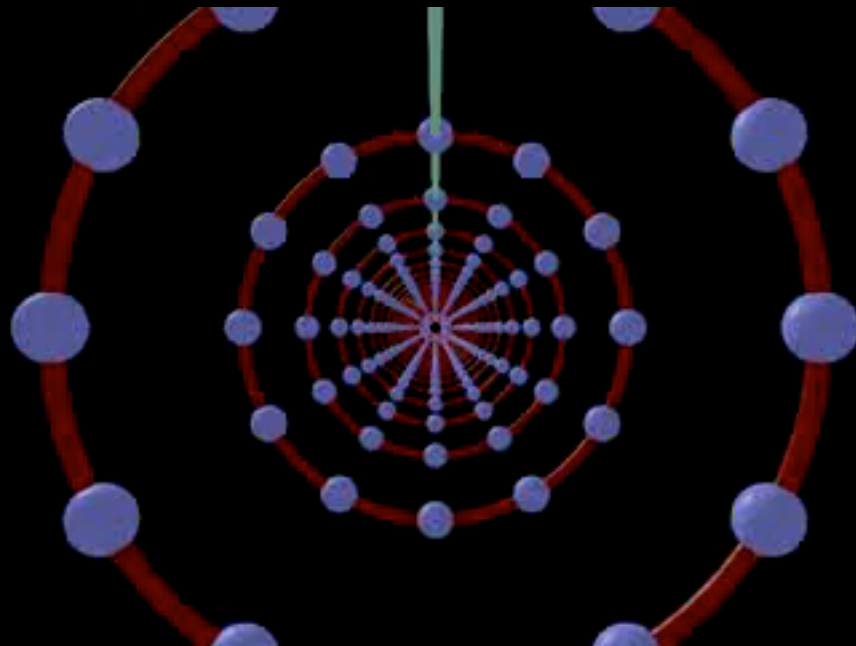


# Gravitational Waves

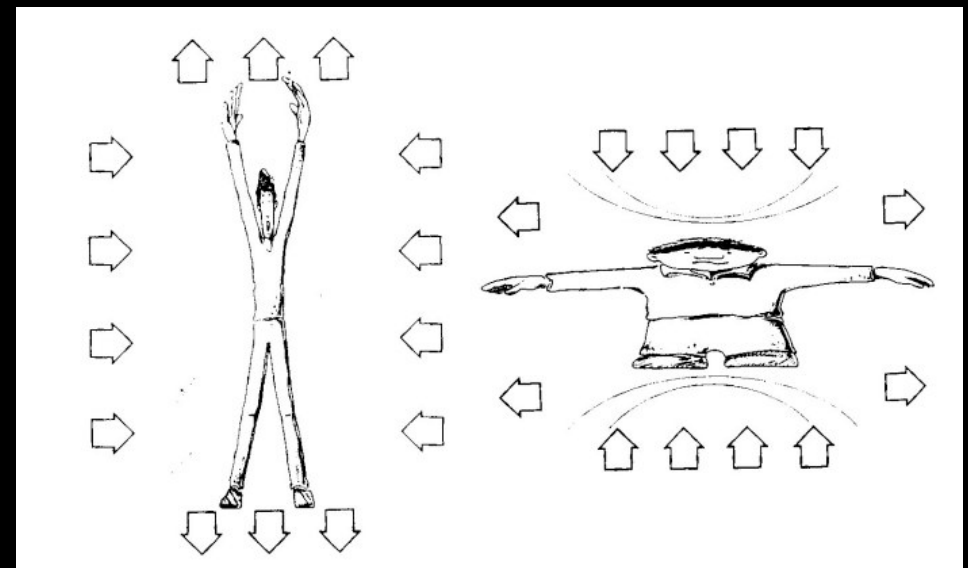
Credit: Michael  
Penn State Schuykill



Credit: Michael  
Penn State Schuykill



Credit: GSFC/D. Berry



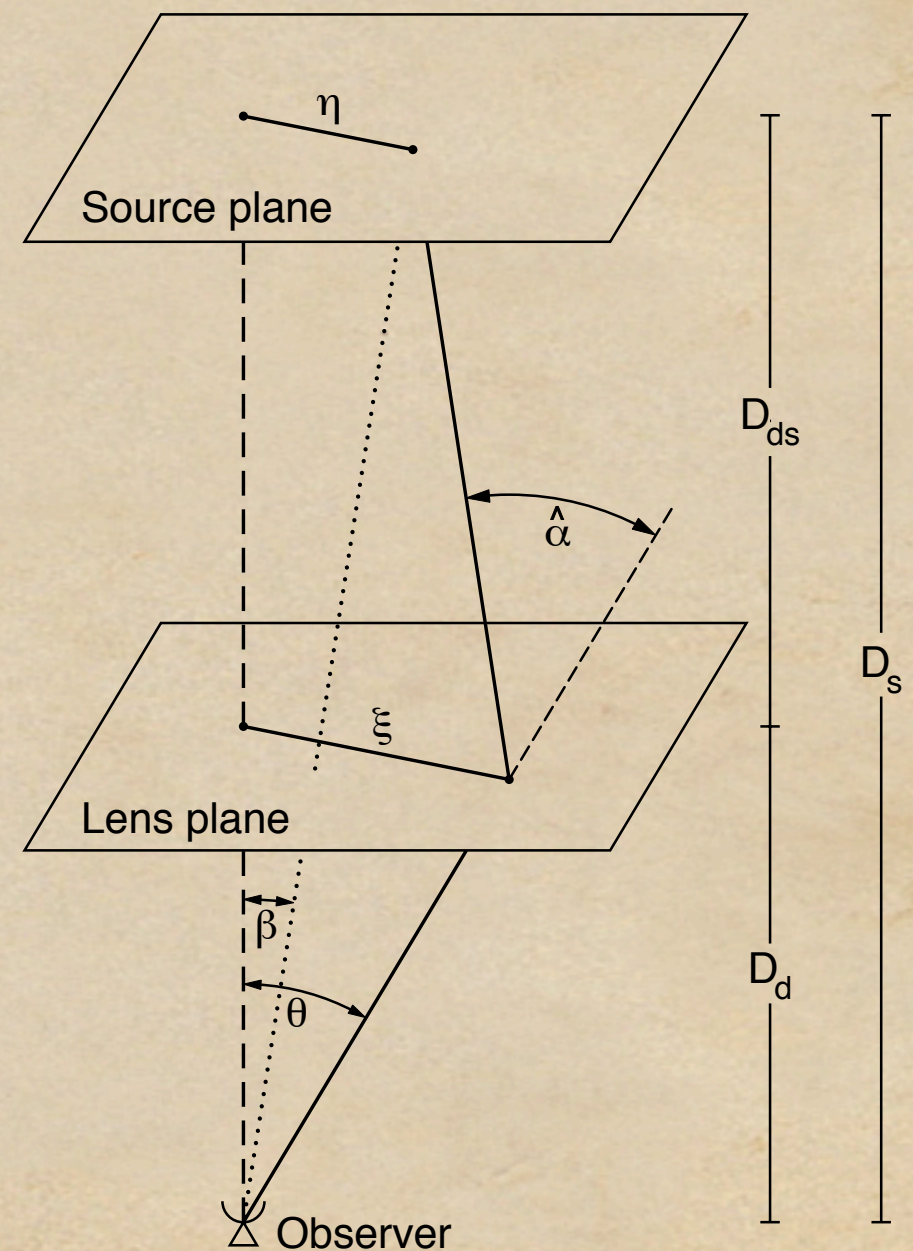
credit: <http://www.inl.infn.it/~auriga/>



# Gravitational Lensing and GW

The Deflection:

$$\vec{\beta} = \vec{\theta} - \vec{\alpha}(\vec{\theta})$$



Credit: Bartelmann and Schneider 2001

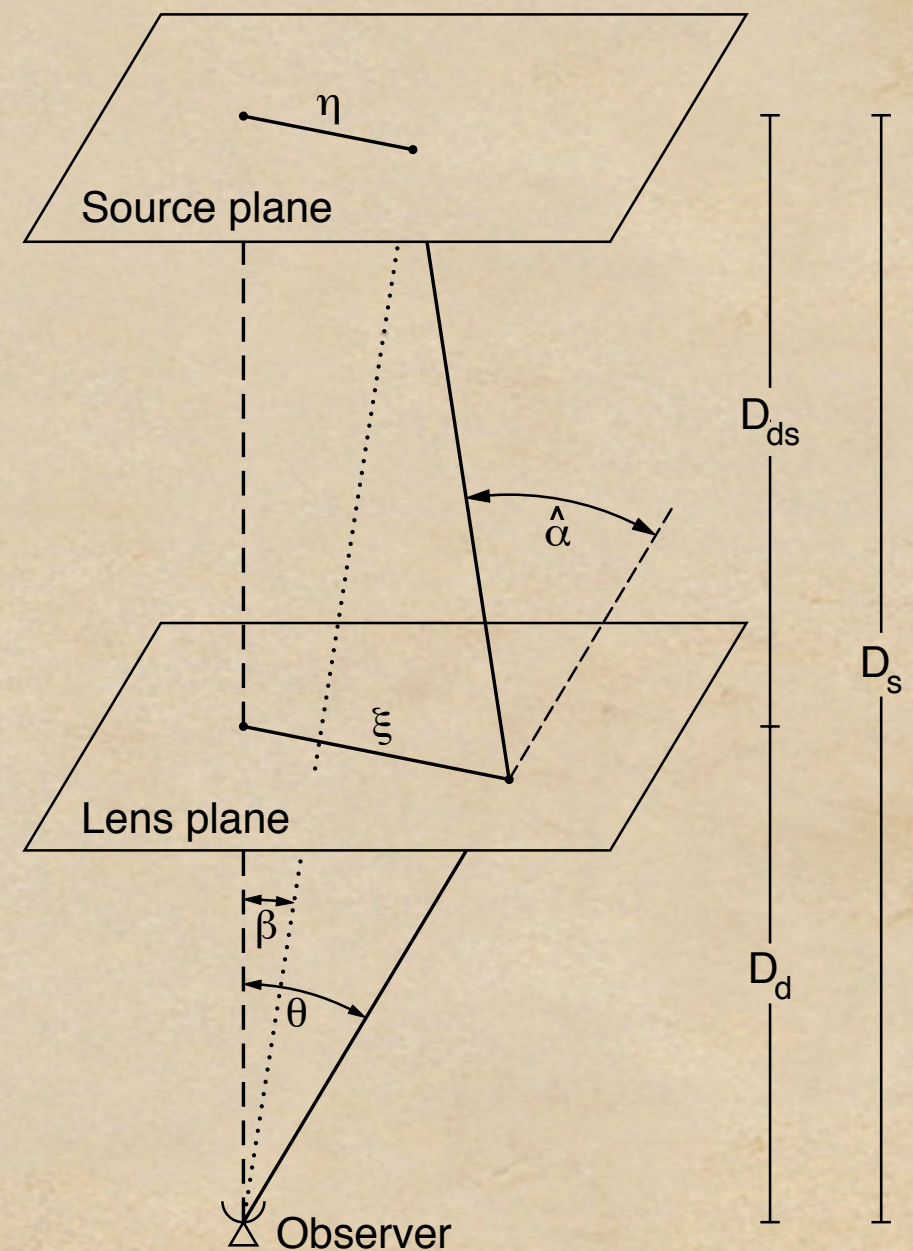


# Gravitational Lensing and GW

The Deflection:

$$\vec{\beta} = \vec{\theta} - \vec{\alpha}(\vec{\theta})$$

$$\vec{\alpha}(\vec{\theta}) = \nabla \phi$$



Credit: Bartelmann and Schneider 2001

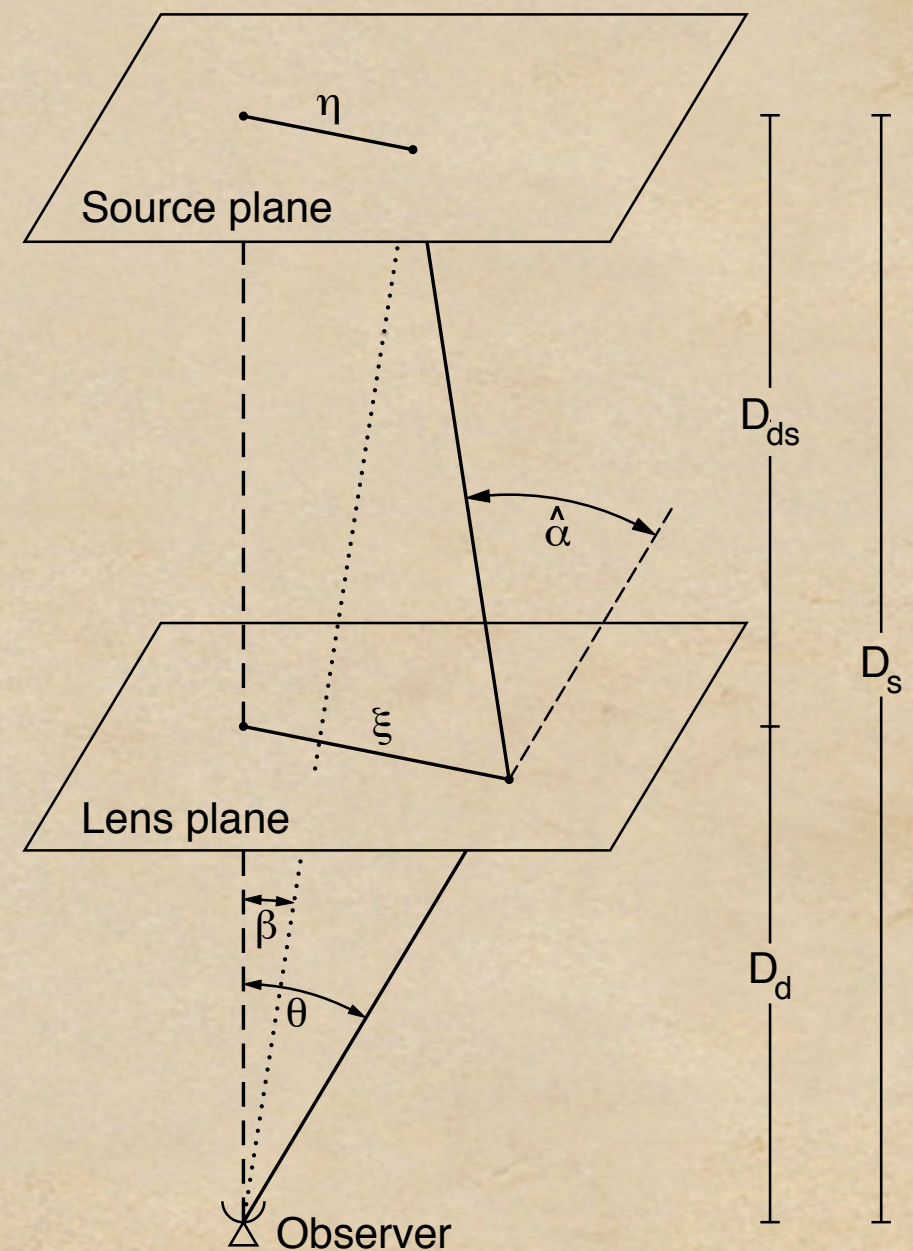


# Gravitational Lensing and GW

The Deflection:

$$\vec{\beta} = \vec{\theta} - \vec{\alpha}(\vec{\theta})$$

$$\mathcal{A}_{ij} = \frac{\partial x_i^S}{\partial x_j^I} \quad \alpha(\vec{\theta}) = \nabla \phi$$



Credit: Bartelmann and Schneider 2001



# Gravitational Lensing and GW

The Deflection:

$$\vec{\beta} = \vec{\theta} - \vec{\alpha}(\vec{\theta})$$

$$\vec{\alpha}(\vec{\theta}) = \nabla \phi$$

$$A_{ij} = \frac{\partial x_i^S}{\partial x_j^I}$$

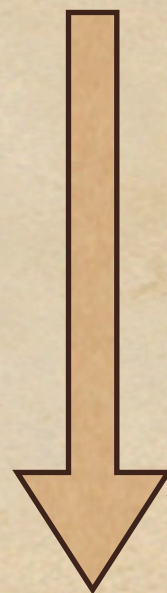
$$= (1 - \kappa)\delta_{ij} - \gamma_{ij} + \omega\epsilon_{ij}$$



trace

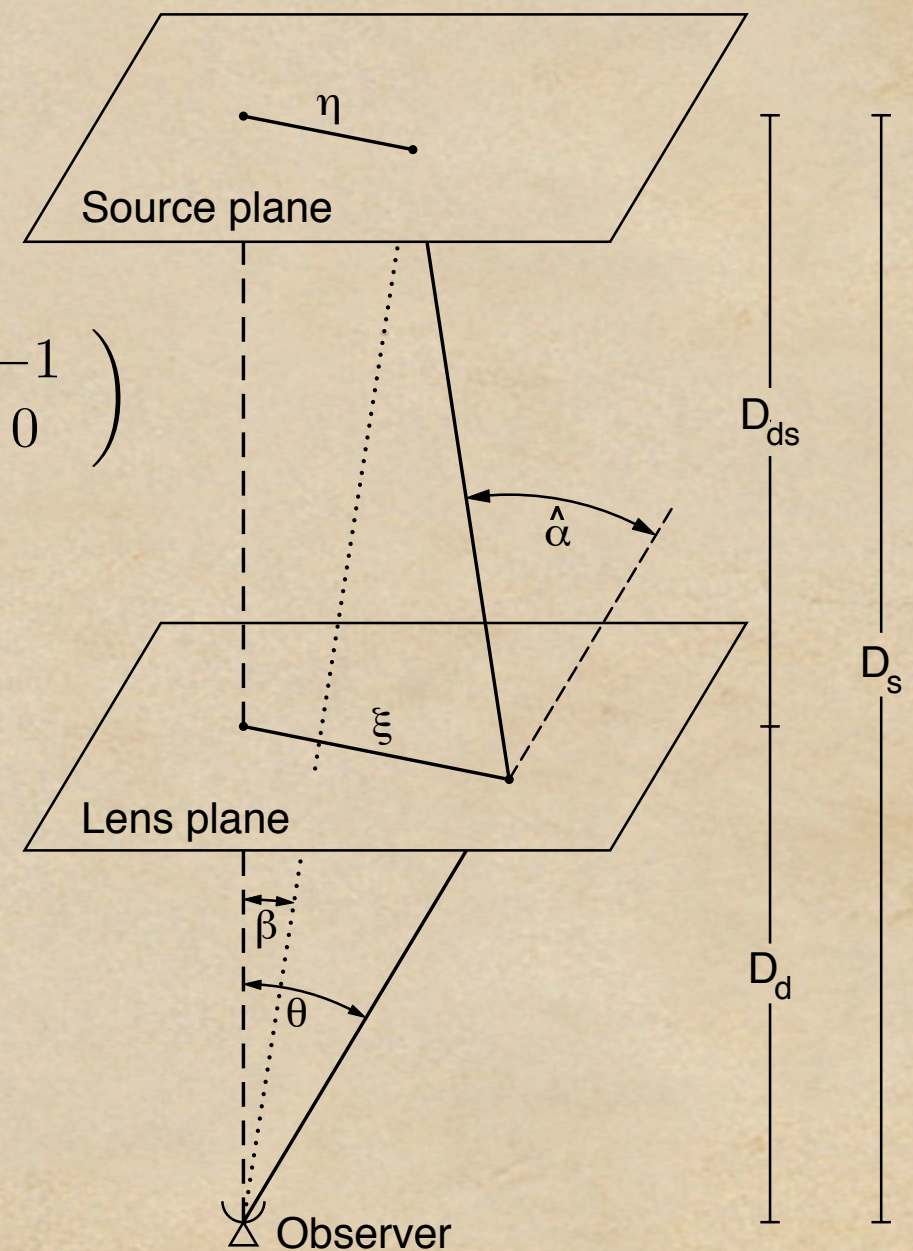


symmetric traceless



antisymmetric rotation

$$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$$



Credit: Bartelmann and Schneider 2001



# Gravitational Lensing and GW

The Deflection:

D.S., P. Serra, A. Cooray, K. Ichiki, D. Baumann,  
PRD, 77, 103515 (2008)

$$\vec{\beta} = \vec{\theta} - \vec{\alpha}(\vec{\theta})$$

$$\alpha(\vec{\theta}) = \nabla \phi$$

$$A_{ij} = \frac{\partial x_i^S}{\partial x_j^I}$$

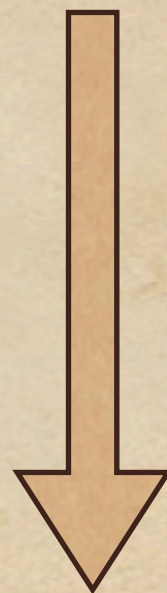
$$= (1 - \kappa)\delta_{ij} - \gamma_{ij} + \omega\epsilon_{ij}$$



trace

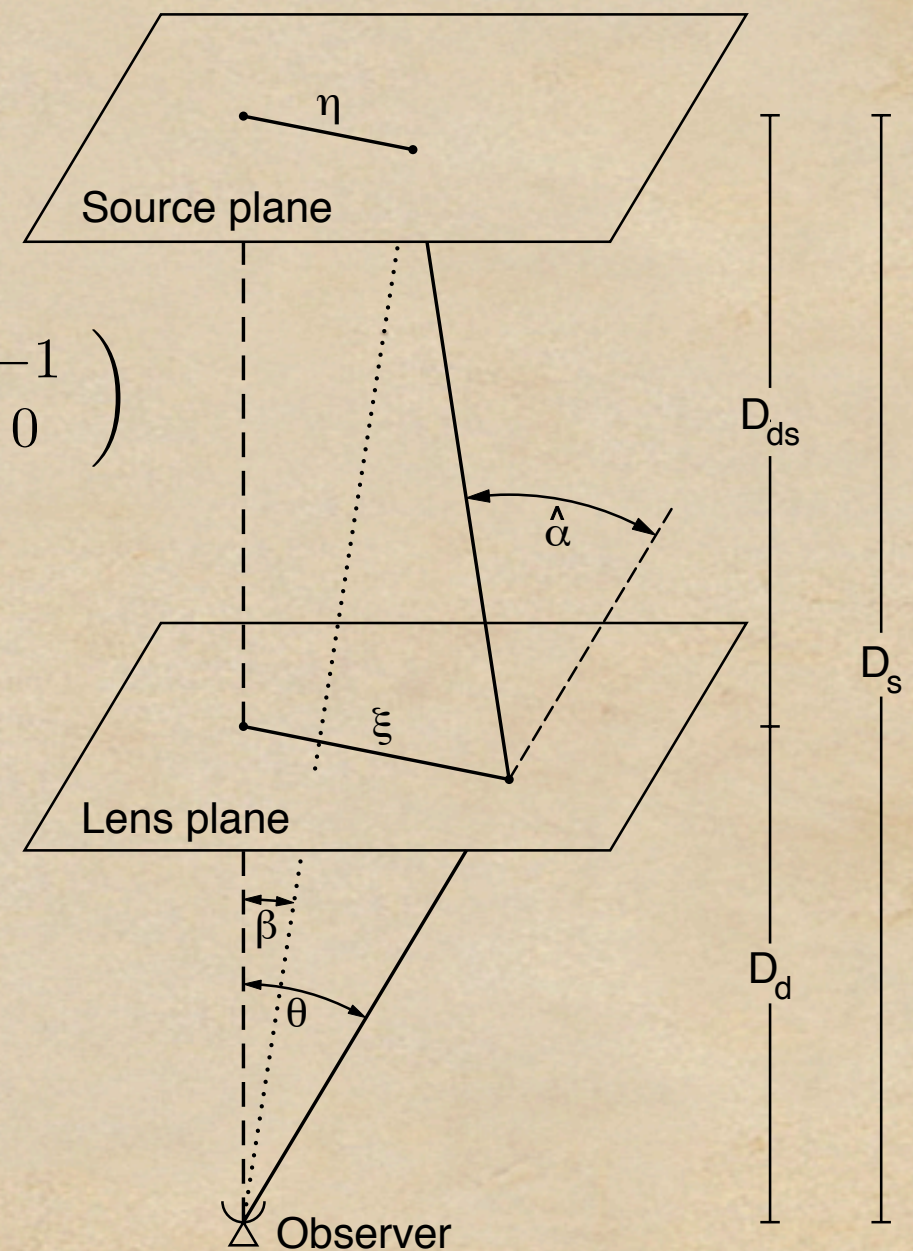


symmetric traceless



antisymmetric rotation

$$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$$



Credit: Bartelmann and Schneider 2001



# At the End of the Hour...

## Dark Energy

- \* Why Pursue Dark Energy?
- \* DE Equation of State (EOS)
- \* DE from SNe Ia ++
- \* Beware of Systematics
  - Two Population Model
  - Gravitational Lensing

## CMB Bispectrum

- \* Why Non-Gaussianity?
- \* Why in CMB Bispectrum?
- \* The  $f_{NL}$
- \* WL of CMB Bispectrum
  - ⊗ Analytical Sketch
  - ⊗ Numerical Results



# At the End of the Hour...

## Dark Energy

- \* Why Pursue Dark Energy?
- \* DE Equation of State (EOS)
- \* DE from SNe Ia ++
- \* Beware of Systematics
  - Two Population Model
  - Gravitational Lensing

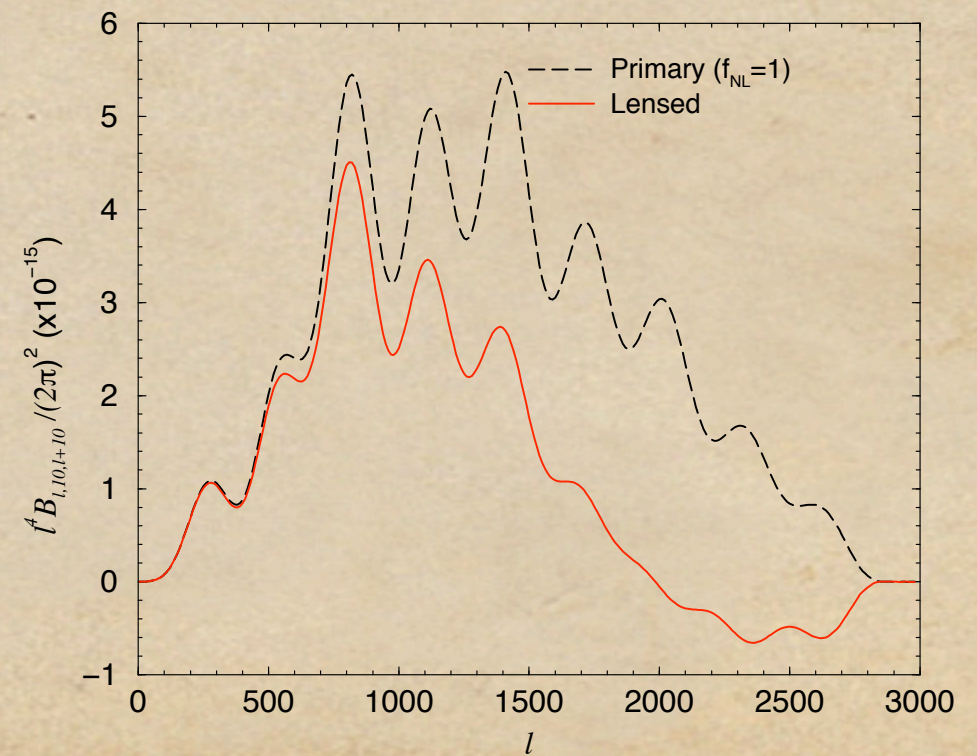
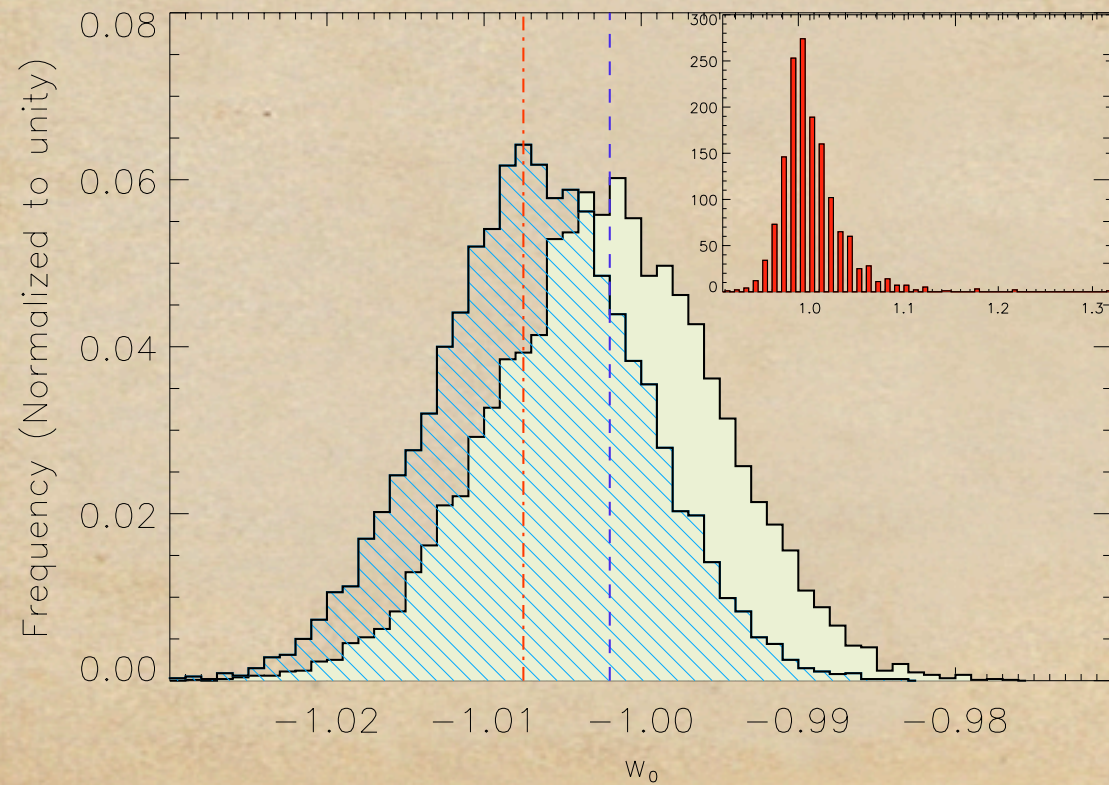
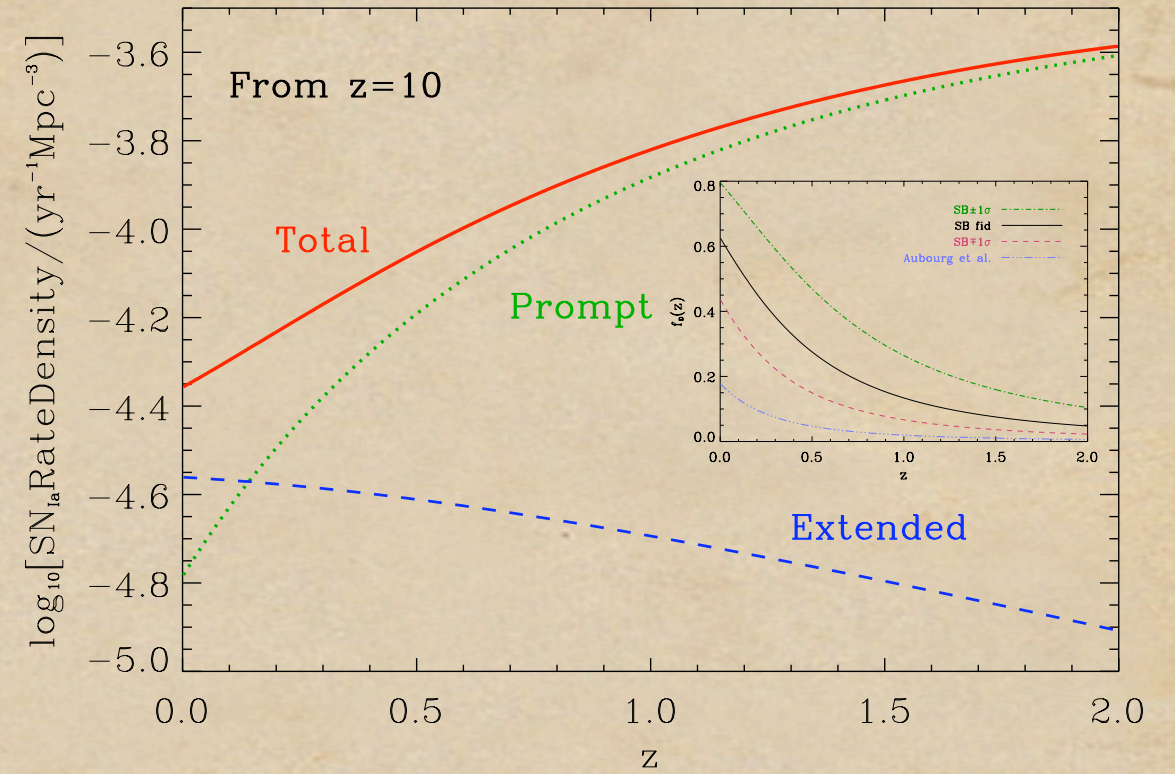
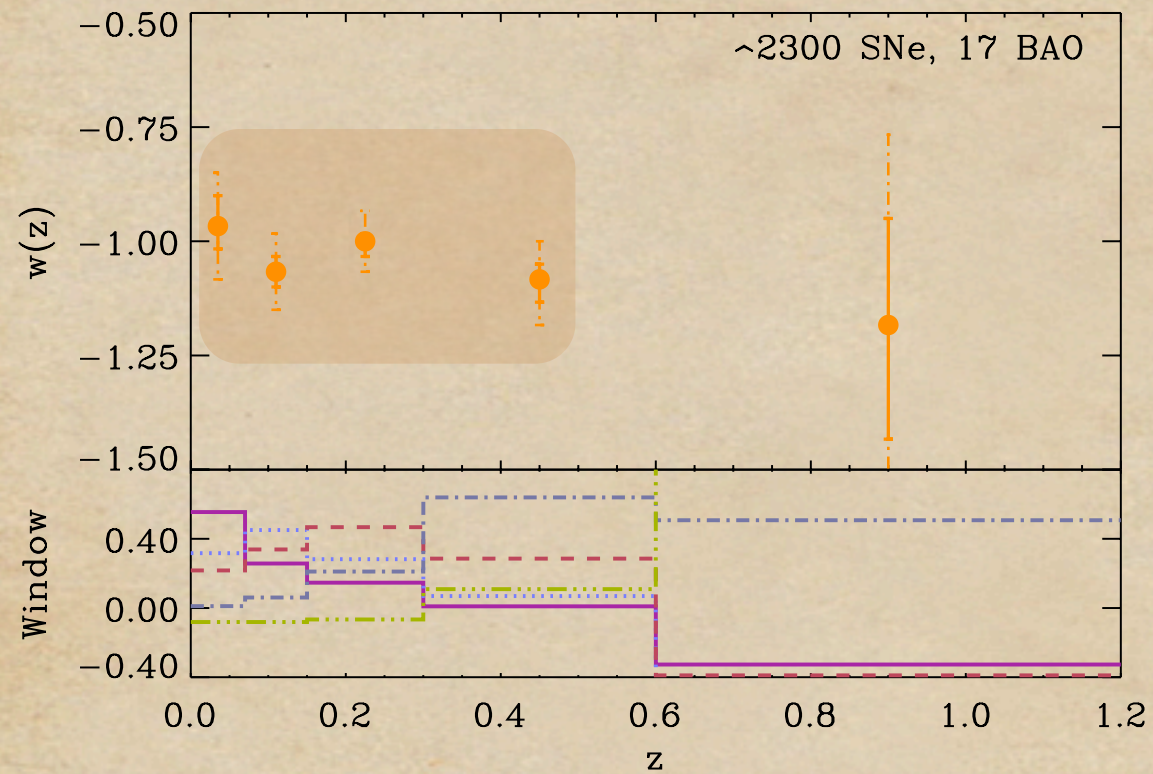
## CMB Bispectrum

- \* Why Non-Gaussianity?
- \* Why in CMB Bispectrum?
- \* The  $f_{NL}$
- \* WL of CMB Bispectrum
  - ⊗ Analytical Sketch
  - ⊗ Numerical Results

## Summary



# Summary







T H A N K Y O U

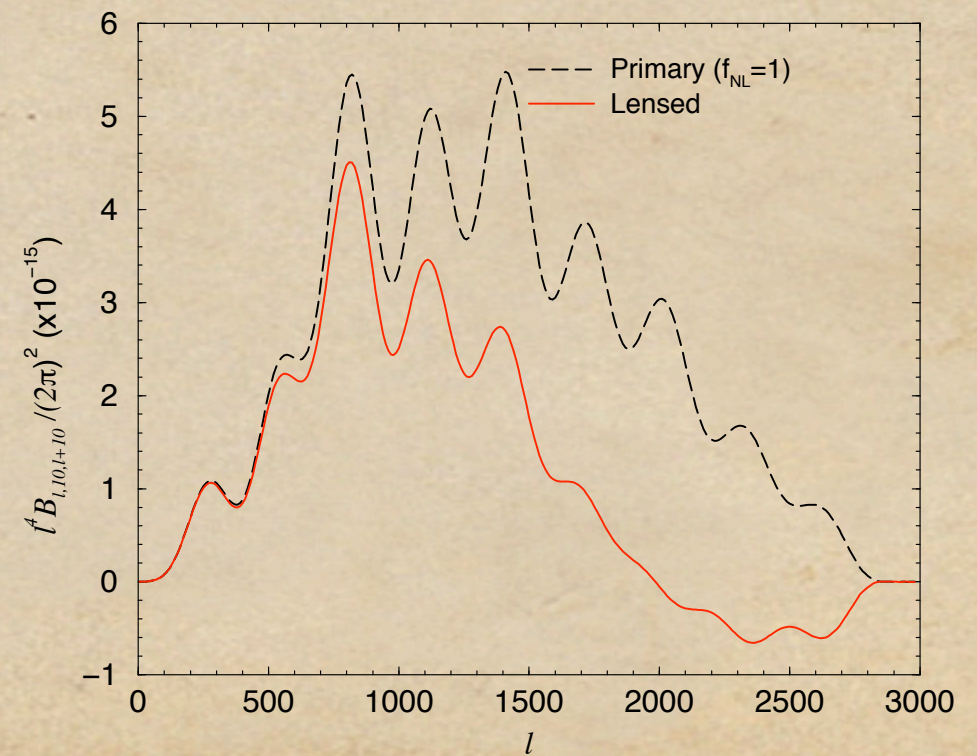
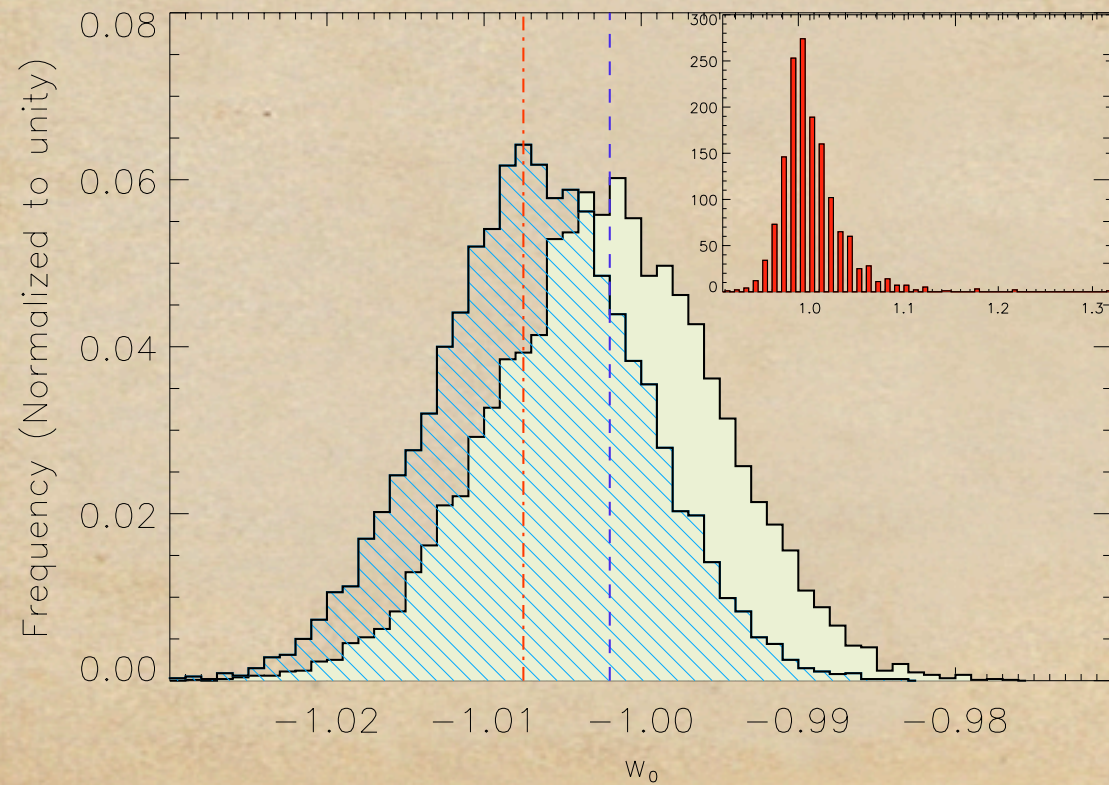
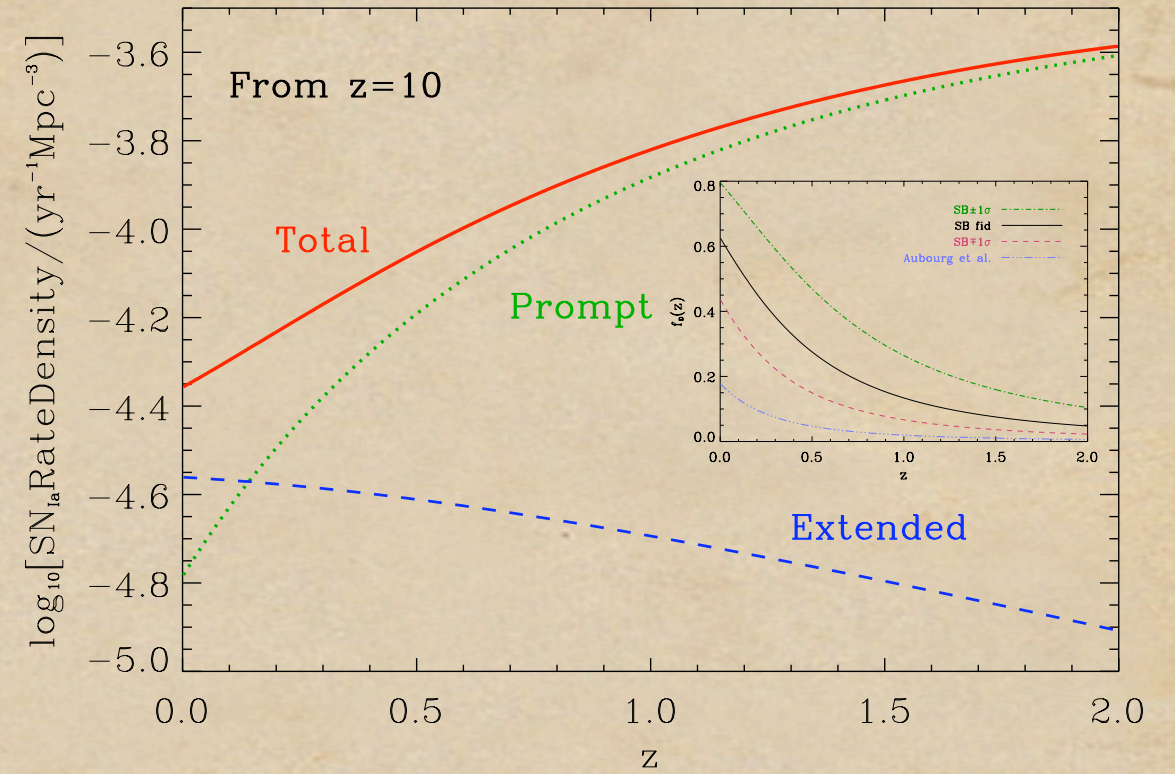
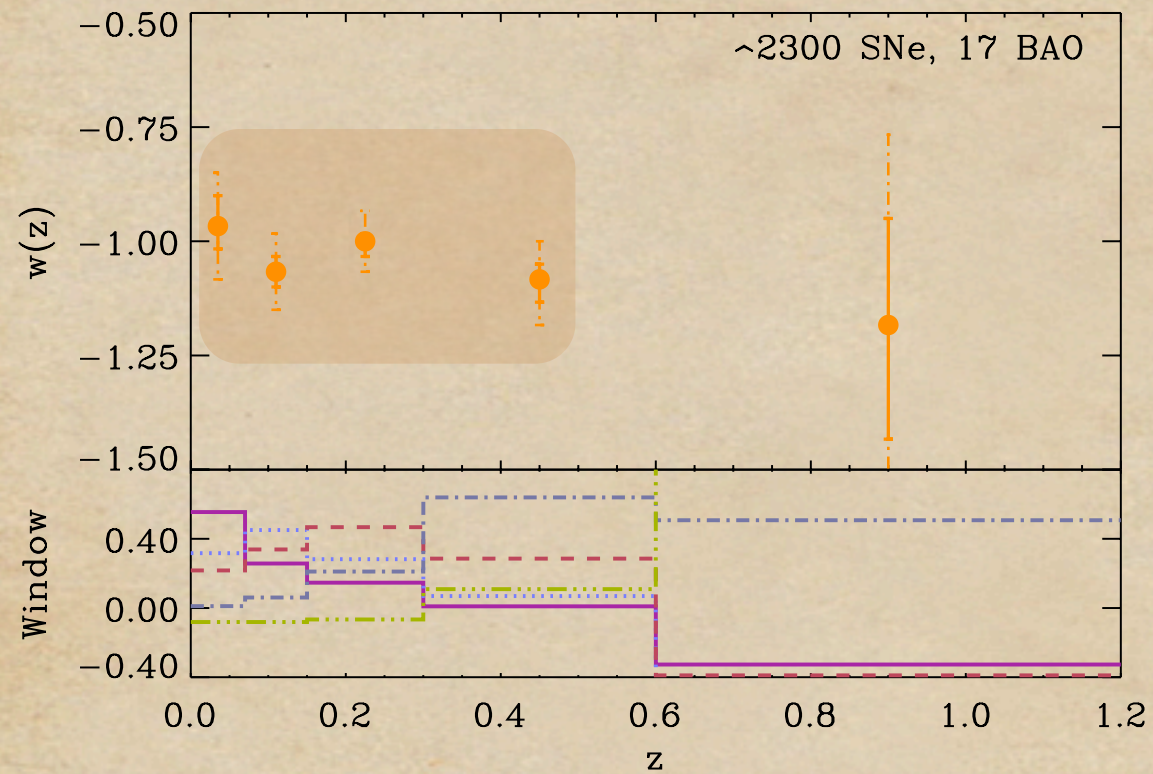
D S A R K A R . O R G

[dulissa.wordpress.com](http://dulissa.wordpress.com)

*DSARKAR.ORG*



# Summary





# Summary

- \* We have shown that the next-generation surveys will be able to constrain the dark energy equation of state in three or more independent redshift bins to better than 10%.
- \* We have found that a post-calibration shift in the standard candle brightness between delayed and prompt SNe can introduce bias in the best-fit dark energy parameters. By controlling the magnitude of any resulting two-population difference to better than 0.025 mag, the bias can be kept under  $1-\sigma$  for a JDEM-like survey without significantly degrading the accuracy of the dark energy measurements.
- \* For a JDEM-like survey, we have shown that the bias in the equation of state measurement is less than a percent level (so long as all the SNe are used in the Hubble diagram).
- \* We have discussed the lensing modification to the CMB bispectrum and demonstrated that lensing leads to an overall decrease in the amplitude of the primary bispectrum at multipoles of interest between 100 and 2000 through additional smoothing introduced by lensing. For a high resolution experiment such as Planck, the lensing modification to the bispectrum must be properly included when attempting to estimate the primordial non-Gaussianity. An ignorance will bias the estimate at the level of 30%.



# Summary

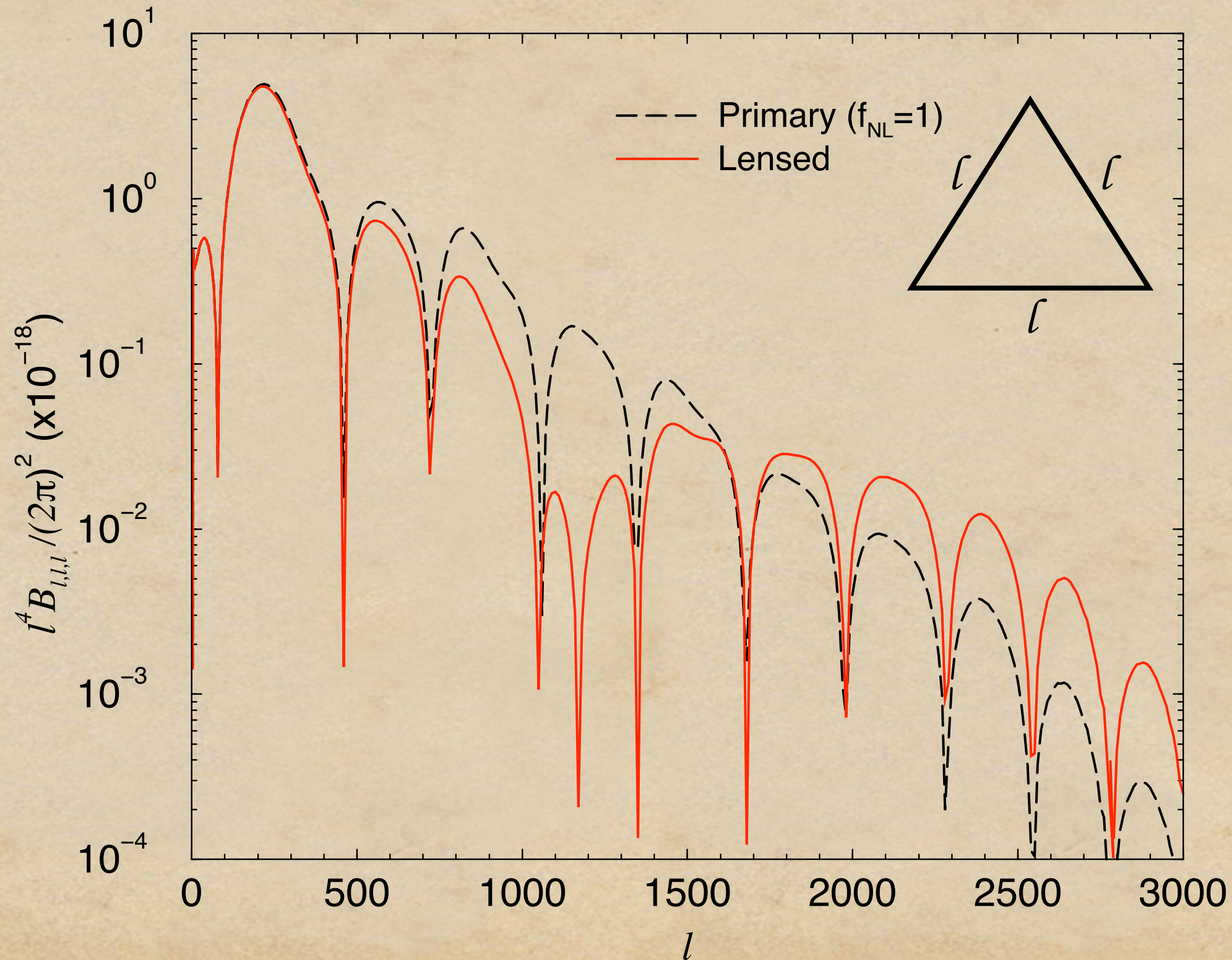
- \* We have shown that the next-generation surveys will be able to constrain the dark energy equation of state in three or more independent redshift bins to better than 10%.
- \* We have found that a post-calibration shift in the standard candle brightness between delayed and prompt SNe can introduce bias in the best-fit dark energy parameters. By controlling the magnitude of any resulting two-population difference to better than 0.025 mag, the bias can be kept under  $1-\sigma$  for a JDEM-like survey without significantly degrading the accuracy of the dark energy measurements.
- \* For a JDEM-like survey, we have shown that the bias in the equation of state measurement is less than a percent level (so long as all the SNe are used in the Hubble diagram).
- \* We have discussed the lensing modification to the CMB bispectrum and demonstrated that lensing leads to an overall decrease in the amplitude of the primary bispectrum at multipoles of interest between 100 and 2000 through additional smoothing introduced by lensing. For a high resolution experiment such as Planck, the lensing modification to the bispectrum must be properly included when attempting to estimate the primordial non-Gaussianity. An ignorance will bias the estimate at the level of 30%.



XTRA SLIDES

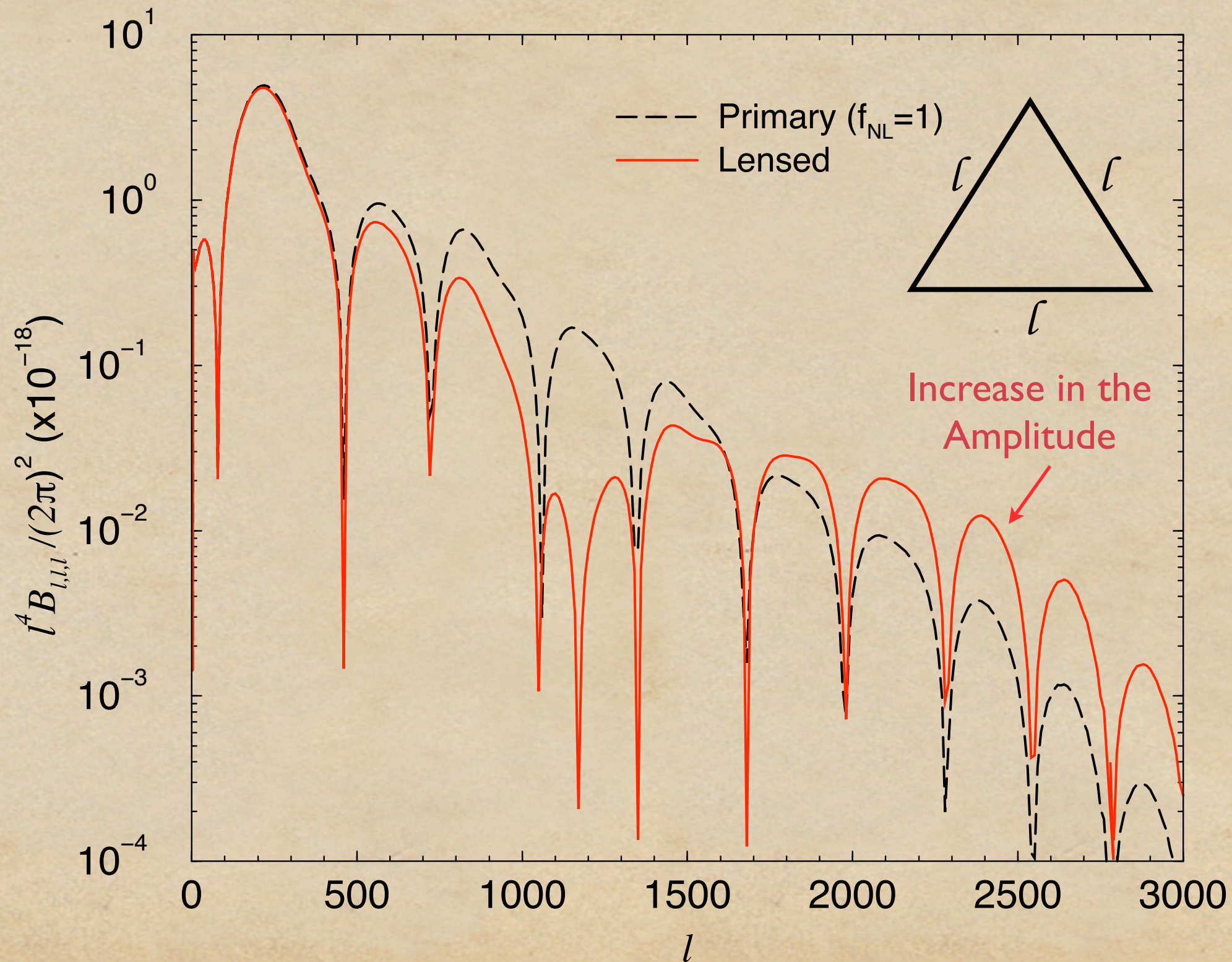


# CMB Bispectrum of the equilateral case



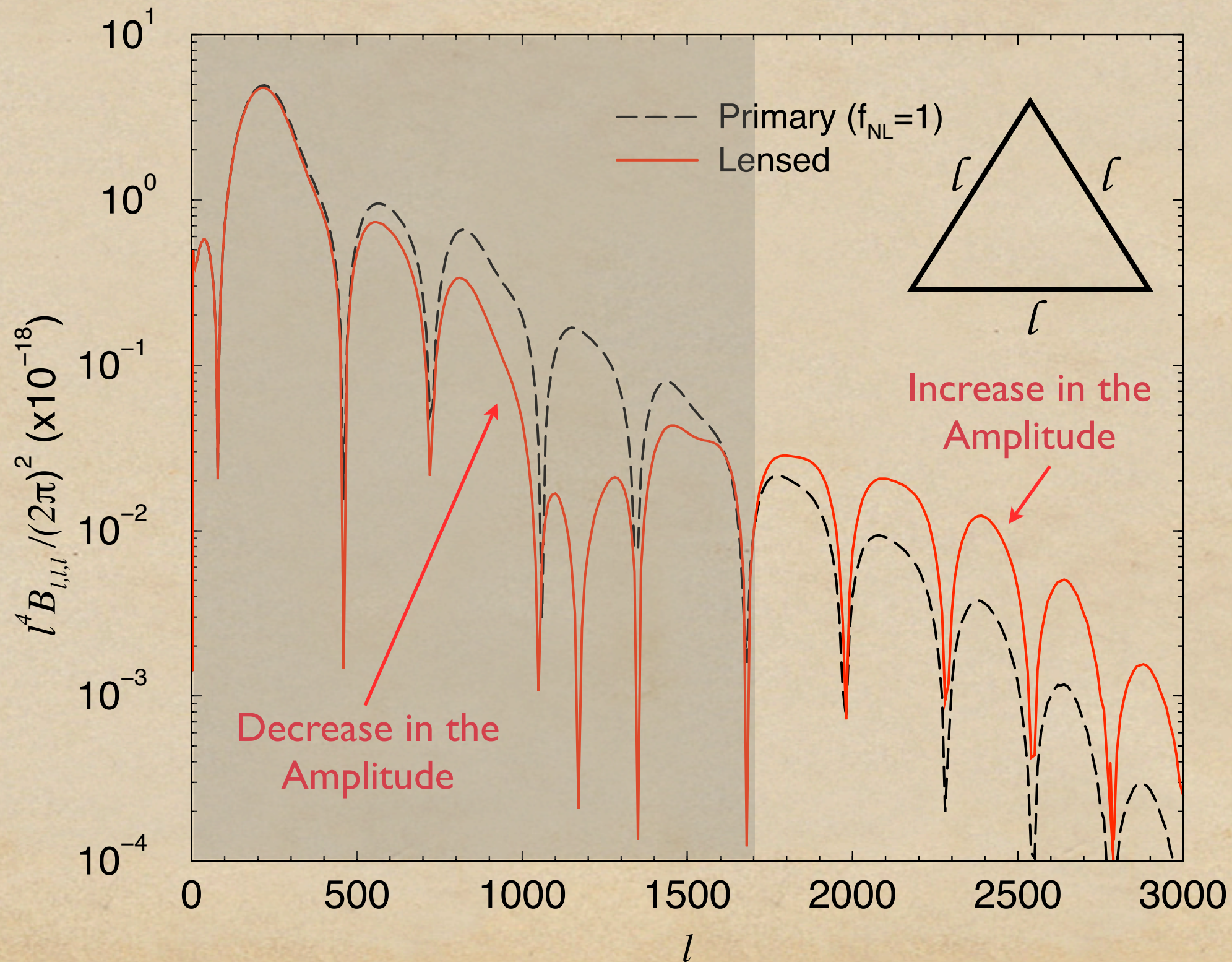


# CMB Bispectrum of the equilateral case



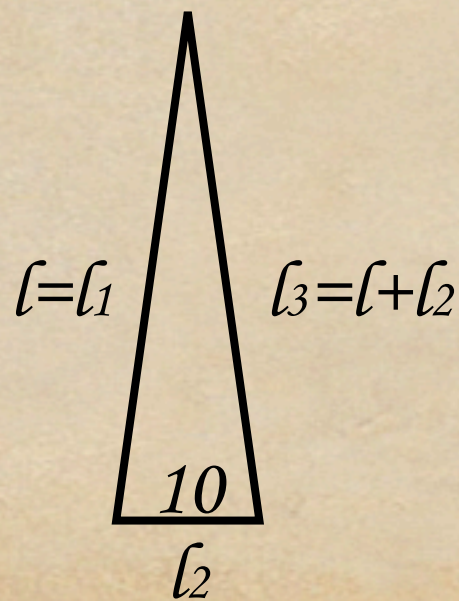
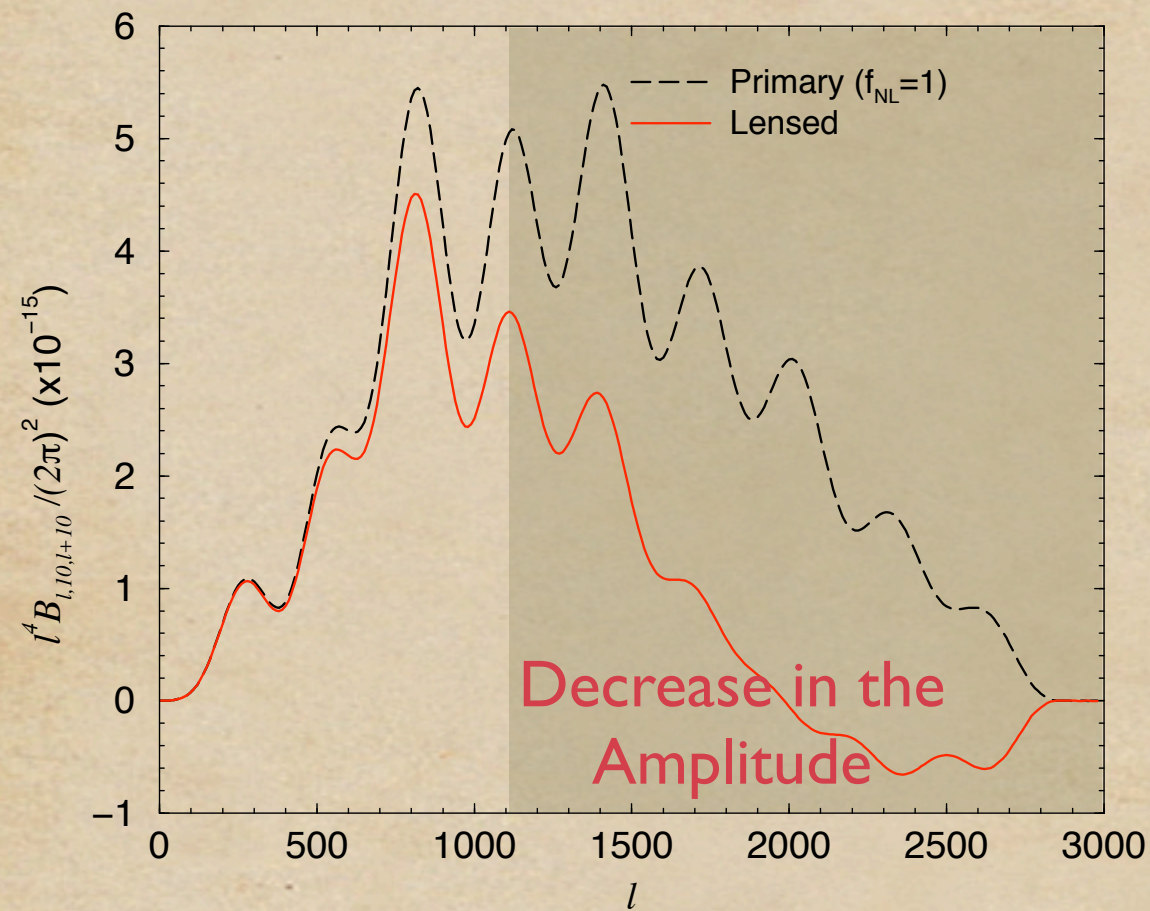


# CMB Bispectrum of the equilateral case



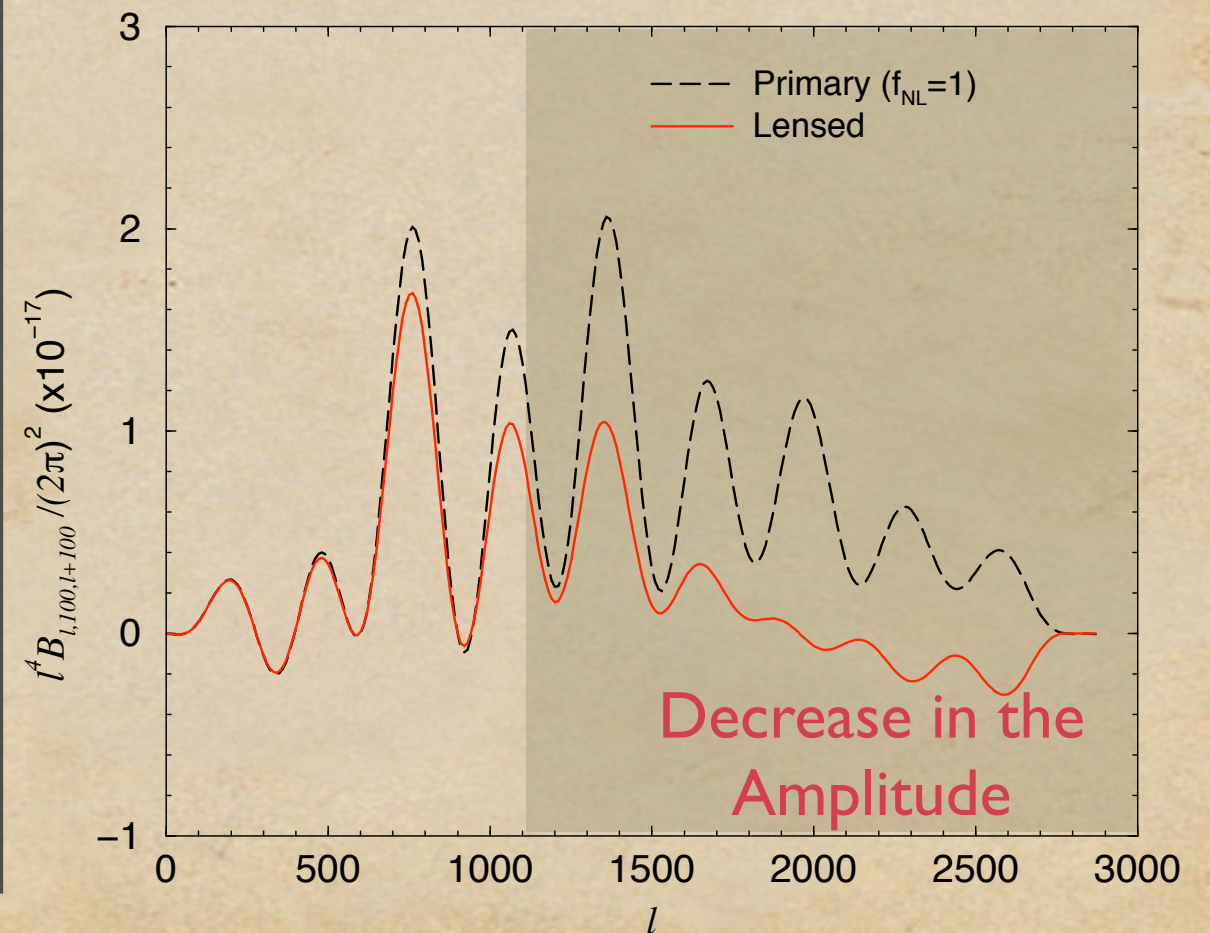
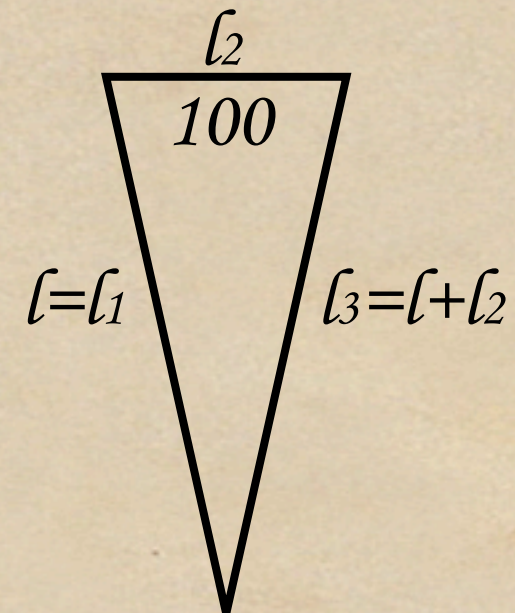
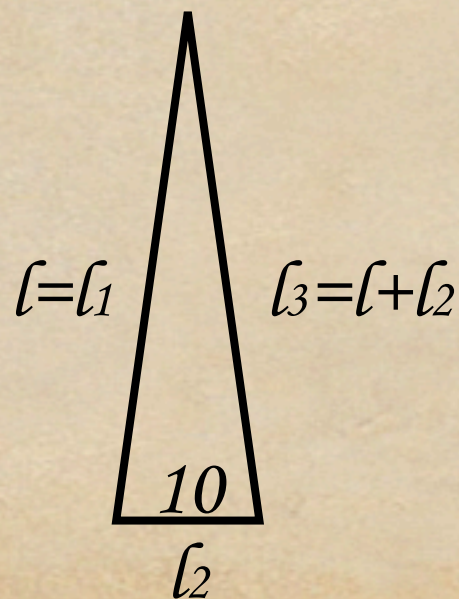
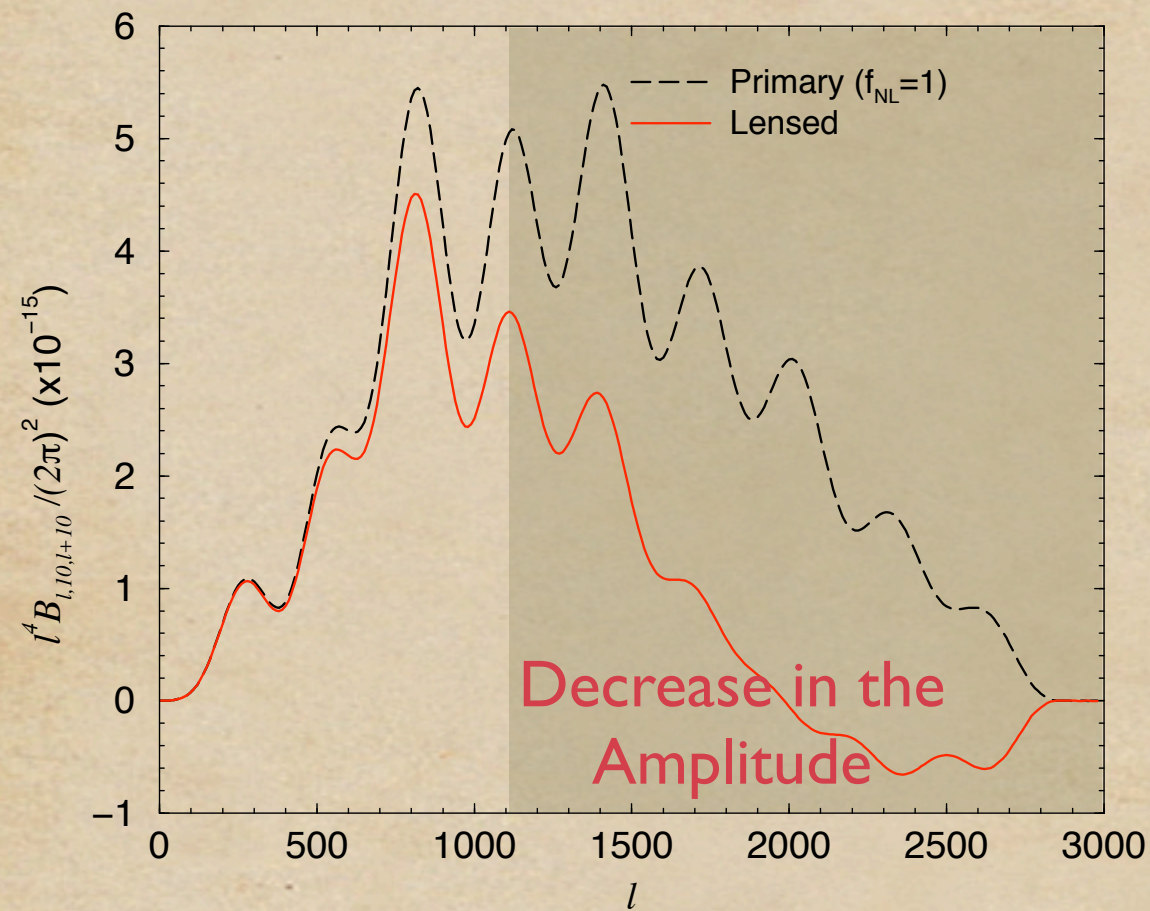


# CMB Bispectrum of the squeezed case(s)



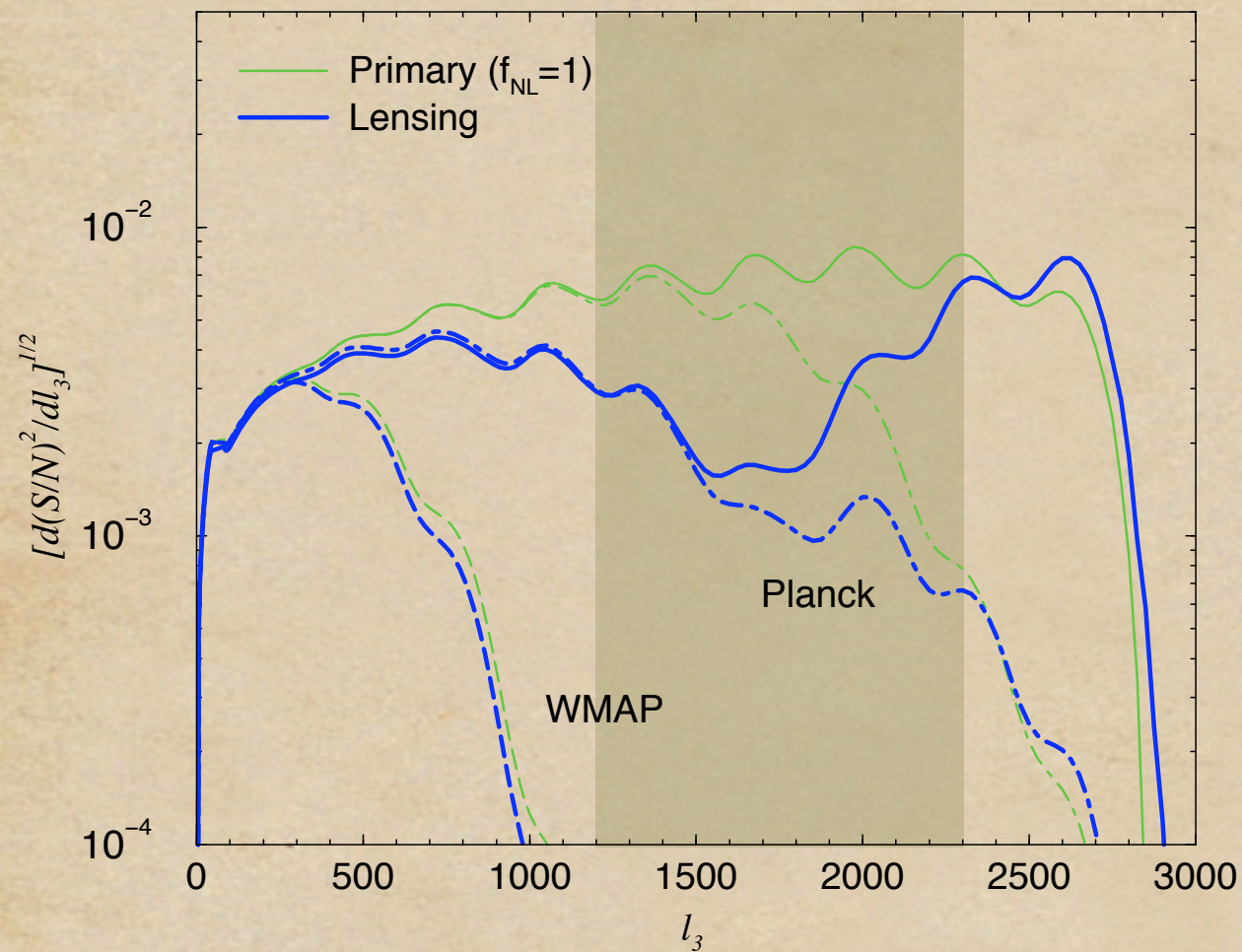


# CMB Bispectrum of the squeezed case(s)





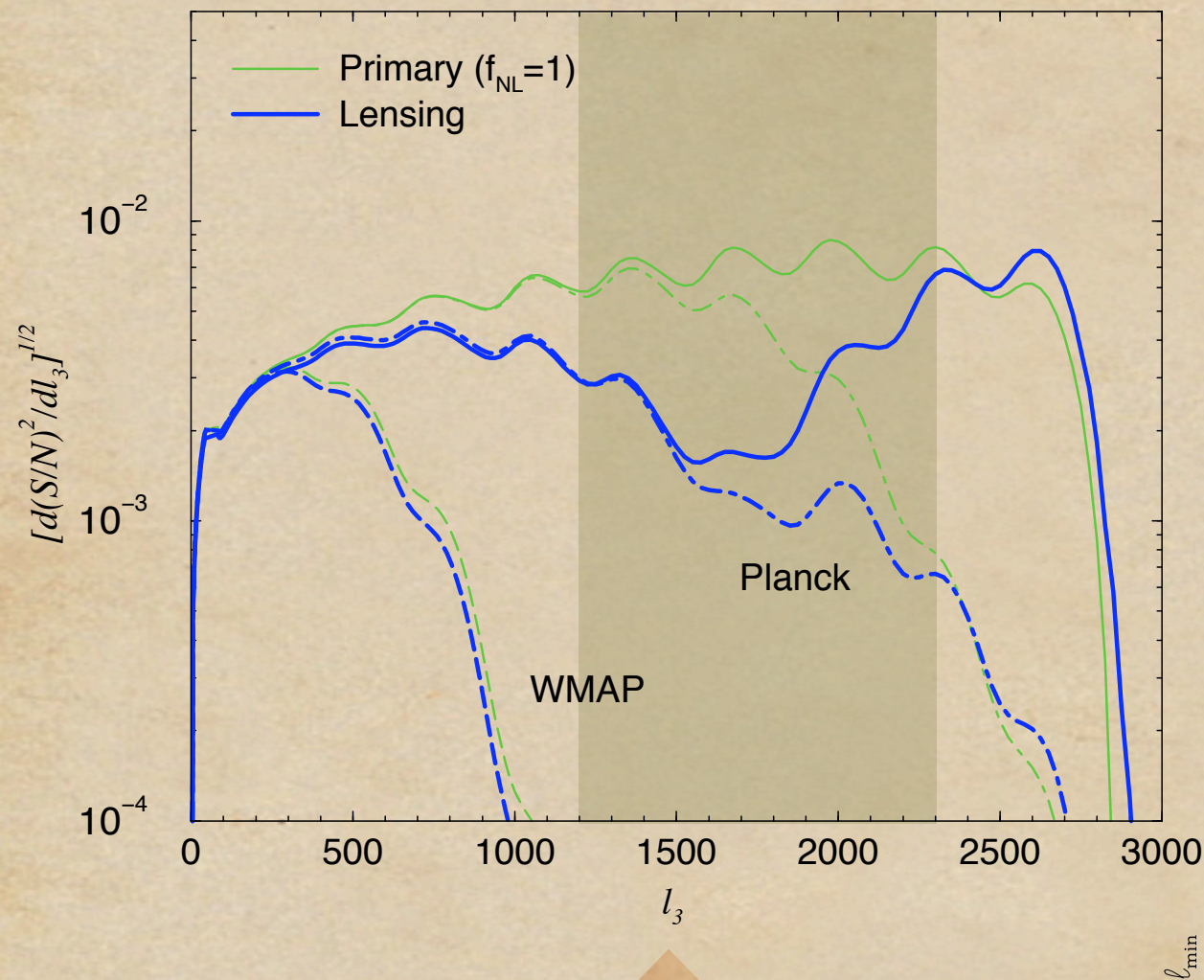
# Reduction in the S/N due to Lensing



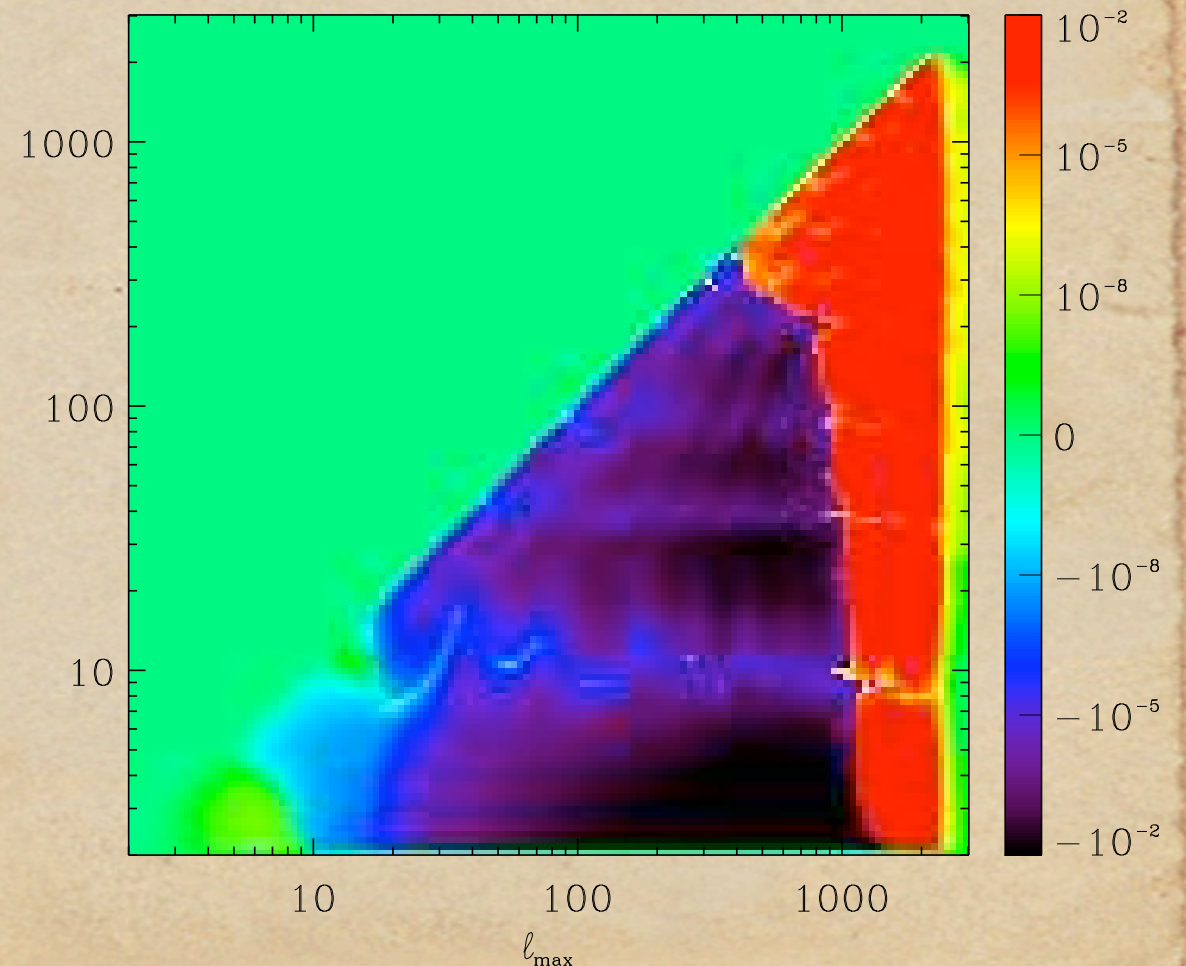
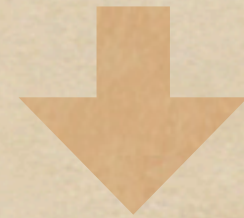
$$\left(\frac{S}{N}\right)^2 = \sum_{l_1 l_2 l_3} \frac{(B_{l_1 l_2 l_3}^\Theta)^2}{6C_{l_1}^{tot} C_{l_2}^{tot} C_{l_3}^{tot}}$$



# Reduction in the S/N due to Lensing



$$\frac{d \left[ \left( \frac{S}{N} \right)_{\text{lensed}}^2 - \left( \frac{S}{N} \right)_{\text{unlensed}}^2 \right]}{d \log l_{\text{max}} d \log l_{\text{min}}}$$



$$\left( \frac{S}{N} \right)^2 = \sum_{l_1 l_2 l_3} \frac{(B_{l_1 l_2 l_3}^\Theta)^2}{6 C_{l_1}^{\text{tot}} C_{l_2}^{\text{tot}} C_{l_3}^{\text{tot}}}$$



# Primary CMB Bispectrum

The CMB Temperature Perturbation in the Sky:

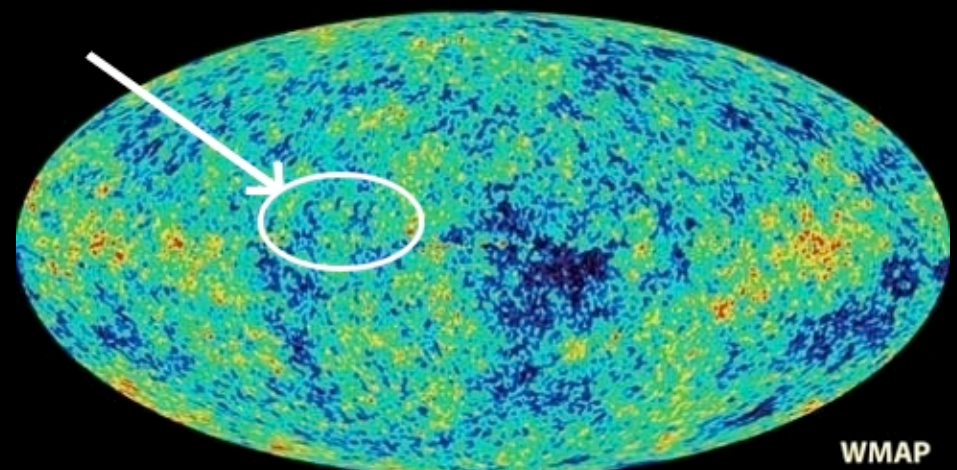
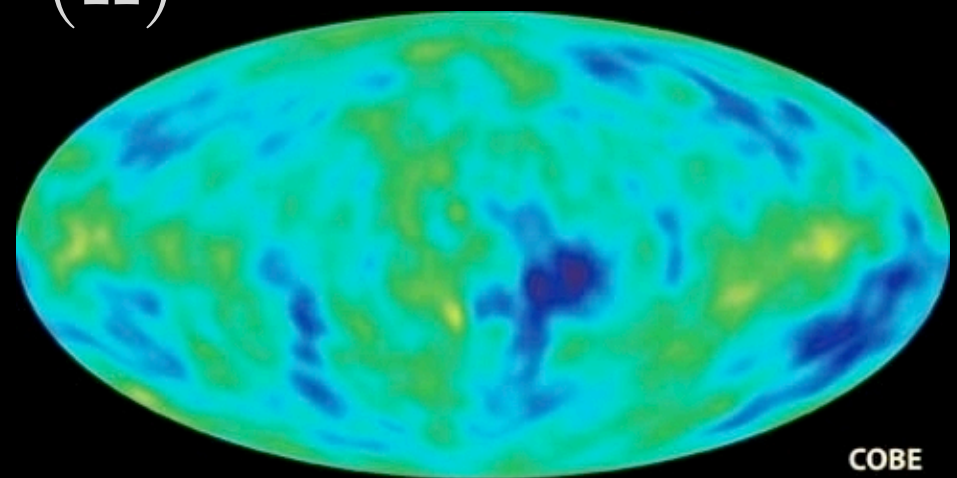
$$\Theta(\hat{\mathbf{n}}) \equiv \frac{\Delta T(\hat{\mathbf{n}})}{T} = \sum_{lm} \Theta_{lm} Y_l^m(\hat{\mathbf{n}})$$

Power Spectrum:

$$\langle \Theta_{lm} \Theta_{l'm'} \rangle = \delta_{l,l'} \delta_{m,m'} C_l^{\Theta\Theta}$$

Angular Bispectrum:

$$\langle \Theta_{l_1 m_1} \Theta_{l_2 m_2} \Theta_{l_3 m_3} \rangle = \begin{pmatrix} l_1 & l_2 & l_3 \\ m_1 & m_2 & m_3 \end{pmatrix} B_{l_1 l_2 l_3}^{\Theta}$$





# Primordial Non-Gaussianity: Primary CMB Bispectrum

## Gaussian Quantum Fluctuation

Falk et al. (1993)  $\downarrow \delta\phi \sim g_{\delta\phi} \left( \eta + m_{pl}^{-1} f_{\eta} \eta^2 \right) \downarrow$  Starobinsky (1986)  
Gangui et al. (1994)

## Non-Gaussian Inflation Fluctuation

$\downarrow \Phi \sim m_{pl}^{-1} g_{\Phi} \left( \delta\phi + m_{pl}^{-1} f_{\delta\phi} \delta\phi^2 \right) \downarrow$  Salopek & Bond  
(1990)

## Non-Gaussian Curvature Perturbation

$\downarrow \frac{\Delta T}{T} \sim g_T \left( \Phi + f_{\Phi} \Phi^2 \right) \downarrow$  Pyne & Carroll (1996)

## Non-Gaussian CMB Anisotropy



# A Word or Two on Weak Lensing


## Lensing Potential (under the Born approximation)


$$\phi(\hat{\mathbf{n}}) = -2 \int_0^{r_s} dr' \frac{d_A(r_s - r')}{d_A(r_s) d_A(r')} \Phi(\mathbf{x}(\hat{\mathbf{n}}), r')$$

## Lensing Power Spectrum

$$\phi(\hat{\mathbf{n}}) = \sum_{lm} \phi_{lm} Y_l^m(\hat{\mathbf{n}}) \quad \langle \phi_{lm} \phi_{l'm'} \rangle = \delta_{l,l'} \delta_{m,m'} C_l^\phi$$

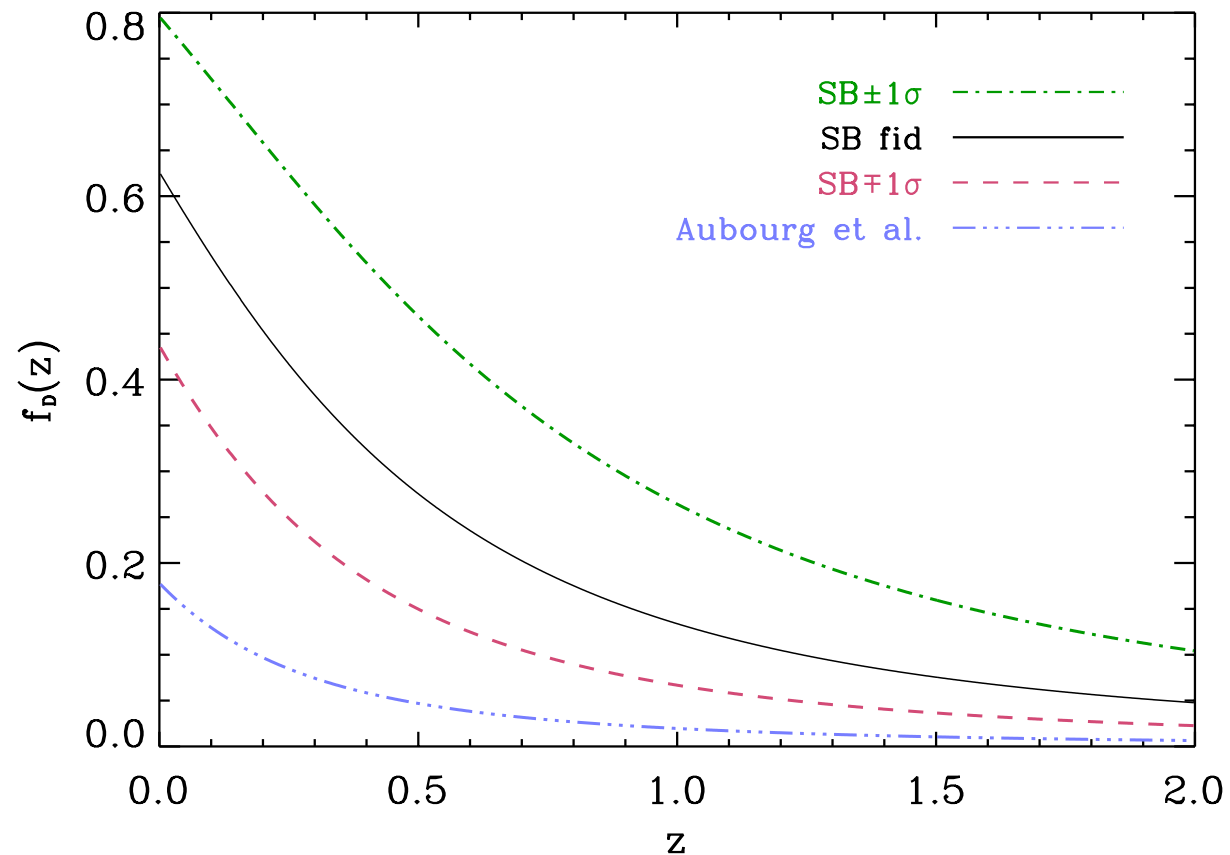
$$C_l^\phi = \frac{2}{\pi} \int k^2 dk P_\Phi(k) [I_l^{len}(k)]^2$$


$$I_l^{len}(k) = \int dr W^{len}(r) j_l(kr)$$

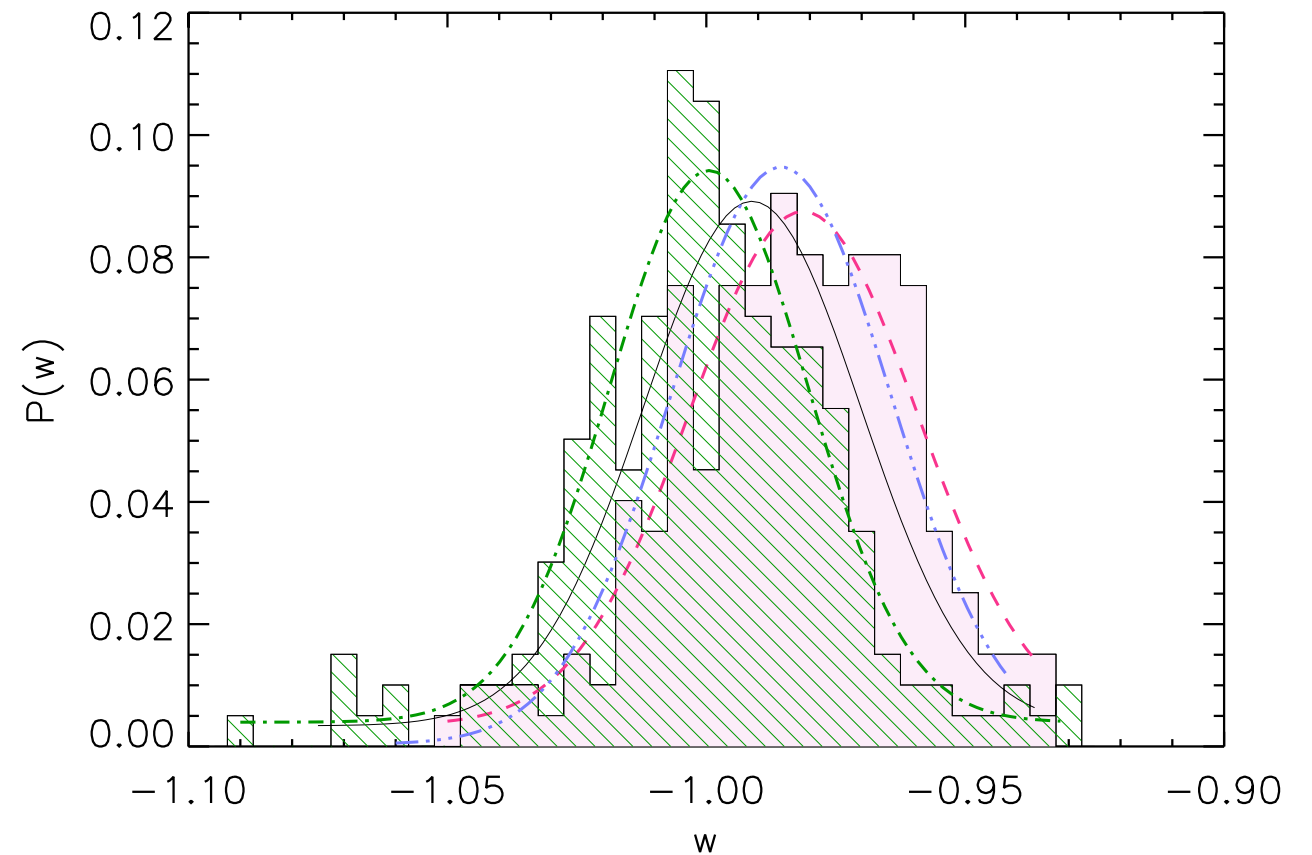

$$W^{len}(r) = -2F(r) \frac{d_A(r_s - r)}{d_A(r) d_A(r_s)}$$



# Uncertainty in Star Formation: Bias in “w”



Delayed Fraction

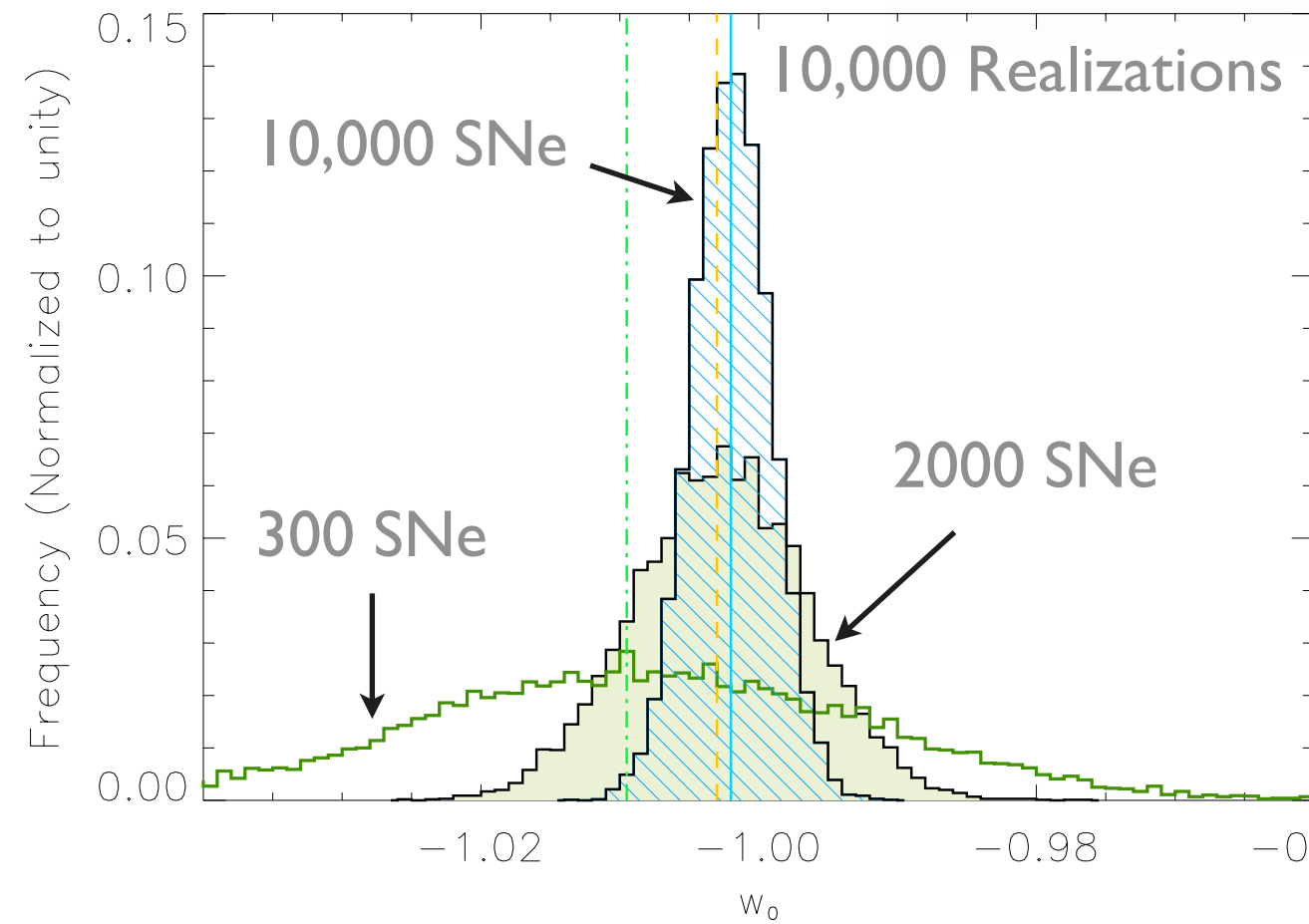


Bias in “w”

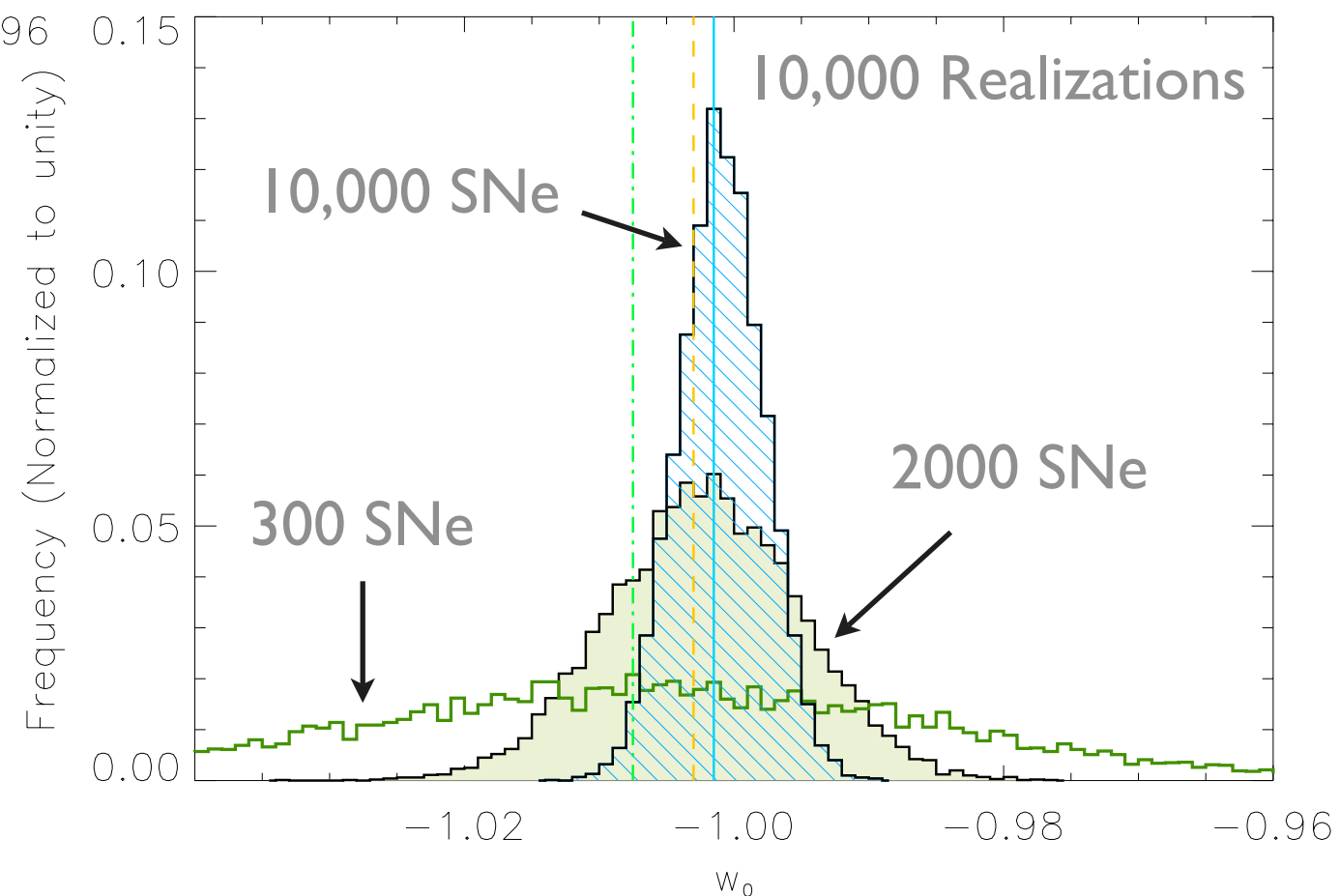
*D.S., A. Amblard, A. Cooray, and D. Holz; ApJL, 684, L13 (2008)*



# Effect of Weak Lensing on Estimates of “w”



*Flux Averaging  
Technique*



*D.S., A. Amblard, D. Holz, A. Cooray; ApJ, 678, 1 (2008)*



# A Little Bit of History

J. E. Gunn and B. M. Tinsley, *Nature*, 257, 454 (1975)

*“New data on the Hubble diagram, combined with constraints on the density of the Universe and the ages of galaxies, suggest that the most plausible cosmological models have a positive cosmological constant, are closed, too dense to make deuterium in the big bang, and will expand for ever. Possible errors in the supporting arguments are discussed.”*

G. Efstathiou, W. J. Sutherland, and S. J. Maddox, *Nature*, 348, 705 (1990)

*“...We argue here that the successes of the CDM theory can be retained and the new observations accommodated in a spatially flat cosmology in which as much as 80% of the critical density is provided by a positive cosmological constant, which is dynamically equivalent to endowing the vacuum with a non-zero energy density. In such a universe, expansion was dominated by CDM until a recent epoch, but is now governed by the cosmological constant ...”*

J. P. Ostriker and P. J. Steinhardt, *Nature*, 377, 600 (1995)

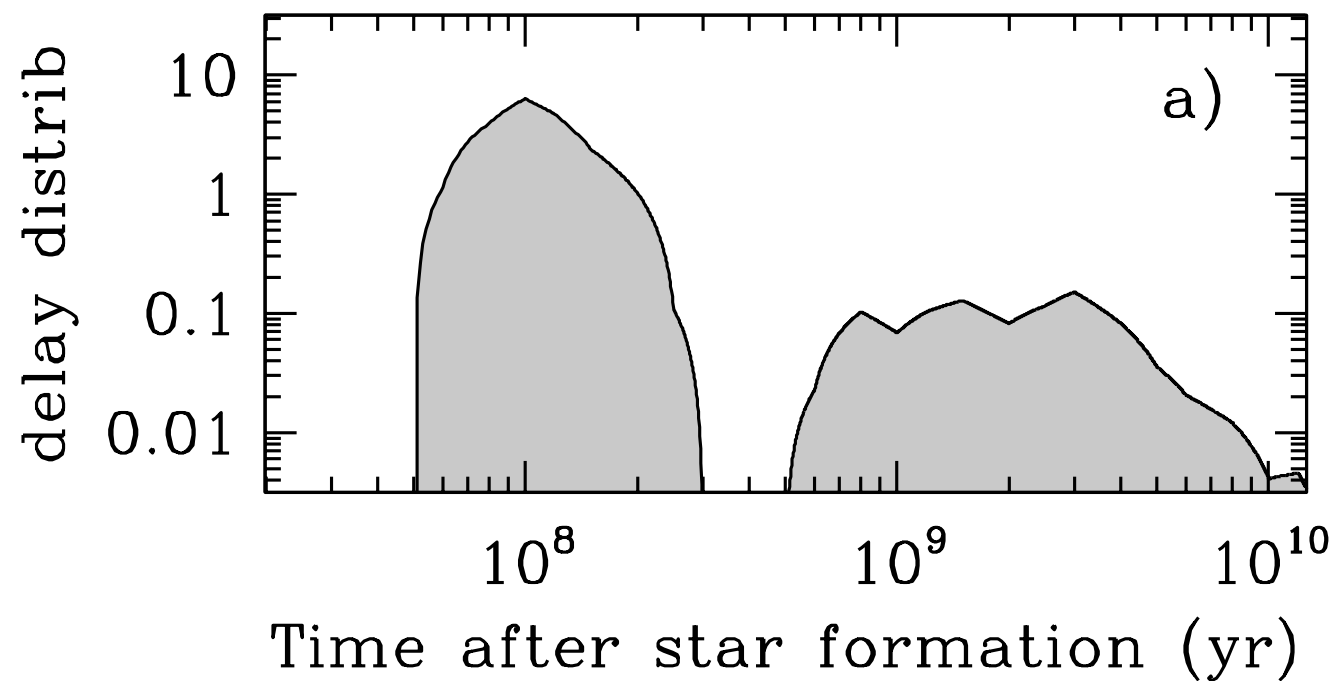
*“OBSERVATIONS are providing progressively tighter constraints on cosmological models advanced to explain the formation of large-scale structure in the Universe ...The observations do not yet rule out the possibility that we live in an ever-expanding open Universe, but a Universe having the critical energy density and a large cosmological constant appears to be favoured.”*

J. S. Bagla, T. Padmanabhan, and J. V. Narlikar, *Comments Astrophys.*, 18, 275 (1996)

*“... the conclusion today is inescapable that the standard big bang models without the cosmological constant are effectively ruled out.”*



# Evolution based on Two SN Populations



Bimodal  
Delay Time Distribution

*Belczynski et al. 2005*

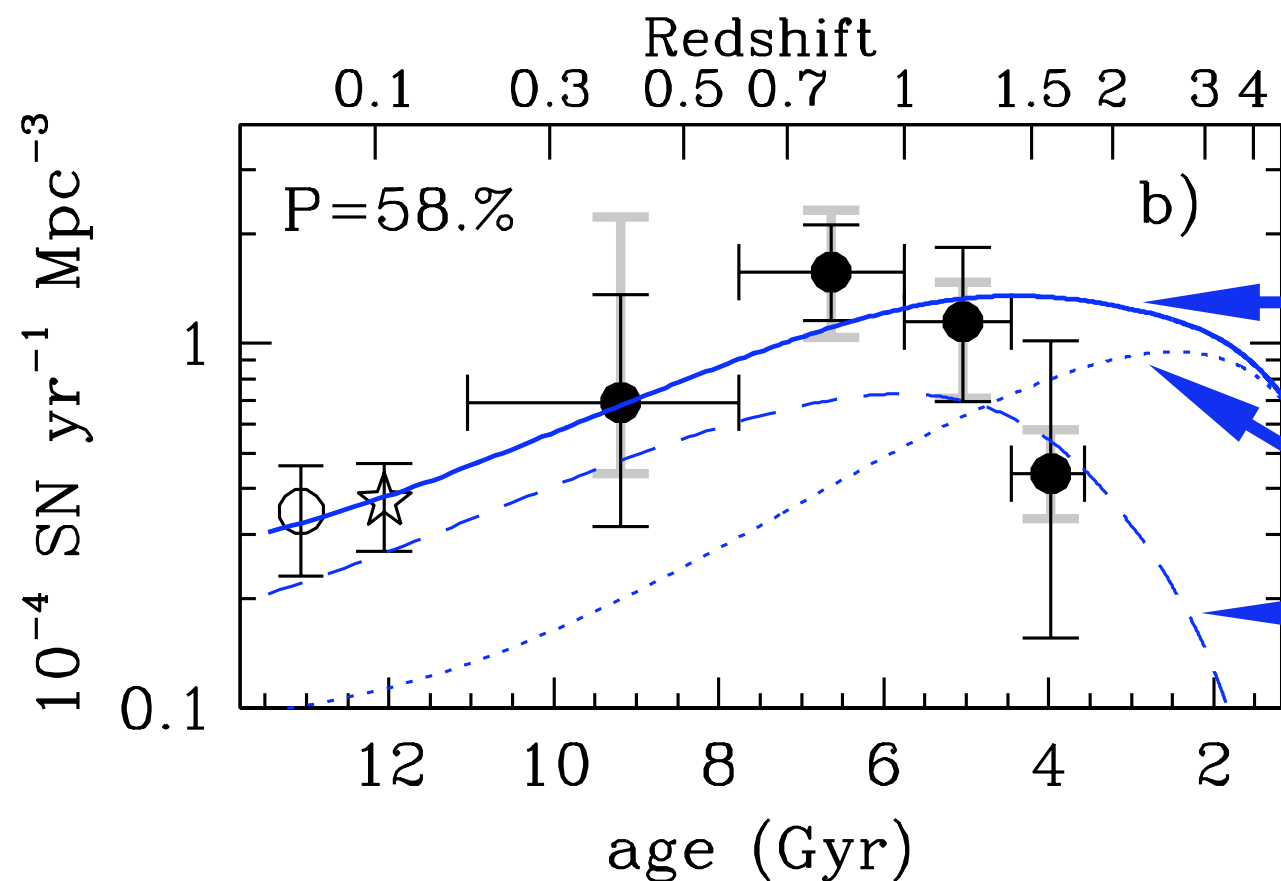
*Mannucci et al. 2006*

Data From:

*Mannucci et al. 2005*

*Strolger et al. 2003*

*Dahlen et al. 2004*



Total

Prompt

Delayed/Extended/Tardy