

# TIDAL STREAMS AS GALACTIC POTENTIOMETERS

DEVDEEP SARKAR  
EXTRAGALACTIC ASTROPHYSICS

February 08, 2007



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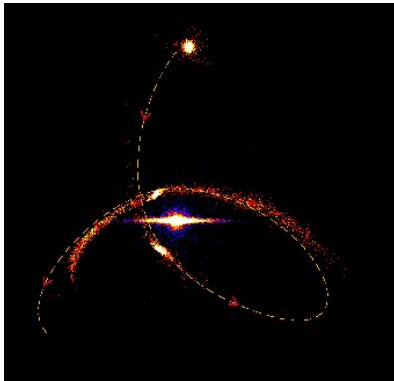
# TIDAL STREAMS

## The Origin and all that...

- Natural by-product of hierarchical structure formation.
- Can be produced along the orbit of a satellite galaxy when stars and/or gas are torn from it by tidal forces from its host.
- The stripped material populates the leading and trailing tidal streams that are aligned with the orbit of the satellite.

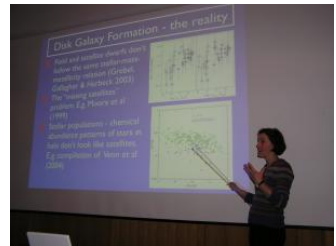


# TIDAL STREAMS



## Tidal Streams around Milky Way

DEVDEEP SARKAR EXTRAGALACTIC ASTROPHYSICS



Kathryn V. Johnston



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## Motivation From Observations

- Several globular clusters known to possess excess unbound stars outside their tidal radii.





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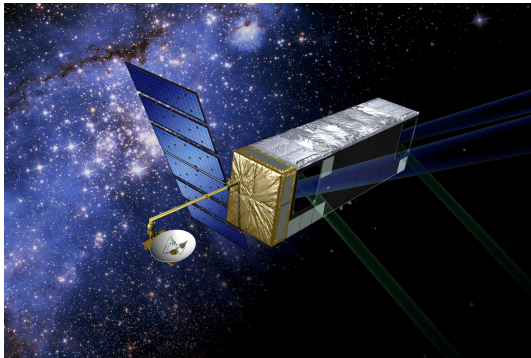
# POTENTIAL POTENTIOMETER?

## Motivation From Observations

- Several globular clusters known to possess excess unbound stars outside their tidal radii.
- Moving groups in the halo with no bound counterparts.
- Discovery of a carbon star trail encircling the Galaxy (Irwin & Totten 1998) provides the first example of data sampling the entire length of a stellar tidal stream.



# POTENTIAL POTENTIOMETER?



(<http://planetquest.jpl.nasa.gov/SIM>)

## Future Observations

Upcoming satellite missions, e.g., SIM, will accurately measure five out of the six phase-space coordinates of a star.



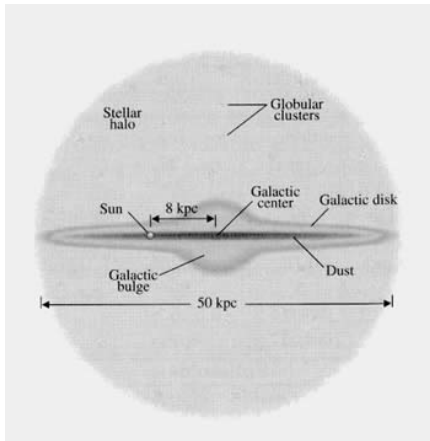
# WHY JOHNSTON ET AL. 1999?

## Exploring the possibilities...

This *letter* investigates, through numerical simulations, the extent to which the potential of the Milky Way can be recovered using a data set such as the carbon star stream (Irwin & Totten 1998) and assuming that phase-space positions can be inferred with accuracy of SIM satellite.



# MODELING THE GALAXY



## Three Component Model for MW

- The Disk
- The Spheroid
- The Halo



# MODELING THE GALAXY

## The Spheroid (Hernquist 1990)

$$\Phi_{spheroid} = -\frac{GM_{spheroid}}{r + c}$$

## The (Old!) Halo

$$\Phi_{halo} = v_{halo}^2 \ln(r^2 + d^2)$$

- The Three-Component Model as Presented in Spergel 1996 and Johnston et al. 1996.

## The Disk (Miyamoto-Nagai 1975)

$$\Phi_{disk} = \frac{GM_{disk}}{\sqrt{R^2 + \left(a + \sqrt{z^2 + b^2}\right)^2}}$$



# MODELING THE GALAXY

## The (NEW!) *Oblate* and *Triaxial* Halo

$$\Phi_{halo}(x, y, z) = \frac{v_{circ}^2}{2} \ln(x^2 + \frac{y^2}{p^2} + \frac{z^2}{q^2} + c^2)$$

## The Disk (Miyamoto-Nagai 1975)

$$\Phi_{disk} = \frac{GM_{disk}}{\sqrt{R^2 + \left(a + \sqrt{z^2 + b^2}\right)^2}}$$

- The Model as Presented in Johnston et al. 1999.

## The Spheroid (Hernquist 1990)

$$\Phi_{spheroid} = -\frac{GM_{spheroid}}{r + c}$$



# MODELING THE SATELLITES

## Assumptions

- 1 Since the satellite mass is much smaller than the MW, *dynamical friction* and *energy exchange* are assumed negligible.

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# MODELING THE SATELLITES

## Assumptions

- 1 Since the satellite mass is much smaller than the MW, *dynamical friction* and *energy exchange* are assumed negligible.
- 2 Interactions between the satellites will occur infrequently so that the evolution of each satellite can be considered independently.

(Johnston et al. 1996)



# MODELING THE SATELLITES

## Evolution of $10^4$ Particles

- Each satellite is modeled with a collection of  $10^4$  self-gravitating particles whose mutual interactions are calculated using a self-consistent field code (Hernquist & Ostriker 1992).
- The particles are initially distributed as a **Plummer model** and let evolve in a MW-potential for 10 Gyr.

## Plummer (1911) Model

$$\Phi = -\frac{GM}{\sqrt{r^2 + r_0^2}}$$



# ENERGY DISTANCES

## Tidal Radius

$$r_{\text{tide}} = R \left( \frac{m_{\text{sat}}}{M_R} \right)^{1/3}$$

## Orbital Energies $E$ of Material

$$\epsilon = r_{\text{tide}} \frac{d\Phi}{dR} = r_{\text{tide}} \frac{GM_R}{R^2}$$

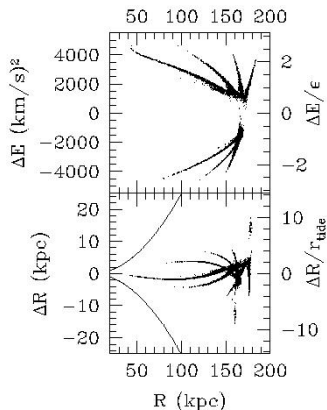
of satellite's orbital energy  $E_{\text{sat}}$ .

## Pericenter!

These equations should be evaluated at the pericenter of the satellite's orbit since most of the mass loss will occur where the tidal field of the Milky Way is strongest.



# ENERGY DISTANCES



(Johnston et al. 1999)

## Distance Estimates

$$E = \frac{1}{2} [v_{los}^2 + d^2 (\mu_l^2 + \mu_b^2)] + \Phi_{MW}$$

## Result from Simulation 11

Energy offset  $\mp 5\epsilon/4$  from  $E_{sat}$ .

Distance estimate to within few  $r_{tide}$ .



# CONSTRAINING GALACTIC POTENTIAL

## The Algorithm

Johnston et al. (1999)



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- For each assumed potential, integrate the satellite's orbit backward and calculate  $r_{tide}$  and  $\epsilon$  at the pericenter.

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- For each assumed potential, integrate the satellite's orbit backward and calculate  $r_{tide}$  and  $\epsilon$  at the pericenter.
- For each star in the debris with  $l$ ,  $b$ ,  $\mu_l$ ,  $\mu_b$ , and  $v_{los}$ :

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  - create  $n_{test}$  particles with energies  $E$  in the range  $\pm 3\epsilon/4$  about  $(E_{sat} \mp 5\epsilon/4)$  if the star is ahead/behind the satellite

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  - estimate the “energy distance” to each particle
  - integrate backward in time for a Galactic lifetime

Johnston et al. (1999)



# CONSTRAINING GALACTIC POTENTIAL

## The Algorithm (cont'd...)

- For each star in the debris with  $l$ ,  $b$ ,  $\mu_l$ ,  $\mu_b$ , and  $v_{los}$ :
  - credit the potential with a “capture” whenever any of these particles is separated by  $dr < 1.8r_{tide}$  and a velocity  $dv < (Gm_{sat}/dr)^{1/2}$ .

Johnston et al. (1999)



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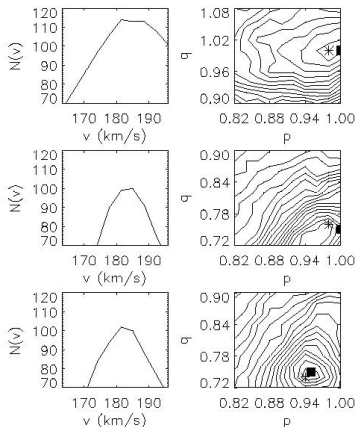
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- Assign the potential's “score” as the number of successful captures.
- The potential having the highest score is the most likely one!

Johnston et al. (1999)



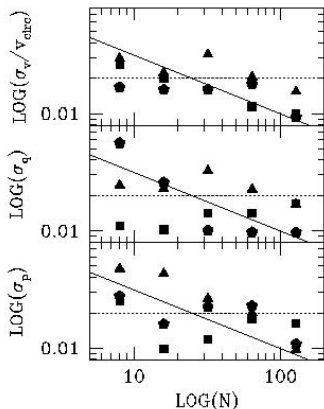
# SIMULATION RESULTS



## Recaptured Particles

*Left-hand panels:* Maximum number of captured particles for fixed  $v_{circ}$  and arbitrary  $q$ ,  $p$ . *Right-hand panels:* Maximum number of rebound particles contoured in the  $p$ - $q$  plane for the most likely value of  $v_{circ}$  from the left-hand panels.

# SIMULATION RESULTS



## Dispersion

$$\sigma_w = (\langle w^2 \rangle - \langle w \rangle^2)^{1/2}$$

Bootstrapped errors in the potential calculated with  $N$  stars. The solid line is given by  $\sigma_w = 1/10\sqrt{N}$ . The dotted line shows the size of one cell of the gridded distribution from which  $\sigma_w$  was calculated.



(Johnston et al. 1999)

# WHAT HAVE WE LEARNT?

## From Johnston et al. (1999)...

- Use of SIM measurements of stars in tidal streams to probe the Galactic potential seems promising.
- The 5D phase-space information for only 100 stars can be used to determine the circular velocity and shape of the Galactic halo with accuracies of a few percent...more than an order-of-magnitude improvement in our knowledge about MW's mass distribution.

## cont'd...

However, discussion has been limited to four-parameter model...uncertainty will increase with the number of parameters varied.





# FROM P241C TO ...

-  K. V. Johnston, L. Hernquist, & M. Bolte; ApJ, 465, 278 (1996)
-  K. V. Johnston, H. Zhao, D. N. Spergel, & L. Hernquist; ApJ, 512, 109 (1999)
-  C. Murali & J. Dubinski; ApJ, 118, 911 (1999)
-  R. Ibata, G. F. Lewis, M. Irwin, E. Totten, & T. Quinn; ApJ, 551, 294 (2001)
-  C. Grillmair & R. Johnson; ApJ, 639, 17 (2006)
-  YOU (2007? 2014?)

